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# **Tamaas Documentation**

*Release 0+untagged.56.g13bcf0c*

**Lucas Frérot**

**Jun 08, 2026**



## TABLE OF CONTENTS:

<b>1</b>	<b>Library overview</b>	<b>3</b>
1.1	Tutorials . . . . .	3
1.2	Citations . . . . .	3
1.3	Changelog . . . . .	4
1.4	Seeking help . . . . .	4
1.5	Contribution . . . . .	4
<b>2</b>	<b>Quickstart</b>	<b>5</b>
2.1	Installation from PyPI . . . . .	5
2.2	Installation with Spack . . . . .	5
2.3	Docker image . . . . .	6
2.4	Singularity container . . . . .	7
2.5	Installation from source . . . . .	7
2.6	Building the docs . . . . .	9
2.7	Running the contact pipe tools . . . . .	9
2.8	Running the tests . . . . .	10
<b>3</b>	<b>Random rough surfaces</b>	<b>11</b>
3.1	Generating a surface . . . . .	11
3.2	Custom filter . . . . .	12
3.3	Surface Statistics . . . . .	13
<b>4</b>	<b>Model and integral operators</b>	<b>15</b>
4.1	Units in Tamaas . . . . .	15
4.2	Model types . . . . .	15
4.3	Model creation and basic functionality . . . . .	16
4.4	Integral operators . . . . .	18
4.5	Model dumpers . . . . .	19
<b>5</b>	<b>Solving contact</b>	<b>21</b>
5.1	Elastic contact . . . . .	21
5.2	Contact with adhesion . . . . .	22
5.3	Viscoelastic contact . . . . .	23
5.4	Tangential contact . . . . .	24
5.5	Elasto-plastic contact . . . . .	24
5.6	Using PETSc Solvers . . . . .	26
5.7	Custom Contact Solvers . . . . .	26
<b>6</b>	<b>Working with MPI</b>	<b>27</b>
6.1	Transparent MPI context . . . . .	27
6.2	MPI convenience methods . . . . .	29

<b>7</b>	<b>Examples</b>	<b>31</b>
<b>8</b>	<b>Performance</b>	<b>33</b>
8.1	Parallelism . . . . .	33
8.2	Integration algorithm . . . . .	34
8.3	Computational methods & Citations . . . . .	34
<b>9</b>	<b>Frequently Asked Questions</b>	<b>37</b>
9.1	Importing <code>tamaas</code> module gives a circular import error on Windows . . . . .	37
9.2	What are the units in Tamaas? . . . . .	37
9.3	Do contact solvers solve for a total force or an average pressure? . . . . .	37
9.4	<code>scons dev</code> fails to install Tamaas with <code>externally-managed-environment</code> error . . . . .	37
<b>10</b>	<b>Developer documentation</b>	<b>39</b>
10.1	Documentation . . . . .	39
10.2	Writing code . . . . .	39
10.3	Running tests . . . . .	40
10.4	Git workflow . . . . .	40
<b>11</b>	<b>API Reference</b>	<b>41</b>
11.1	Python API . . . . .	41
11.2	C++ API . . . . .	73
<b>12</b>	<b>Indices and tables</b>	<b>203</b>
	<b>Python Module Index</b>	<b>205</b>

JOSS [10.21105/joss.02121](https://doi.org/10.21105/joss.02121)

 [launch binder](#)

Tamaas (from *تامت* meaning “contact” in Arabic and Farsi) is a high-performance rough-surface periodic contact code based on boundary and volume integral equations. The clever mathematical formulation of the underlying numerical methods (see e.g. [doi:10.1007/s00466-017-1392-5](https://doi.org/10.1007/s00466-017-1392-5) and [arxiv:1811.11558](https://arxiv.org/abs/1811.11558)) allows the use of the fast-Fourier Transform, a great help in achieving peak performance: Tamaas is consistently *two orders of magnitude faster* (and lighter) than traditional FEM! Tamaas is aimed at researchers and practitioners wishing to compute realistic contact solutions for the study of interface phenomena.

You can see Tamaas in action with our interactive [tutorials](#).



## LIBRARY OVERVIEW

Tamaas is mainly composed of three components:

- Random surface generation procedures
- Model state objects and operators
- Contact solving procedures

These parts are meant to be independent as well as inter-operable. The first one provides an interface to several stochastic surface generation algorithms described in *Random rough surfaces*. The second provides an interface to a state object *Model* (and C++ class `tamaas::Model`) as well as integral operators based on the state object (see *Model and integral operators*). Finally, the third part provides contact solving routines that make use of the integral operators for performance (see *Solving contact*).

### 1.1 Tutorials

The following tutorial notebooks can also be used to learn about Tamaas:

- Elastic Contact ([live notebook](#), [notebook viewer](#))
- Rough Surfaces ([live notebook](#), [notebook viewer](#))

### 1.2 Citations

Tamaas is the fruit of a research effort. To give proper credit to its creators and the scientists behind the methods it implements, you can use the `tamaas.utils.publications()` function at the end of your python scripts. This function scans global variables and prints the relevant citations for the different capabilities of Tamaas used. Note that it may miss citations if some objects are not explicitly stored in named variables, so please examine the relevant publications in [doi:10.21105/joss.02121](https://doi.org/10.21105/joss.02121).

## 1.3 Changelog

The changelog can be consulted [here](#).

## 1.4 Seeking help

You can ask your questions on [gitlab](#) using this [form](#). If you do not have an account, you can create one [on this page](#).

## 1.5 Contribution

Contributions to Tamaas are welcome, whether they are code, bug, or documentation related. Please have a read at the *Developer documentation*.

### 1.5.1 Code

Please [fork Tamaas](#) and [submit your patch](#) as a merge request.

### 1.5.2 Bug reports

You can also contribute to Tamaas by reporting any bugs you find [here](#) if you have an account on [gitlab](#). Please read the *FAQ* before posting.

## QUICKSTART

Here is a quick introduction to get you started with Tamaas.

### 2.1 Installation from PyPI

If you have a Linux system, or have installed the [Windows Subsystem for Linux](#), you can simply run `python3 -m pip install tamaas`. This installs the latest stable version of Tamaas from [PyPI](#). You can get the latest cutting-edge build of Tamaas with:

```
python3 -m pip install \
  --extra-index-url https://gitlab.com/api/v4/projects/19913787/packages/pypi/simple \
  tamaas
```

---

**Note:** To limit the number of statically linked dependencies in the wheel package, the builds that can be installed via PyPI or the GitLab package registry do not include parallelism or architecture specific optimizations. If you want to execute Tamaas in parallel, or want to improve performance, it is highly recommended that you install with Spack or compile from source with the instructions below.

---

### 2.2 Installation with Spack

If you have [Spack](#) installed (e.g. in an HPC environment), you can install Tamaas with the following:

```
spack install tamaas
```

This will install an MPI-enabled version of tamaas with Scipy solvers. The command `spack info tamaas` shows the build variants. To disable MPI, you should disable MPI in the FFTW variant:

```
spack install tamaas ^fftw~mpi
```

The Spack package for Tamaas allows installation from the repository with `spack install tamaas@master`.

You can also use Spack to create container recipes with `spack containerize`. Here's an example `spack.yaml` for Tamaas which creates an image with OpenMPI and NetCDF so that Tamaas can be executed in parallel within the container with [Singularity](#):

```
spack:
  config:
    build_jobs: 2
```

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```

specs:
- matrix:
  - [py-mpi4py, py-netcdf4, tamaas@master+solvers]
  - ["^openmpi@4 fabrics=ofi,psm2,ucx schedulers=none"]
concretizer:
  unify: true
container:
  format: singularity
  images:
  os: ubuntu:20.04
  spack: develop
  os_packages:
  final:
    - gfortran

```

## 2.3 Docker image

We provide Docker images that are automatically built and pushed to the Gitlab registry for compatibility reasons (mainly with macOS). To get the latest image simply run:

```

docker pull registry.gitlab.com/tamaas/tamaas
# to rename for convenience
docker tag registry.gitlab.com/tamaas/tamaas tamaas

```

Then you can run scripts directly:

```

docker run -v $PWD:/app -t tamaas python3 /app/your_script.py
# or
docker run tamaas tamaas surface --sizes 16 16 --cutoffs 4 4 8 --hurst 0.8 | docker_
↪run -i tamaas tamaas contact 0.1 > results.npy

```

**Warning:** The provided Docker image and Dockerfile offer limited customization options and are hard-wired to use OpenMPI. If the use case/goal is to run in HPC environments, containers generated with Spack should be preferred, as they allow greater flexibility in the dependency selection and installed packages.

The Dockerfile at the root of the Tamaas repository can be used to build an image containing Tamaas with a full set of dependencies and customize the build options. Simply run:

```

docker build -t tamaas .

```

**Tip:** The following arguments can be passed to docker to customize the Tamaas build (with the `--build-arg` flag for `docker build`):

- `BACKEND`: parallelism model for loops
- `FFTW_THREADS`: parallelism model for FFTW3
- `USE_MPI`: compile an MPI-parallel version of Tamaas

See below for explanations.

## 2.4 Singularity container

A `singularity` container can be created from the docker image with:

```
singularity build tamaas.sif docker://registry.gitlab.com/tamaas/tamaas
```

To run the image with MPI:

```
mpirun singularity exec --home=$PWD tamaas.sif python3 <your_script>
```

## 2.5 Installation from source

First make sure the following dependencies are installed for Tamaas:

- a **C++ compiler** with full **C++14** and **OpenMP** support
- **SCons** (python build system)
- **FFTW3**
- **thrust** (1.9.2+)
- **boost** (pre-processor)
- **python 3+** with **numpy**
- **pybind11** (included as submodule)
- **expolit** (included as submodule)

Optional dependencies are:

- an MPI implementation
- **FFTW3** with MPI/threads/OpenMP (your pick) support
- **scipy** (for nonlinear solvers)
- **uvw**, **h5py**, **netCDF4** (for dumpers)
- **googletest** and **pytest** (for tests)
- **Doxygen** and **Sphinx** (for documentation)

---

**Tip:** On a HPC environment, use the following variables to specify where the dependencies are located:

- `FFTW_ROOT`
- `THRUST_ROOT`
- `BOOST_ROOT`
- `PYBIND11_ROOT`
- `GTEST_ROOT`

---

**Note:** You can use the provided Dockerfile to build an image with the external dependencies installed.

---

You should first clone the git repository with the submodules that are dependencies to tamaas (`pybind11` and `googletest`):

```
git clone --recursive https://gitlab.com/tamaas/tamaas.git
```

The build system uses [SCons](#). In order to compile Tamaas with the default options:

```
scons
```

After compiling a first time, you can edit the compilation options in the file `build-setup.conf`, or alternatively supply the options directly in the command line:

```
scons option=value [...]
```

To get a list of **all** build options and their possible values, you can run `scons -h`. You can run `scons -H` to see the SCons-specific options (among them `-j n` executes the build with `n` threads and `-c` cleans the build). Note that the build is aware of the `CXX` and `CXXFLAGS` environment variables.

Once compiled, you need to create a [virtual environment](#) (see [Frequently Asked Questions](#)), then install with:

```
scons install prefix=/your/virtual_env
```

The above command automatically calls `pip` if it is installed. If want to install an editable package for development, run:

```
scons dev
```

This is equivalent to running `pip install -e build-release/python[all]`. You can check that everything is working fine with:

```
python3 -c 'import tamaas; print(tamaas)'
```

## 2.5.1 Important build options

Here are a selected few important compilation options:

### **build\_type**

Controls the type of build, which essentially changes the optimisation level (`-O0` for debug, `-O2` for profiling and `-O3` for release) and the amount of debug information. Default type is `release`. Accepted values are:

- `release`
- `debug`
- `profiling`

### **CXX**

Compiler (uses the environment variable `CXX` by default).

### **CXXFLAGS**

Compiler flags (uses the environment variable `CXXFLAGS` by default). Useful to add tuning flags (e.g. `-march=native` `-mtune=native` for GCC or `-xHOST` for Intel), or additional optimisation flags (e.g. `-flto` for link-time optimization).

### **backend**

Controls the Thrust parallelism backend. Defaults to `omp` for OpenMP. Accepted values are:

- `omp`: OpenMP
- `cpp`: Sequential
- `tbb` (unsupported): Threading Building Blocks

**fftw\_threads**

Controls the FFTW thread model. Defaults to `omp` for OpenMP. Accepted values are:

- `omp`: OpenMP
- `threads`: PThreads
- `none`: Sequential

**use\_mpi**

Activates MPI-parallelism (boolean value).

**use\_petsc**

Activates PETSc solvers for non-linear problems and contact.

More details on the above options can be found in [Performance](#).

## 2.6 Building the docs

Documentation is built using `scons doc`. Make sure to have the correct dependencies installed (they are already provided in the Docker image).

## 2.7 Running the contact pipe tools

Once installed, the python package provides a `tamaas` command, which defines three subcommands that can be used to explore the mechanics of elastic rough contact:

- `surface` generates randomly rough surfaces (see [Random rough surfaces](#))
- `contact` solves an elastic contact problem with a surface read from `stdin` (see [Solving contact](#))
- `volume` reads a 2D model from `stdin` (Numpy format) and computes volumetric displacement, strain and stress. Outputs a model object to `stdout`
- `convert` converts a model in Numpy format to another file format (e.g. VTK Rectangular grid, with `UVW`)
- `plot` plots the 2D normal surface tractions and displacements read from `stdin`

Here's a sample command line for you to try out:

```
tamaas surface --cutoffs 2 4 64 --size 512 512 --hurst 0.8 | tamaas contact 1 > model_
↪2d.npz
tamaas plot < model_2d.npz
tamaas volume 0.3 16 < model_2d.npz | tamaas convert vtk > model_3d.vtr
```

Check out the help of each command (e.g. `tamaas surface -h`) for a description of the arguments.

## 2.8 Running the tests

You need to activate the `build_tests` option to compile the tests:

```
scons build_tests=True
```

Tests can then be run with the `scons test` command. Make sure you have [pytest](#) installed.

## RANDOM ROUGH SURFACES

The generation of stochastically rough surfaces is controlled in Tamaas by two abstract classes: `tamaas::SurfaceGenerator` and `tamaas::Filter`. The former provides access lets the user set the surface sizes and random seed, while the latter encodes the information of the spectrum of the surface. Two surface generation methods are provided:

- `tamaas::SurfaceGeneratorFilter` implements a Fourier filtering algorithm (see [Hu & Tonder](#)),
- `tamaas::SurfaceGeneratorRandomPhase` implements a random phase filter.

Both of these rely on a `tamaas::Filter` object to provided the filtering information (usually power spectrum density coefficients). Tamaas provides two such classes and allows for Python subclassing:

- `tamaas::Isopowerlaw` provides a roll-off powerlaw,
- `tamaas::RegularizedPowerlaw` provides a powerlaw with a regularized rolloff.

Tamaas also provided routines for surface statistics.

### 3.1 Generating a surface

Let us now see how to generate a surface. Frist create a filter object and set the surface sizes:

```
import tamaas as tm

# Create spectrum object
spectrum = tm.Isopowerlaw2D()

# Set spectrum parameters
spectrum.q0 = 4
spectrum.q1 = 4
spectrum.q2 = 32
spectrum.hurst = 0.8
```

The `spectrum` object can be queried for information, such as the root-mean-square of heights, the various statistical moments, the spectrum bandwidth, etc. Then we create a generator object and build the random surface:

```
generator = tm.SurfaceGeneratorFilter2D([128, 128])
generator.spectrum = spectrum
generator.random_seed = 0

surface = generator.buildSurface()
```

---

**Important:** The surface object is a `numpy.ndarray` wrapped around internal memory in the generator object, so a subsequent call to `buildSurface` may change its content. Note that if `generator` goes out of scope its

memory will not be freed if there is still a live reference to the surface data.

---

**Important:** If ran in an MPI context, the constructor of `SurfaceGeneratorFilter2D` (and others) expects the *global* shape of the surface. The shape can also be changed with `generator.shape = [64, 64]`.

---

It is common to normalize a surface after it has been generated so that one can scale the surface to a desired statistic, e.g. to specify the root-mean-square of slopes:

```
rms_slopes = 0.25
surface /= iso.rmsSlopes()
surface *= rms_slopes

# Compute root-mean-square of slopes in Fourier domain
print(tm.Statistics2D.computeSpectralRMSSlope(surface))
# Compute root-mean-square of slopes with finite differences
# (introduces discretization error)
print(tm.Statistics2D.computeFDRMSSlope(surface))
```

**Note:** The spectrum object gives the expected value of surface statistics, but the corresponding value for a surface realization can differ (particularly if the `SurfaceGeneratorFilter2D` is used). One could normalize a surface with the *actual* statistic, but this leads to **biased** quantities when a representative sample of surfaces is used.

---

## 3.2 Custom filter

Tamaas provides several classes that can be derived directly with Python classes, and `tamaas::Filter` is one of them. Since it provides a single pure virtual method `computeFilter`, it is easy to write a sub-class. Here we implement a class that takes a user-defined auto-correlation function and implements the `computeFilter` virtual function:

```
import numpy

class AutocorrelationFilter(tm.Filter2D):
    def __init__(self, autocorrelation):
        tm.Filter2D.__init__(self)
        self.autocorrelation = autocorrelation.copy()

    def computeFilter(self, filter_coefficients):
        shifted_ac = numpy.fft.ifftshift(self.autocorrelation)

        # Fill in the PSD coefficients
        filter_coefficients[...] = numpy.sqrt(np.fft.rfft2(shifted_ac))
        # Normalize
        filter_coefficients[...] *= 1 / numpy.sqrt(self.autocorrelation.size)
```

Here `filter_coefficients` is also a `numpy.ndarray` and is therefore easily manipulated. The creation of the surface then follows the same pattern as previously:

```
# Create spectrum object
autocorrelation = ... # set your desired autocorrelation
spectrum = AutocorrelationFilter(autocorrelation)
```

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```

generator = tm.SurfaceGenerator2D()
generator.shape = autocorrelation.shape
generator.spectrum = spectrum

surface = generator.buildSurface()

```

The lifetime of the `spectrum` object is associated to the generator when `setSpectrum` is called.

### 3.3 Surface Statistics

Tamaas provides the C++ class `tamaas::Statistics` and its wrapper `Statistics2D` to compute statistics on surfaces, including:

- power spectrum density
- autocorrelation
- spectrum moments
- root-mean-square of heights  $\sqrt{\langle h^2 \rangle}$
- root-mean-square of slopes (computed in Fourier domain)  $\sqrt{\langle |\nabla h|^2 \rangle}$

All these quantities are computed in a discretization-independent manner: increasing the number of points in the surface should not drastically change the computed values (for a given spectrum). This allows to refine the discretization as much as possible to approximate a continuum. Note that the autocorrelation and PSD are fft-shifted. Here is a sample code plotting the PSD and autocorrelation:

```

psd = tm.Statistics2D.computePowerSpectrum(surface)
psd = numpy.fft.fftshift(psd, axes=0) # Shifting only once axis because of R2C
↳transform

import matplotlib.pyplot as plt
from matplotlib.colors import LogNorm

plt.imshow(psd.real, norm=LogNorm())

acf = tm.Statistics2D.computeAutocorrelation(surface)
acf = numpy.fft.fftshift(acf)

plt.figure()
plt.imshow(acf)

plt.show()

```

See `examples/statistics.py` for more usage examples of statistics.



## MODEL AND INTEGRAL OPERATORS

The class `tamaas::Model` (and its counterpart `Model`) is both a central class in Tamaas and one of the simplest. It mostly serves as holder for material properties, fields and integral operators, and apart from a linear elastic behavior does not perform any computation on its own.

### 4.1 Units in Tamaas

All quantities in Tamaas are unitless. To put real units onto them, one can use the following equation, which must have a consistent set of units:

$$\frac{u}{L} = \frac{\pi}{k} \frac{p}{\frac{E}{1-\nu^2}}.$$

It relates the surface displacement  $u$  to the pressure  $p$ , with the Young's modulus  $E$ , the Poisson coefficient  $\nu$  and the *horizontal* physical size of the system  $L$  (i.e. the horizontal period of the system). The wavenumber  $k$  is adimensional. This means that  $L$  is the natural unit for lengths (which can be specified when creating the `Model` object), and  $E^* := E/(1 - \nu^2)$  is the natural unit for pressures (which can be accessed with `model.E_star`). All other units (areas, forces, energies, etc.) are derived from these two units.

In general, it is a good idea to work with a unit set that gives numerical values of the same order of magnitude to minimize floating point errors in algebraic operations. While this is not always possible, because in elastic contact we have  $u \sim h_{\text{rms}}$  and  $p \sim h'_{\text{rms}} E^*$ , which are dependent, one should avoid using meters if expected lengths are nanometers for example.

### 4.2 Model types

`tamaas::Model` has a concrete subclass `tamaas::ModelTemplate` which implements the model function for a given `tamaas::model_type`:

#### **tamaas::basic\_2d**

Model type used in normal frictionless contact: traction and displacement are 2D fields with only one component.

#### **tamaas::surface\_2d**

Model type used in frictional contact: traction and displacement are 2D fields with three components.

#### **tamaas::volume\_2d**

Model type used in elastoplastic contact: tractions are the same as with `tamaas::surface_2d` but the displacement is a 3D field.

The enumeration values suffixed with `_1d` are the one dimensional (line contact) counterparts of the above model types. The domain physical dimension and number of components are encoded in the class `tamaas::model_type_traits`.

## 4.3 Model creation and basic functionality

The instantiation of a `Model` requires the model type, the physical size of the system, and the number of points in each direction:

```
physical_size = [1., 1.]
discretization = [512, 512]
model = tm.Model(tm.model_type.basic_2d, physical_size, discretization)
```

**Warning:** For models of type `volume_*d`, the first component of the `physical_size` and `discretization` arrays corresponds to the depth dimension ( $z$  in most cases). For example:

```
tm.Model(tm.model_type.basic_2d, [0.3, 1, 1], [64, 81, 81])
```

creates a model of depth 0.3 and surface size  $1^2$ , while the number of points is 64 in depth and  $81^2$  on the surface. This is done for data contiguity reasons, as we do discrete Fourier transforms in the horizontal plane.

**Note:** If ran in an MPI context, the constructor to `Model` expects the *global* system sizes and discretization of the model.

**Tip:** Deep copies of model objects can be done with the `copy.deepcopy()` function:

```
import copy
model_copy = copy.deepcopy(model)
```

Note that it only copies fields, not operators or dumpers.

### 4.3.1 Model properties

The properties `E` and `nu` can be used to set the Young's modulus and Poisson ratio respectively:

```
model.E = 1
model.nu = 0.3
```

**Tip:** The Greenwood–Tripp equivalence, sometimes called Johnson equivalence, allows one to model a normal, frictionless contact between two homogeneous linear, isotropic, elastic materials with rough surfaces  $h_\alpha$  and  $h_\beta$  as the contact of a rigid-rough surface  $h_\beta - h_\alpha$  and a flat elastic solid with an equivalent contact modulus  $E^*$ :

$$\frac{1}{E^*} = \frac{1 - \nu_\alpha^2}{E_\alpha^2} + \frac{1 - \nu_\beta^2}{E_\beta^2} = \frac{1}{E_\alpha^*} + \frac{1}{E_\beta^*}$$

Since a model only defines a single set of elastic properties  $(E, \nu)$ , one can model contact between two different elastic materials by computing  $E^*$  *a priori*, and setting  $(E, \nu) = (E^*, 0)$ . The total displacement  $u$  computed by, for example, a contact solver can then be redistributed in proportion according to:

$$\frac{1}{E^*}u = \frac{1}{E_\alpha^*}u_\alpha + \frac{1}{E_\beta^*}u_\beta$$

Note that is equivalence breaks down with friction, plasticity, heterogeneities, anisotropy, etc.

### 4.3.2 Fields

Fields can be easlily accessed with the `[]` operator, similar to Python's dictionaries:

```
surface_traction = model['traction']
# surface_traction is a numpy array
```

To know what fields are available, you can call the `list` function on a model (`list(model)`). You can add new fields to a model object with the `[]` operator: `model['new_field'] = new_field`, which is convenient for dumping fields that are computed outside of Tamaas.

**Note:** The fields `traction` and `displacement` are always registered in models, and are accessible via `model.traction` and `model.displacement`.

A model can also be used to compute stresses from a strain field:

```
import numpy

strain = numpy.zeros(model.shape + [6]) # Mandel--Voigt notation
stress = numpy.zeros_like(strain)

model.applyElasticity(stress, strain)
```

**Tip:** `print(model)` gives a lot of information about the model: the model type, shape, registered fields, and more!

### Manipulating fields

Fields are stored in C-contiguous order. The last dimension of any field is always the vector/tensor components, if the number of components is greater than one. The other dimensions are the space dimensions, in `z`, `x`, (`y`) order for volumetric quantities and `x`, (`y`) for boundary quantities.

**Tip:** To select normal component of the surface displacement of a `volume_2d` model, one can write:

```
model.displacement[0, ..., 2]
```

Symmetric tensors are stored in Mandel–Voigt notation as vectors in the form:

$$\underline{\sigma} = (\sigma_{11}, \sigma_{22}, \sigma_{33}, \sqrt{2}\sigma_{12}, \sqrt{2}\sigma_{13}, \sqrt{2}\sigma_{23}).$$

## 4.4 Integral operators

Integral operators are a central part of Tamaas: they are carefully designed for performance in periodic system. When a *Model* object is used with contact solvers or with a residual object (for plasticity), the objects using the model register integral operators with the model, so the user typically does not have to worry about creating integral operators.

Integral operators are accessed through the *operators* property of a model object. The `[]` operator gives access to the operators, and `list(model.operators)` gives the list of registered operators:

```
# Accessing operator
elasticity = model.operators['hooke']

# Applying operator
elasticity(strain, stress)

# Print all registered operators
print(list(model.operators))
```

---

**Note:** At model creation, these operators are automatically registered:

- `hooke`: Hooke's elasticity law
- `von_mises`: computes Von Mises stresses
- `deviatoric`: computes the deviatoric part of a stress tensor
- `eigenvalues`: computes the eigenvalues of a symmetric tensor field

*Westergaard* operators are automatically registered when *solveNeumann* or *solveDirichlet* are called.

---

### 4.4.1 Additional operators

Tamaas defines operators beyond the default ones listed above, but does not instantiate them by default because they require additional storage. Most are automatically instantiated as needed (e.g. with *Residual*), but the *ModelFactory* class can be used to register these additional operators.

---

**Tip:** Some operators define their own fields, just like a model. For example, the Fourier coefficients are a field of the Westergaard operator.

---

#### HookeField

The *HookeField* operator defines a linear elastic constitutive law with space-dependent property, which is assigned via the `mu` field belonging to the operator:

```
# Register the operator with a name
tm.ModelFactory.registerHookeField(model, 'heterogeneous')

# Function defining the shear modulus
mu = lambda z, x, y: ...

# Assign the shear modulus values
model.operators['heterogeneous']['mu'][:] = mu(z, x, y)
```

## Non-periodic surface operator

The Westergaard operator computes equilibrium surface displacement from normal pressure for a periodic system, but a non-periodic equilibrium computation is possible with the DC-FFT method. The operator is registered with `ModelFactory.registerNonPeriodic`.

## Volume operators

When the model type is `volume_2d`, two volume-based half-space operators are available (with their gradients): the Boussinesq and the Mindlin operators.

The Boussinesq operator acts on a traction field defined on the boundary (i.e. the half-space surface) and constructs a volumetric displacement field in equilibrium with this traction field  $\mathbf{t}$ , with a divergence-free stress. The operator is often referred-to with the symbol  $\mathcal{M}$ , and satisfies:

$$\operatorname{div}(\mathcal{C} : \varepsilon[\mathcal{M}[\mathbf{t}]]) = \mathbf{0}, \quad \text{with} \quad (\mathcal{C} : \varepsilon[\mathcal{M}[\mathbf{t}]]) \cdot \mathbf{n}|_{\text{surface}} = \mathbf{t}$$

The Mindlin operator acts on a volumetric eigenstress field and constructs a displacement field in equilibrium with the eigenstress and with a free surface (i.e. zero traction on the boundary). The operator is often referred to with the symbol  $\mathcal{N}$ , and satisfies:

$$\operatorname{div}(\mathcal{C} : \varepsilon[\mathcal{N}[\tau]]) = -\operatorname{div}(\tau), \quad \text{with} \quad (\mathcal{C} : \varepsilon[\mathcal{N}[\tau]]) \cdot \mathbf{n}|_{\text{surface}} = \mathbf{0}$$

The gradient of these operators computes the strain instead of displacement.

These fields are instantiated with `ModelFactory.registerVolumeOperators`. They have the following names:

- `boussinesq, boussinesq_gradient`
- `mindlin, mindlin_gradient`

## 4.4.2 Scipy Sparse interoperability

Scipy defines an interface for matrix-vector products with the class `scipy.sparse.linalg.LinearOperator`. This interface is implemented by several operators in Tamaas, and can be used easily with the function `scipy.sparse.linalg.aslinearoperator()`:

```
from scipy.sparse.linalg import aslinearoperator

ε = np.ravel(model['strain']) # make one-dimensional
C = aslinearoperator(model.operators['hooke'])
σ = C * ε
```

This makes these linear operators easily composable (with the operators `+`, `-`, `*`) and interoperable with Scipy's sparse linear solvers.

## 4.5 Model dumpers

The submodule `tamaas.dumpers` contains a number of classes to save model data into different formats:

### *UVWDumper*

Dumps a model to VTK format. Requires the UVW python package which you can install with pip:

```
pip install uvw
```

This dumper is made for visualization with VTK based software like [Paraview](#).

#### *NumpyDumper*

Dumps a model to a compressed Numpy file.

#### *H5Dumper*

Dumps a model to a compressed **HDF5** file. Requires the **h5py** package. Saves separate files for each dump of a model.

#### **NetCDFDumper**

Dumps a model to a compressed **NetCDF** file. Requires the **netCDF4** package. Saves sequential dumps of a model into a single file, with the `frame` dimension containing the model dumps.

The dumpers are initialized with a basename and the fields that you wish to write to file (optionally you can set `all_fields` to `True` to dump all fields in the model). By default, each write operation creates a new file in a separate directory (e.g. *UVWDumper* creates a `paraview` directory). To write to a specific file you can use the `dump_to_file` method. Here is a usage example:

```
from tamaas.dumpers import UVWDumper, H5Dumper

# Create dumper
uvw_dumper = UVWDumper('rough_contact_example', 'stress', 'plastic_strain')

# Dump model
uvw_dumper << model

# Or alternatively
model.addDumper(H5Dumper('rough_contact_archive', all_fields=True))
model.addDumper(uvw_dumper)
model.dump()
```

The last `model.dump()` call will trigger all dumpers. The resulting files will have the following hierachy:

```
./paraview/rough_contact_example_0000.vtr
./paraview/rough_contact_example_0001.vtr
./hdf5/rough_contact_archive_0000.h5
```

---

**Important:** Currently, only *H5Dumper* and *NetCDFDumper* support parallel output with MPI.

---

## SOLVING CONTACT

The resolution of contact problems is done with classes that inherit from `tamaas::ContactSolver`. These usually take as argument a `tamaas::Model` object, a surface described by a `tamaas::Grid` or a 2D numpy array, and a tolerance. We will see the specificities of the different solver objects below.

### 5.1 Elastic contact

The most common case is normal elastic contact, and is most efficiently solved with `tamaas::PolonskyKeerRey`. The advantage of this class is that it combines two algorithms into one. By default, it considers that the contact pressure field is the unknown, and tries to minimize the complementary energy of the system under the constraint that the mean pressure should be equal to the value supplied by the user, for example:

```
# ...
solver = tm.PolonskyKeerRey(model, surface, 1e-12)
solver.solve(1e-2)
```

Here the average pressure is  $1e-2$ . The solver can also be instantiated by specifying the the constraint should be on the mean gap instead of mean pressure:

```
solver = tm.PolonskyKeerRey(model, surface, 1e-12, constraint_type=tm.PolonskyKeerRey.
→gap)
solver.solve(1e-2)
```

The contact problem is now solved for a mean gap of  $1e-2$ . Note that the choice of constraint affects the performance of the algorithm.

#### 5.1.1 Non-periodic contact

When the primal type is pressure, it is possible to solve a non-periodic normal contact problem by first registering a non-periodic integral operator (based on the DC-FFT method) then telling the contact solver to use it in its energy functional:

```
tm.ModelFactory.registerNonPeriodic(model, 'dcfft')
solver.setIntegralOperator('dcfft')
solver.solve(1e-2)
```

Note however that the solver still shifts the displacement field so that the gap is everywhere positive and zero in the contact zones. This loses the information of the absolute displacement relative to the initial position of the surface. This can be recovered post-solve with:

```
model.operators['dcfft'](model.traction, model.displacement)
```

The example `nonperiodic.py` shows an Hertzian contact example.

## 5.1.2 Computing solutions for loading sequence

The module `tamaas.utils` defines a convenience function `load_path`, which generates solution models for a sequence of loads. This allows lazy evaluation and reduces boiler-plate:

```
from tamaas.utils import load_path

loads = np.linspace(0.01, 0.1, 10)
for model in load_path(solver, loads):
    ... # do some computation on model, e.g. compute contact clusters
```

The function `load_path` accepts the following optional arguments:

### **verbose**

Prints solver output (i.e. iteration, cost function and error)

### **callback**

A function to call after each solve, before the next load step. Useful for dumping model in generator expressions.

## 5.2 Contact with adhesion

The second algorithm hidden in `tamaas::PolonskyKeerRey` considers the **gap** to be the unknown. The constraint on the mean value can be chosen as above:

```
solver = tm.PolonskyKeerRey(model, surface, 1e-12,
                             primal_type=tm.PolonskyKeerRey.gap,
                             constraint_type=tm.PolonskyKeerRey.gap)

solver.solve(1e-2)
```

The advantage of this formulation is to be able to solve adhesion problems (Rey et al.). This is done by adding a term to the potential energy functional that the solver tries to minimize:

```
adhesion_params = {
    "rho": 2e-3,
    "surface_energy": 2e-5
}

adhesion = tm.ExponentialAdhesionFunctional(surface)
adhesion.setParameters(adhesion_params)
solver.addFunctionalTerm(adhesion)

solver.solve(1e-2)
```

Custom classes can be used in place of the example term here. One has to inherit from `tamaas::Functional`:

```
import numpy

class AdhesionPython(tm.Functional):
    """
    Functional class that extends a C++ class and implements the virtual
```

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```

methods
"""

def __init__(self, rho, gamma):
    super().__init__(self)
    self.rho = rho
    self.gamma = gamma

def computeF(self, gap, pressure):
    return -self.gamma * numpy.sum(np.exp(-gap / self.rho))

def computeGradF(self, gap, gradient):
    gradient += self.gamma * numpy.exp(-gap / self.rho) / self.rho

```

This example is actually equivalent to `tamaas::functional::ExponentialAdhesionFunctional`.

**Tip:** Computing the true contact area properly depends on the primal variable (by default pressure). The function `tm.Statistics2D.contact` helps compute the true contact area correctly in parallel. It can also be given the contact perimeter for a more accurate computation:

```

perimter = np.sum([
    c.perimter for c in tm.FloodFill.getClusters(model.traction > 0, False)
])

area = tm.Statistics2D.contact(model.traction, perimter)

```

Or with the gap as the primal variable:

```

perimeter = np.sum([
    c.perimter for c in tm.FloodFill.getClusters(model['gap'] > 0, False)
])

area = 1. - tm.Statistics2D.contact(model['gap'], perimeter)

```

## 5.3 Viscoelastic contact

The solver class `tamaas::MaxwellViscoelastic` solves the quasi-static problem of a viscoelastic material in contact with a rigid rough surface. The viscoelastic behaviour is described with a [generalized Maxwell model](#), i.e. a parallel assembly of Maxwell elements, with one purely elastic chain, defined by the elastic properties of the `tamaas::Model` object:

```

# Defining the elastic branch (i.e. the behavior at t = ∞)
model.E = 3
model.nu = 0.5

# Characteristic times of the relaxation function
times = [0.1, 1, 10]

# Shear moduli for each branch of the model
shear_moduli = [3, 3/2, 1/3]

# Time step

```

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```

Δt = 1e-3

# Solver instantiation
solver = tm.MaxwellViscoelastic(model, surface, 1e-10,
                               time_step=Δt,
                               shear_moduli=shear_moduli,
                               characteristic_times=times)

# Solve one timestep with given load
solver.solve(load)

```

**Warning:** The time scales of the generalized Maxwell model are **relaxation** time scales. Under a constant normal contact load, the relevant characteristic times are **creep** time scales, which are obtained by multiplying the relaxation time scales by  $E(t = \infty)/E(t = 0)$ .

**Warning:** The current viscoelastic formulation is limited to incompressible (`model.nu = 0.5`) materials.

**Tip:** The viscoelastic solver keeps track of loading and deformation history. Use `solver.reset()` to erase this data and start loading from a rest configuration.

## 5.4 Tangential contact

For frictional contact, several solver classes are available. Among them, `tamaas::Condat` is able to solve a coupled normal/tangential contact problem regardless of the material properties. It however solves an associated version of the Coulomb friction law. In general, the Coulomb friction used in contact makes the problem ill-posed.

Solving a tangential contact problem is not much different from normal contact:

```

mu = 0.3 # Friction coefficient
solver = tm.Condat(model, surface, 1e-12, mu)
solver.max_iter = 5000 # The default of 1000 may be too little
solver.solve([1e-2, 0, 1e-2]) # 3D components of applied mean pressure

```

## 5.5 Elasto-plastic contact

For elastic-plastic contact, one needs three different solvers: an elastic contact solver like the ones described above, a non-linear solver and a coupling solver. The non-linear solvers available in Tamaas are implemented in python and inherit from the C++ class `tamaas::EPSolver`. They make use of the non-linear solvers available in scipy:

### *DFSANESolver*

Implements an interface to `scipy.optimize.root()` with the DFSANE method.

### *NewtonKrylovSolver*

Implements an interface to `scipy.optimize.newton_krylov()`.

These solvers require a residual vector to cancel, the creation of which is handled with `tamaas::ModelFactory`. Then, an instance of `tamaas::EPICSolver` is needed to couple the contact and non-linear solvers for the elastic-plastic contact problem:

```
import tamaas as tm

from tamaas.nonlinear_solvers import DFSANESolver

# Definition of modeled domain
model_type = tm.model_type.volume_2d
discretization = [32, 51, 51] # Order: [z, x, y]
flat_domain = [1, 1]
system_size = [0.5] + flat_domain

# Setup for plasticity
material = tm.materials.IsotropicHardening(model,
                                           sigma_y=0.1 * model.E,
                                           hardening=0.01 * model.E)

residual = tm.Residual(model, material)
epsolver = DFSANESolver(residual)

# ...

csolver = tm.PolonskyKeerRey(model, surface, 1e-12)

epic = tm.EPICSolver(csolver, epsolver, 1e-7, relaxation=0.3)
epic.solve(1e-3)

# or use an accelerated scheme (which can sometimes not converge)

epic.acceleratedSolve(1e-3)
```

By default, `tamaas::EPICSolver::solve()` uses a relaxed fixed point. It can be tricky to make it converge: you need to decrease the relaxation parameter passed as argument of the constructor, but this also hinders the convergence rate. The function `tamaas::EPICSolver::acceleratedSolve()` does not require the tweaking of a relaxation parameter, so it can be faster if the latter does not have an optimal value. However, it is not guaranteed to converge.

Finally, during the first iterations, the fixed point error will be large compared to the error of the non-linear solver. It can improve performance to have the tolerance of the non-linear solver (which is the most expensive step of the fixed point solve) decrease over the iterations. This can be achieved with the decorator class `ToleranceManager`:

```
from tamaas.nonlinear_solvers import ToleranceManager, DFSANESolver

@ToleranceManager(start=1e-2,
                  end=1e-9,
                  rate=1 / 3)
class Solver(DFSANESolver):
    pass

# ...

epsolver = Solver(residual)

# or

epsolver = ToleranceManager(1e-2, 1e-9, 1/3)(DFSANESolver)(residual)
```

## 5.6 Using PETSc Solvers

Two C++ classes in Tamaas interface with PETSc solvers, provided `use_petsc=True` was used at compilation:

- `tamaas::petsc::OptimizationSolver` uses PETSc's Toolkit for Advanced Optimization (TAO) to solve normal contact problems.
- `tamaas::petsc::NonlinearSolver` uses PETSc's SNES interface to solve non-linear problems (e.g. plasticity).

Both classes accept PETSc's command-line parameter lists, so that everything about these solvers can be adjusted at run-time by the user, e.g. the linear solver, the tolerance, the line search strategy, etc.

### 5.6.1 Solving contact

Due to the definition of a standard [quadratic constrained program](#) in TAO, the contact problem solved by `tamaas::petsc::OptimizationSolver` is constrained only by the condition that the gap be non-negative. This means that the average pressure cannot be prescribed. Instead, the contact surface can be uniformly shifted by  $\delta$  to control the contact (positive values of the mean height generally induce larger contact), with contact occurring when:

$$\delta \geq -\sup_x \{h(x) - \langle h \rangle\}$$

## 5.7 Custom Contact Solvers

The `tamaas::ContactSolver` class can be derived in Python so that users can interface with Scipy's `scipy.optimize.minimize()` function or PETSc's solvers accessible in the Python [interface](#). See `examples/scipy_penalty.py` for an example on how to proceed.

## WORKING WITH MPI

Distributed memory parallelism in Tamaas is implemented with `MPI`. Due to the bottleneck role of the fast-Fourier transform in Tamaas' core routines, the data layout of Tamaas is that of `FFTW`. Tamaas is somewhat affected by limitations of `FFTW`, and `MPI` only works on systems with a 2D boundary, i.e. `basic_2d`, `surface_2d` and `volume_2d` model types (which are the most important anyways, since rough contact mechanics can yield different scaling laws in 1D).

The following parts of Tamaas are tested with `MPI`:

- Rough surface generation
- Surface statistics computation
- Contact solvers
- Residual-based solvers for contact with volumetric terms, like plasticity

(with `DFSANECXXSolver`)

- Dumping models with `H5Dumper` and `NetCDFDumper`.

---

**Tip:** One can look at `examples/plasticity.py` for a full example of an elastic-plastic contact simulation that can run in `MPI`.

---

### 6.1 Transparent MPI context

Some parts of Tamaas work transparently with `MPI` and no additional work or logic is needed.

**Warning:** `MPI_Init()` is automatically called when importing the `tamaas` module in Python. While this works transparently most of the time, in some situations, e.g. in Singularity containers, the program can hang if `tamaas` is imported first. It is therefore advised to run `from mpi4py import MPI before import tamaas` to avoid issues.

### 6.1.1 Creating a model

The following snippet creates a model whose global shape is [16, 2048, 2048]:

```
import tamaas as tm

model = tm.Model(tm.model_type.volume_2d,
                 [0.1, 1, 1], [16, 2048, 2048])
print(model.shape, model.global_shape)
```

Running this code with `mpirun -np 3` will print the following (not necessarily in this order):

```
[16, 683, 2048] [16, 2048, 2048]
[16, 682, 2048] [16, 2048, 2048]
[16, 683, 2048] [16, 2048, 2048]
```

Note that the partitioning occurs on the  $x$  dimension of the model (see below for more information on the data layout imposed by FFTW).

### 6.1.2 Creating a rough surface

Similarly, rough surface generators expect a global shape and return the partitioned data:

```
iso = tm.Isopowerlaw2D()
iso.q0, iso.q1, iso.q2, iso.hurst = 4, 4, 32, .5
gen = tm.SurfaceGeneratorRandomPhase2D([2048, 2048])
gen.spectrum = iso

surface = gen.buildSurface()
print(surface.shape, tm.mpi.global_shape(surface.shape))
```

With `mpirun -np 3` this should print:

```
(682, 2048) [2048, 2048]
(683, 2048) [2048, 2048]
(683, 2048) [2048, 2048]
```

### Handling partitioning edge cases

Under certain conditions, FFTW may assign to one or more processes a size of zero to the  $x$  dimension of the model. If that happens, the surface generator will raise a runtime error, which causes a deadlock because it does not exit the processes with zero data. The correct way to handle this edge case is:

```
from mpi4py import MPI

try:
    gen = tm.SurfaceGeneratorRandomPhase2D([128, 128])
except RuntimeError as e:
    print(e)
    MPI.COMM_WORLD.Abort(1)
```

This will correctly kill all processes. Alternatively, `os._exit()` can be used, but one should avoid `sys.exit()`, as it kills the process by raising an exception, which still results in a deadlock.

### 6.1.3 Computing statistics

With a model's data distributed among independent process, computing global properties, like the true contact area, must be done in a collective fashion. This is transparently handled by the *Statistics* class, e.g. with:

```
contact = tm.Statistics2D.contact(model.traction)
```

This gives the correct contact fraction, whereas something like `np.mean(model.traction > 0)` will give a different result on each processor.

### 6.1.4 Nonlinear solvers

The only nonlinear solver (for plastic contact) that works with MPI is *DFSANECXXSolver*, which is a C++ implementation of *DFSANESolver* that works in an MPI context.

---

**Note:** Scipy and Numpy use optimized BLAS routines for array operations, while Tamaas does not, which results in *serial* performance of the C++ implementation of the DF-SANE algorithm being lower than the Scipy version.

---

### 6.1.5 Dumping models

The only dumpers that properly works in MPI are the *H5Dumper* and *NetCDFDumper*. Output is then as simple as:

```
from tamaas.dumpers import H5Dumper
H5Dumper('output', all_fields=True) << model
```

This is useful for doing post-processing separately from the main simulation: the post-processing can then be done in serial.

## 6.2 MPI convenience methods

Not every use case can be handled transparently, but although adapting existing scripts to work in an MPI context can require some work, especially if said scripts rely on numpy and scipy for pre- and post-processing (e.g. constructing a parabolic surface for hertzian contact, computing the total contact area), the module *mpi* provides some convenience functions to make that task easier. The functions *mpi.scatter* and *mpi.gather* can be used to scatter/gather 2D data using the partitioning scheme expected from FFTW (see figure below). The functions *mpi.rank* and *mpi.size* are used to determine the local process rank and the total number of processes respectively.

If finer control is needed, the function *mpi.local\_shape* gives the 2D shape of the local data if given the global 2D shape (its counterpart *mpi.global\_shape* does the exact opposite), while *mpi.local\_offset* gives the offset of the local data in the global *x* dimension. These two functions mirror FFTW's own data distribution functions.

The *mpi* module also contains a function *sequential* whose return value is meant to be used as a context manager. Within the sequential context the default communicator is `MPI_COMM_SELF` instead of `MPI_COMM_WORLD`.

For other MPI functionality not covered by Tamaas that may be required, one can use *mpi4py*, which in conjunction with the methods in *mpi* should handle just about any use case.

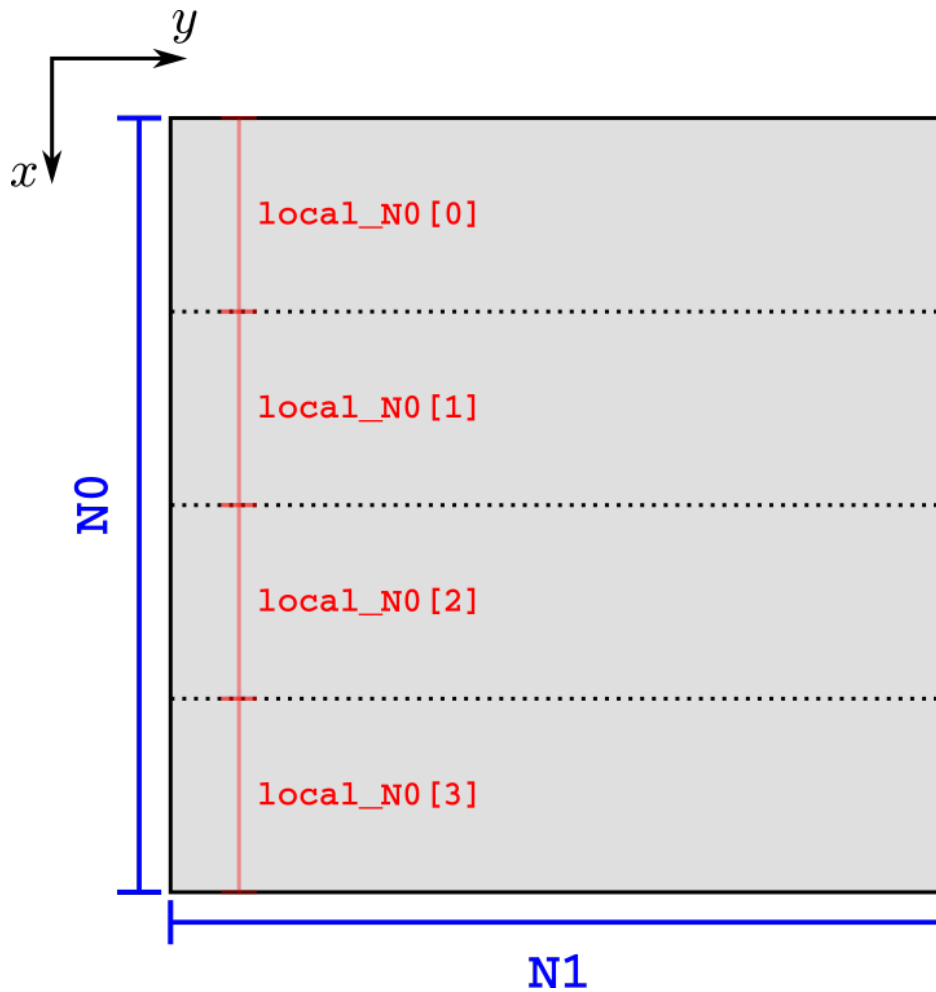


Fig. 1: 2D Data distribution scheme from FFTW.  $N_0$  and  $N_1$  are the number of points in the  $x$  and  $y$  directions respectively. The array `local_N0`, indexed by the process rank, give the local size of the  $x$  dimension. The `local_offset` function gives the offset in  $x$  for each process rank.

## EXAMPLES

The directory `examples/` in Tamaas' root repository contains example scripts dedicated to various aspects of Tamaas:

**`statistics.py`**

This script generates a rough surface and computes its power spectrum density as well as its autocorrelation function.

**`rough_contact.py`**

This script generates a rough surface and solves an adhesion-less elastic contact problem.

**`adhesion.py`**

This script solves a rough contact problem with an exponential energy functional for adhesion. It also shows how to derive an energy functional in python.

**`saturation.py`**

This script solves a saturated contact problem (i.e. pseudo-plasticity) with a rough surface.

**`stresses.py`**

This script solves an equilibrium problem with an eigenstrain distribution and a surface traction distribution and writes the output to a VTK file. It demonstrates how the integral operators that Tamaas uses internally for elastic-plastic contact can be used directly in Python.

**`plasticity.py`**

This script solves an elastoplastic Hertz contact problem with three load steps and writes the result to VTK files.

**`scipy_penalty.py`**

This script shows how to implement a contact solver in python that uses the contact functionals of Tamaas. Here we use Scipy's `scipy.optimize.minimize()` function to solve a contact problem with penalty.

**`nonperiodic.py`**

This script shows how to solve a non-periodic problem and compute the true surface interference

**`viscoelastic_contact.py`**

This script solves a viscoelastic contact problem with a rough surface.



## PERFORMANCE

### 8.1 Parallelism

Tamaas implements shared-memory parallelism using `thrust`. The Thrust backend can be controlled with the following values of the `backend` build option:

**omp**

Thrust uses its OpenMP backend (the default). The number of threads is controlled by OpenMP.

**cpp**

Thrust does not run in threads (i.e. sequential). This is the recommended option if running multiple MPI tasks.

**tbb**

Thrust uses its `TBB` backend. Note that this option is not fully supported by Tamaas.

---

**Tip:** When using the OpenMP or TBB backend, the number of threads can be manually controlled by the `initialize` function. When OpenMP is selected for the backend, the environment variable `OMP_NUM_THREADS` can also be used to set the number of threads.

---

FFTW has its own system for thread-level parallelism, which can be controlled via the `fftw_threads` option:

**none**

FFTW does not use threads.

**threads**

FFTW uses POSIX/Win32 threads for parallelism.

**omp**

FFTW uses OpenMP.

---

**Note:** As with the Thrust backend, the number of threads for FFTW can be controlled with `initialize`.

---

Finally, the boolean variable `use_mpi` controls whether Tamaas is compiled with MPI-parallelism. If yes, Tamaas will be linked against `libfftw3_mpi` regardless of the thread model.

---

**Important:** Users wary of performance should use MPI, as it yields remarkably better scaling properties than the shared memory parallelism models. Care should also be taken when compiling with both OpenMP and MPI support: setting the number of threads to more than one in an MPI context can decrease performance.

---

## 8.2 Integration algorithm

In its implementation of the volume integral operators necessary for elastic-plastic solutions, Tamaas differentiates two way of computing the intermediate integral along  $z$  in the partial Fourier domain:

- Cutoff integration: because the intermediate integral involves kernels of the form  $\exp(q(x - y))$ , it is easy to truncate the integral when  $x$  and  $y$  are far apart, especially for large values of  $q$ . This changes the complexity of the intermediate integral from  $O(N_1 N_2 N_3^2)$  (the naive implementation) to  $O(\sqrt{N_1^2 + N_2^2} N_3^2)$ .
- Linear integration: this method relies on a separation of variables  $\exp(q(x - y)) = \exp(qx) \cdot \exp(-qy)$ . This allows to break the dependency in  $N_3^2$  of the number of operations, so that the overall complexity of the intermediate integral is  $O(N_1 N_2 N_3)$ .

Details on both algorithms can be found in<sup>1</sup>. Tamaas uses linear integration by default because it is faster in many cases without introducing a truncation error. Unfortunately, it has a severe drawback when considering systems with a fine surface discretization: due to  $q$  increasing with the number of points on the surface, the separated terms  $\exp(qx)$  and  $\exp(-qy)$  may overflow and underflow respectively. Tamaas will warn if that is the case, and users have two options to remedy the situation:

- Change the integration method by calling `setIntegrationMethod` with the desired `integration_method` on the `Model` object you use in the computation.
- Compile Tamaas with the option `real_type='long double'`. To make manipulation of numpy arrays easier, a `dtype` is provided in the `tamaas` module which can be used to create numpy arrays compatible with Tamaas' floating point type (e.g. `x = np.linspace(0, 1, dtype=tamaas.dtype)`)

Both these options negatively affect the performance, and it is up to the user to select the optimal solution for their particular use case.

## 8.3 Computational methods & Citations

Tamaas uses specialized numerical methods to efficiently solve elastic and elastoplastic periodic contact problems. Using a boundary integral formulation and a half-space geometry for the former allow (a) the focus of computational power to the contact interface since the bulk response can be represented exactly, (b) the use of the fast-Fourier transform for the computation of convolution integrals. In conjunction with a boundary integral formulation of the bulk state equations, a conjugate gradient approach is used to solve the contact problem.

---

**Note:** The above methods are state-of-the-art in the domain of rough surface contact. Below are selected publications detailing the methods used in elastic contact with and without adhesion:

- Boundary integral formulation:
  - Stanley and Kato (*J. of Tribology*, 1997)
- Conjugate Gradient:
  - Polonsky and Keer (*Wear*, 1999)
  - Rey, Anciaux and Molinari (*Computational Mechanics*, 2017)
- Frictional contact:
  - Condat (*J. of Optimization Theory and Applications*, 2012)

---

<sup>1</sup> L. Frérot, "Bridging scales in wear modeling with volume integral methods for elastic-plastic contact," École Polytechnique Fédérale de Lausanne, 2020 (Section 2.3.2). doi:10.5075/epfl-thesis-7640.

For elastic-plastic contact, Tamaas uses a similar approach by implementing a *volume* integral formulation of the bulk equilibrium equations. Thanks to kernel expressions that are directly formulated in the Fourier domain, the method reduces the algorithmic complexity, memory requirements and sampling errors compared to traditional volume integral methods (Frérot, Bonnet, Anciaux and Molinari, [Computer Methods in Applied Mechanics and Engineering, 2019, arxiv:1811.11558](#)). The figure below shows a comparison of run times for an elasticity problem (only a single solve step) between Tamaas and Akantu, a high-performance FEM code using the direct solver MUMPS.

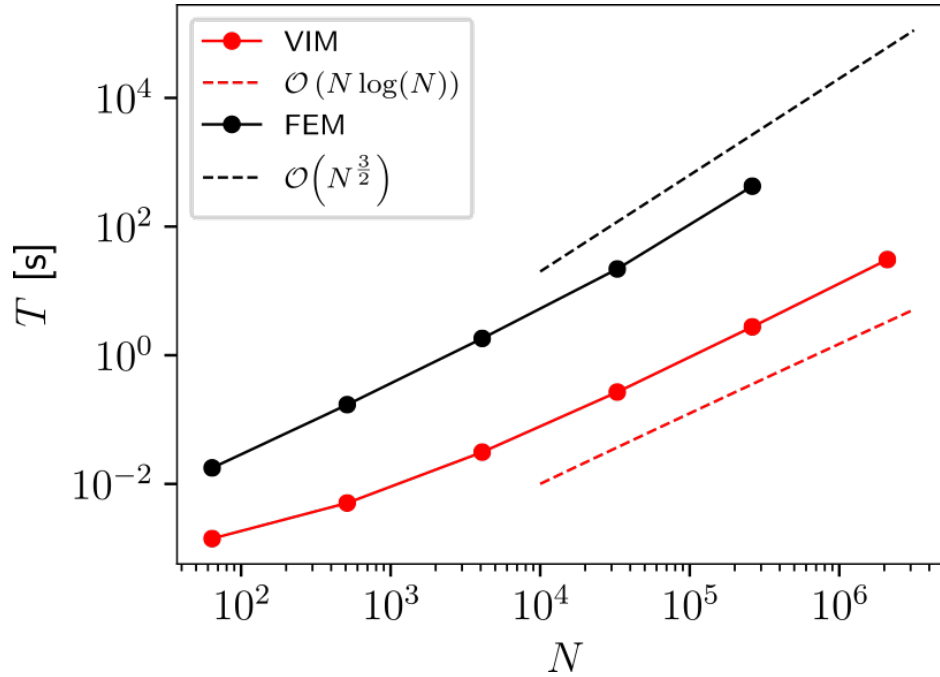


Fig. 1: Comparison of run times between the volume integral implementation (with cutoff integration) of Tamaas and an FEM solve step with a Cholesky factorization performed by Akantu+MUMPS.  $N$  is the total number of points.

Further discussion about the elastic-plastic solver implemented in Tamaas can be found in Frérot, Bonnet, Anciaux and Molinari, ([Computer Methods in Applied Mechanics and Engineering, 2019, arxiv:1811.11558](#)).



## FREQUENTLY ASKED QUESTIONS

### 9.1 Importing `tamaas` module gives a circular import error on Windows

(Similar to this issue) Installing with `pip install tamaas` does not work on Windows, as binary distributions are only built for Linux. To use Tamaas in Windows, use the Windows subsystem for Linux, then use `pip` to *install Tamaas*, or use the *provided Docker images*.

### 9.2 What are the units in Tamaas?

All quantities in Tamaas are unitless. To choose a consistent set of units, see *Units in Tamaas*.

### 9.3 Do contact solvers solve for a total force or an average pressure?

Solvers consider that the argument to the `solve()` method is an average apparent pressure (or average gap in some cases), i.e. the total force divided by the total system area (in the reference configuration). This means that doubling the system size and solving for the same argument to the solver *increases* the total load by a factor 4 (for a 2D surface).

### 9.4 `scons dev` fails to install Tamaas with `externally-managed-environment` error

Pip now refuses to install a package outside of virtual environments (see [PEP 668](#)), even with the `--user` flag on. This encourages the use of virtual environments, either with `venv` or `virtualenv`, which works nicely with `scons dev`.

However, if one **really** needs an editable installation outside of a virtual environment, the `PIPFLAGS` option can be used to circumvent pip's protections (not recommended):

```
scons dev PIPFLAGS="--user --break-system-packages"
```

**Warning:** If misused this can break your system's Python packages. Use virtual environments instead!



## DEVELOPER DOCUMENTATION

If you have code contributions you'd like to submit to Tamaas, you are in the right place. This page describes the good practices and workflows to follow to get your code in Tamaas.

### 10.1 Documentation

Documentation can be built with `scons doc`, provided the adequate dependencies are installed. The generated files are in `build-${build_type}/doc/`, with the C++ API in the `doxygen/html` subfolder and the Sphinx documentation in the `sphinx/html` subfolder. Use them as reference when developing, most functions and classes in Tamaas have API-level documentation.

#### 10.1.1 Writing documentation

Every new functionality in Tamaas should have *at minimum* API-level documentation. In C++, this is done with [Doxygen-styled comments](#).

API-level documentation in Python can be done with [pybind11's docstrings](#).

### 10.2 Writing code

To check that your code matches Tamaas' coding convention, please run `scons lint` *before* committing. This will check the code style of your changes. It runs `clang-format`, `clang-tidy`, `flake8` and `mypy`.

---

**Tip:** Subcommands can be used to run individual linting software:

- `scons clang-format`
  - `scons clang-tidy`
  - `scons flake8`
  - `scons mypy`
- 

**Note:** As redundancy measure, linting also occurs in continuous integration on Gitlab. Review the step artifacts to see which changes are necessary.

---

## 10.3 Running tests

**Warning:** Make sure to run in a virtual environment where Tamaas is installed with `scons dev`, see the *Frequently Asked Questions*.

To run tests on your local machine:

```
scons build_tests=True
scons test
```

The `verbose=True` build option ensures that test output is verbose as well, useful when writing new parametrized tests. Individual tests can be run with:

```
pytest build-release/tests/test_westergaard.py
```

Check the output for the lines indicating where the Tamaas python extension and the `libTamaas` shared libraries were loaded from. For instance, an editable install of Tamaas should give an output like:

```
module file: <path-to-tamaas>/build-release/python/tamaas/__init__.py
wrapper: <path-to-tamaas>/build-release/python/tamaas/_tamaas.cpython-311-x86_64-
↳linux-gnu.so
libTamaas: static link
```

## 10.4 Git workflow

Please follow the very simple [GitHub flow](#) to submit changes, essentially:

1. Fork the project and create a branch to contain your changes
2. Make your changes
3. Create a merge request
4. Address review changes

### 10.4.1 Commit messages

Commit messages are a very important trace of changes to the code, and should contain enough context information to understand the motivation for the change. A typical commit message structure should be:

```
one-line short description of the change

1 or more paragraphs detailing, for example:
- what problem the commit fixes
- anything non-trivial the code does
- things that had to be researched to fix the issue
- other important contextual information
```

There is no limit to a commit message length, and that's a good thing: the more context the better, particularly for new functionality and non-trivial changes (like breaking changes).

## 11.1 Python API

### 11.1.1 Tamaas root module

A high-performance library for periodic rough surface contact

See `__author__`, `__license__`, `__copyright__` for extra information about Tamaas.

- User documentation: <https://tamaas.readthedocs.io>
- Bug Tracker: <https://gitlab.com/tamaas/tamaas/-/issues>
- Source Code: <https://gitlab.com/tamaas/tamaas>

### 11.1.2 Tamaas C++ bindings

Compiled component of Tamaas

**class** `tamaas._tamaas.AdhesionFunctional`

Bases: *Functional*

`__init__` (\*args, \*\*kwargs)

**computeF** (*self*: *tamaas.\_tamaas.Functional*, *arg0*: *GridBaseWrap<T>*, *arg1*: *GridBaseWrap<T>*) → float  
Compute functional value

**computeGradF** (*self*: *tamaas.\_tamaas.Functional*, *arg0*: *GridBaseWrap<T>*, *arg1*: *GridBaseWrap<T>*) → None  
None

Compute functional gradient

**property parameters**

Parameters dictionary

**setParameterers** (*self*: *tamaas.\_tamaas.AdhesionFunctional*, *arg0*: *dict[str, float]*) → None

**class** `tamaas._tamaas.AndersonMixing`

Bases: *EPICSolver*

Fixed-point scheme with fixed memory size and Anderson mixing update to help and accelerate convergence. See doi:10.1006/jcph.1996.0059 for reference.

`__init__` (*self*: *tamaas.\_tamaas.AndersonMixing*, *contact\_solver*: *tamaas.\_tamaas.ContactSolver*, *elasto\_plastic\_solver*: *tamaas.\_tamaas.EPSolver*, *tolerance*: *float = 1e-10*, *memory*: *int = 5*) → None

**acceleratedSolve** (*self*: `tamaas._tamaas.EPICSolver`, *normal\_pressure*: `float`) → `float`

Solves the EP contact with an accelerated fixed-point scheme. May not converge!

**property** `max_iter`

**property** `model`

**property** `relaxation`

**solve** (*self*: `tamaas._tamaas.EPICSolver`, *normal\_pressure*: `float`) → `float`

Solves the EP contact with a relaxed fixed-point scheme. Adjust the relaxation parameter to help convergence.

**property** `tolerance`

**exception** `tamaas._tamaas.AssertionError`

Bases: `AssertionError`

**\_\_init\_\_** (*\*args*, *\*\*kwargs*)

**add\_note** ()

Exception.add\_note(note) – add a note to the exception

**args**

**with\_traceback** ()

Exception.with\_traceback(tb) – set self.\_\_traceback\_\_ to tb and return self.

**class** `tamaas._tamaas.BEEngine`

Bases: `pybind11_object`

**\_\_init\_\_** (*\*args*, *\*\*kwargs*)

**getModel** (*self*: `tamaas._tamaas.BEEngine`) → `tamaas::Model`

**property** `model`

**registerDirichlet** (*self*: `tamaas._tamaas.BEEngine`) → `None`

**registerNeumann** (*self*: `tamaas._tamaas.BEEngine`) → `None`

**solveDirichlet** (*self*: `tamaas._tamaas.BEEngine`, *arg0*: `GridBaseWrap<T>`, *arg1*: `GridBaseWrap<T>`) → `None`

**solveNeumann** (*self*: `tamaas._tamaas.BEEngine`, *arg0*: `GridBaseWrap<T>`, *arg1*: `GridBaseWrap<T>`) → `None`

**class** `tamaas._tamaas.BeckTeboulle`

Bases: `ContactSolver`

**\_\_init\_\_** (*self*: `tamaas._tamaas.BeckTeboulle`, *model*: `tamaas._tamaas.Model`, *surface*: `GridBaseWrap<T>`, *tolerance*: `float`, *mu*: `float`) → `None`

**addFunctionalTerm** (*self*: `tamaas._tamaas.ContactSolver`, *arg0*: `tamaas._tamaas.Functional`) → `None`

Add a term to the contact functional to minimize

**computeCost** (*self*: `tamaas._tamaas.BeckTeboulle`, *arg0*: `bool`) → `float`

**property** `dump_freq`

Frequency of displaying solver info

**property functional**

**property max\_iter**

Maximum number of iterations

**property model**

**setDumpFrequency** (*self*: tamaas.\_tamaas.ContactSolver, *dump\_freq*: int) → None

**setMaxIterations** (*self*: tamaas.\_tamaas.ContactSolver, *max\_iter*: int) → None

**solve** (*self*: tamaas.\_tamaas.BeckTeboulle, *p0*: list[float]) → float

**property surface**

**property tolerance**

Solver tolerance

**class** tamaas.\_tamaas.Cluster1D

Bases: pybind11\_object

**\_\_init\_\_** (*self*: tamaas.\_tamaas.Cluster1D) → None

**property area**

Area of cluster

**property bounding\_box**

Compute the bounding box of a cluster

**property extent**

Compute the extents of a cluster

**getArea** (*self*: tamaas.\_tamaas.Cluster1D) → int

**getPerimeter** (*self*: tamaas.\_tamaas.Cluster1D) → int

**getPoints** (*self*: tamaas.\_tamaas.Cluster1D) → list[Annotated[list[int], FixedSize(1)]]

**property perimeter**

Get perimeter of cluster

**property points**

Get list of points of cluster

**class** tamaas.\_tamaas.Cluster2D

Bases: pybind11\_object

**\_\_init\_\_** (*self*: tamaas.\_tamaas.Cluster2D) → None

**property area**

Area of cluster

**property bounding\_box**

Compute the bounding box of a cluster

**property extent**

Compute the extents of a cluster

**getArea** (*self*: tamaas.\_tamaas.Cluster2D) → int

**getPerimeter** (*self*: tamaas.\_tamaas.Cluster2D) → int

**getPoints** (*self*: tamaas.\_tamaas.Cluster2D) → list[Annotated[list[int], FixedSize(2)]]

**property perimeter**

Get perimeter of cluster

**property points**

Get list of points of cluster

**class** tamaas.\_tamaas.Cluster3D

Bases: pybind11\_object

**\_\_init\_\_** (*self*: tamaas.\_tamaas.Cluster3D) → None

**property area**

Area of cluster

**property bounding\_box**

Compute the bounding box of a cluster

**property extent**

Compute the extents of a cluster

**getArea** (*self*: tamaas.\_tamaas.Cluster3D) → int

**getPerimeter** (*self*: tamaas.\_tamaas.Cluster3D) → int

**getPoints** (*self*: tamaas.\_tamaas.Cluster3D) → list[Annotated[list[int], FixedSize(3)]]

**property perimeter**

Get perimeter of cluster

**property points**

Get list of points of cluster

**class** tamaas.\_tamaas.Condat

Bases: *ContactSolver*

Main solver for frictional contact problems. It has no restraint on the material properties or friction coefficient values, but solves an associated version of the Coulomb friction law, which differs from the traditional Coulomb friction in that the normal and tangential slip components are coupled.

**\_\_init\_\_** (*self*: tamaas.\_tamaas.Condat, *model*: tamaas.\_tamaas.Model, *surface*: GridBaseWrap<T>, *tolerance*: float, *mu*: float) → None

**addFunctionalTerm** (*self*: tamaas.\_tamaas.ContactSolver, *arg0*: tamaas.\_tamaas.Functional) → None

Add a term to the contact functional to minimize

**computeCost** (*self*: tamaas.\_tamaas.Condat, *arg0*: bool) → float

**property dump\_freq**

Frequency of displaying solver info

**property functional**

**property max\_iter**

Maximum number of iterations

**property model**

**setDumpFrequency** (*self*: tamaas.\_tamaas.ContactSolver, *dump\_freq*: int) → None

**setMaxIterations** (*self*: tamaas.\_tamaas.ContactSolver, *max\_iter*: int) → None

**solve** (*self*: tamaas.\_tamaas.Contact, *p0*: list[float], *grad\_step*: float = 0.9) → None

**property surface**

**property tolerance**

Solver tolerance

**class** tamaas.\_tamaas.ContactSolver

Bases: pybind11\_object

**\_\_init\_\_** (*self*: tamaas.\_tamaas.ContactSolver, *arg0*: tamaas.\_tamaas.Model, *arg1*: GridBaseWrap<T>, *arg2*: float) → None

**addFunctionalTerm** (*self*: tamaas.\_tamaas.ContactSolver, *arg0*: tamaas.\_tamaas.Functional) → None

Add a term to the contact functional to minimize

**property dump\_freq**

Frequency of displaying solver info

**property functional**

**property max\_iter**

Maximum number of iterations

**property model**

**setDumpFrequency** (*self*: tamaas.\_tamaas.ContactSolver, *dump\_freq*: int) → None

**setMaxIterations** (*self*: tamaas.\_tamaas.ContactSolver, *max\_iter*: int) → None

**solve** (*\*args*, *\*\*kwargs*)

Overloaded function.

1. solve(*self*: tamaas.\_tamaas.ContactSolver, *target\_force*: list[float]) -> float

Solve the contact for a mean traction/gap vector

2. solve(*self*: tamaas.\_tamaas.ContactSolver, *target\_normal\_pressure*: float) -> float

Solve the contact for a mean normal pressure/gap

**property surface**

**property tolerance**

Solver tolerance

**class** tamaas.\_tamaas.EPICSolver

Bases: pybind11\_object

Main solver class for elastic-plastic contact problems

**\_\_init\_\_** (*self*: tamaas.\_tamaas.EPICSolver, *contact\_solver*: tamaas.\_tamaas.ContactSolver, *elasto\_plastic\_solver*: tamaas.\_tamaas.EPSolver, *tolerance*: float = 1e-10, *relaxation*: float = 0.3) → None

**acceleratedSolve** (*self*: `tamaas._tamaas.EPICSolver`, *normal\_pressure*: `float`) → `float`

Solves the EP contact with an accelerated fixed-point scheme. May not converge!

**property** `max_iter`

**property** `model`

**property** `relaxation`

**solve** (*self*: `tamaas._tamaas.EPICSolver`, *normal\_pressure*: `float`) → `float`

Solves the EP contact with a relaxed fixed-point scheme. Adjust the relaxation parameter to help convergence.

**property** `tolerance`

**class** `tamaas._tamaas.EPSolver`

Bases: `pybind11_object`

Mother class for nonlinear plasticity solvers

**\_\_init\_\_** (*self*: `tamaas._tamaas.EPSolver`, *residual*: `tamaas._tamaas.Residual`) → `None`

**beforeSolve** (*self*: `tamaas._tamaas.EPSolver`) → `None`

**getResidual** (*self*: `tamaas._tamaas.EPSolver`) → `tamaas._tamaas.Residual`

**getStrainIncrement** (*self*: `tamaas._tamaas.EPSolver`) → `GridBaseWrap<T>`

**setToleranceManager** (*self*: `tamaas._tamaas.EPSolver`, *arg0*: `tamaas._tamaas.tolerance_manager`) → `None`

**solve** (*self*: `tamaas._tamaas.EPSolver`) → `None`

**property** `tolerance`

**updateState** (*self*: `tamaas._tamaas.EPSolver`) → `None`

**class** `tamaas._tamaas.ElasticFunctionalGap`

Bases: `Functional`

**\_\_init\_\_** (*self*: `tamaas._tamaas.ElasticFunctionalGap`, *arg0*: `tamaas::IntegralOperator`, *arg1*: `GridBaseWrap<T>`) → `None`

**computeF** (*self*: `tamaas._tamaas.Functional`, *arg0*: `GridBaseWrap<T>`, *arg1*: `GridBaseWrap<T>`) → `float`  
Compute functional value

**computeGradF** (*self*: `tamaas._tamaas.Functional`, *arg0*: `GridBaseWrap<T>`, *arg1*: `GridBaseWrap<T>`) → `None`  
Compute functional gradient

**class** `tamaas._tamaas.ElasticFunctionalPressure`

Bases: `Functional`

**\_\_init\_\_** (*self*: `tamaas._tamaas.ElasticFunctionalPressure`, *arg0*: `tamaas::IntegralOperator`, *arg1*: `GridBaseWrap<T>`) → `None`

**computeF** (*self*: `tamaas._tamaas.Functional`, *arg0*: `GridBaseWrap<T>`, *arg1*: `GridBaseWrap<T>`) → `float`  
Compute functional value

**computeGradF** (*self*: *tamaas.\_tamaas.Functional*, *arg0*: *GridBaseWrap<T>*, *arg1*: *GridBaseWrap<T>*) → None

Compute functional gradient

**class** *tamaas.\_tamaas.ExponentialAdhesionFunctional*

Bases: *AdhesionFunctional*

Potential of the form  $F = -\gamma \cdot \exp(-g/\rho)$

**\_\_init\_\_** (*self*: *tamaas.\_tamaas.ExponentialAdhesionFunctional*, *surface*: *GridBaseWrap<T>*) → None

**computeF** (*self*: *tamaas.\_tamaas.Functional*, *arg0*: *GridBaseWrap<T>*, *arg1*: *GridBaseWrap<T>*) → float

Compute functional value

**computeGradF** (*self*: *tamaas.\_tamaas.Functional*, *arg0*: *GridBaseWrap<T>*, *arg1*: *GridBaseWrap<T>*) → None

Compute functional gradient

**property parameters**

Parameters dictionary

**setParameters** (*self*: *tamaas.\_tamaas.AdhesionFunctional*, *arg0*: *dict[str, float]*) → None

**class** *tamaas.\_tamaas.FieldContainer*

Bases: *pybind11\_object*

**\_\_init\_\_** (*self*: *tamaas.\_tamaas.FieldContainer*) → None

**getField** (*self*: *tamaas::Model*, *field\_name*: *str*) → *GridVariant*

**getFields** (*self*: *tamaas::Model*) → *list[str]*

Return fields list

**registerField** (*self*: *tamaas::Model*, *field\_name*: *str*, *field*: *numpy.ndarray[numpy.float64]*) → None

**class** *tamaas.\_tamaas.Filter1D*

Bases: *pybind11\_object*

Mother class for Fourier filter objects

**\_\_init\_\_** (*self*: *tamaas.\_tamaas.Filter1D*) → None

**computeFilter** (*self*: *tamaas.\_tamaas.Filter1D*, *arg0*: *GridWrap<T, dim>*) → None

Compute the Fourier coefficient of the surface

**class** *tamaas.\_tamaas.Filter2D*

Bases: *pybind11\_object*

Mother class for Fourier filter objects

**\_\_init\_\_** (*self*: *tamaas.\_tamaas.Filter2D*) → None

**computeFilter** (*self*: *tamaas.\_tamaas.Filter2D*, *arg0*: *GridWrap<T, dim>*) → None

Compute the Fourier coefficient of the surface

**exception** *tamaas.\_tamaas.FloatingPointError*

Bases: *FloatingPointError*

**\_\_init\_\_** (*\*args*, *\*\*kwargs*)

**add\_note()**

Exception.add\_note(note) – add a note to the exception

**args**

**with\_traceback()**

Exception.with\_traceback(tb) – set self.\_\_traceback\_\_ to tb and return self.

**class** tamaas.\_tamaas.FloodFill

Bases: pybind11\_object

**\_\_init\_\_**(\*args, \*\*kwargs)

**static getClusters**(contact: GridWrap<T, dim>, diagonal: bool) → list[tamaas.\_tamaas.Cluster2D]

Return a list of clusters from boolean map

**static getSegments**(contact: GridWrap<T, dim>) → list[tamaas.\_tamaas.Cluster1D]

Return a list of segments from boolean map

**static getVolumes**(map: GridWrap<T, dim>, diagonal: bool) → list[tamaas.\_tamaas.Cluster3D]

Return a list of volume clusters

**class** tamaas.\_tamaas.Functional

Bases: pybind11\_object

**\_\_init\_\_**(self: tamaas.\_tamaas.Functional) → None

**computeF**(self: tamaas.\_tamaas.Functional, arg0: GridBaseWrap<T>, arg1: GridBaseWrap<T>) → float

Compute functional value

**computeGradF**(self: tamaas.\_tamaas.Functional, arg0: GridBaseWrap<T>, arg1: GridBaseWrap<T>) →

None

Compute functional gradient

**class** tamaas.\_tamaas.IntegralOperator

Bases: pybind11\_object

**\_\_init\_\_**(self: tamaas.\_tamaas.IntegralOperator, arg0: tamaas.\_tamaas.Model) → None

**apply**(self: tamaas.\_tamaas.IntegralOperator, arg0: numpy.ndarray[numpy.float64], arg1: numpy.ndarray[numpy.float64]) → None

**dirac** = <kind.dirac: 2>

**dirichlet** = <kind.dirichlet: 1>

**getKind**(self: tamaas.\_tamaas.IntegralOperator) → tamaas.\_tamaas.IntegralOperator.kind

**getModel**(self: tamaas.\_tamaas.IntegralOperator) → tamaas.\_tamaas.Model

**getType**(self: tamaas.\_tamaas.IntegralOperator) → tamaas.\_tamaas.model\_type

**property kind**

**matvec**(self: tamaas.\_tamaas.IntegralOperator, arg0: numpy.ndarray[numpy.float64]) → GridBaseWrap<T>

**property model**

**neumann** = <kind.neumann: 0>

**property shape**

**property type**

**updateFromModel** (*self*: `tamaas._tamaas.IntegralOperator`) → None

Resets internal persistent variables from the model

**class** `tamaas._tamaas.Isopowerlaw1D`

Bases: `Filter1D`

Isotropic powerlaw spectrum with a rolloff plateau

**\_\_init\_\_** (*self*: `tamaas._tamaas.Isopowerlaw1D`) → None

**alpha** (*self*: `tamaas._tamaas.Isopowerlaw1D`) → float

Nayak's bandwidth parameter

**computeFilter** (*self*: `tamaas._tamaas.Filter1D`, *arg0*: `GridWrap<T, dim>`) → None

Compute the Fourier coefficient of the surface

**elasticEnergy** (*self*: `tamaas._tamaas.Isopowerlaw1D`) → float

Computes full contact energy (adimensional)

**property hurst**

Hurst exponent

**moments** (*self*: `tamaas._tamaas.Isopowerlaw1D`) → list[float]

Theoretical first 3 moments of spectrum

**property q0**

Long wavelength cutoff

**property q1**

Rolloff wavelength

**property q2**

Short wavelength cutoff

**radialPSDMoment** (*self*: `tamaas._tamaas.Isopowerlaw1D`, *arg0*: float) → float

Computes  $\int k^q \phi(k) k dk$  from 0 to  $\infty$

**rmsHeights** (*self*: `tamaas._tamaas.Isopowerlaw1D`) → float

Theoretical RMS of heights

**rmsSlopes** (*self*: `tamaas._tamaas.Isopowerlaw1D`) → float

Theoretical RMS of slopes

**class** `tamaas._tamaas.Isopowerlaw2D`

Bases: `Filter2D`

Isotropic powerlaw spectrum with a rolloff plateau

**\_\_init\_\_** (*self*: `tamaas._tamaas.Isopowerlaw2D`) → None

**alpha** (*self*: `tamaas._tamaas.Isopowerlaw2D`) → float

Nayak's bandwidth parameter

**computeFilter** (*self*: `tamaas._tamaas.Filter2D`, *arg0*: `GridWrap<T, dim>`) → None

Compute the Fourier coefficient of the surface

**elasticEnergy** (*self*: `tamaas._tamaas.Isopowerlaw2D`) → float

Computes full contact energy (adimensional)

**property hurst**

Hurst exponent

**moments** (*self*: `tamaas._tamaas.Isopowerlaw2D`) → list[float]

Theoretical first 3 moments of spectrum

**property q0**

Long wavelength cutoff

**property q1**

Rolloff wavelength

**property q2**

Short wavelength cutoff

**radialPSDMoment** (*self*: `tamaas._tamaas.Isopowerlaw2D`, *arg0*: float) → float

Computes  $\int k^q \phi(k) k dk$  from 0 to  $\infty$

**rmsHeights** (*self*: `tamaas._tamaas.Isopowerlaw2D`) → float

Theoretical RMS of heights

**rmsSlopes** (*self*: `tamaas._tamaas.Isopowerlaw2D`) → float

Theoretical RMS of slopes

**class** `tamaas._tamaas.Kato`

Bases: `ContactSolver`

**\_\_init\_\_** (*self*: `tamaas._tamaas.Kato`, *model*: `tamaas._tamaas.Model`, *surface*: `GridBaseWrap<T>`, *tolerance*: float, *mu*: float) → None

**addFunctionalTerm** (*self*: `tamaas._tamaas.ContactSolver`, *arg0*: `tamaas._tamaas.Functional`) → None

Add a term to the contact functional to minimize

**computeCost** (*self*: `tamaas._tamaas.Kato`, *use\_tresca*: bool = False) → float

**property dump\_freq**

Frequency of displaying solver info

**property functional**

**property max\_iter**

Maximum number of iterations

**property model**

**setDumpFrequency** (*self*: `tamaas._tamaas.ContactSolver`, *dump\_freq*: int) → None

**setMaxIterations** (*self*: `tamaas._tamaas.ContactSolver`, *max\_iter*: int) → None

**solve** (*self*: `tamaas._tamaas.Kato`, *p0*: list[float], *proj\_iter*: int = 50) → None

**solveRegularized** (*self*: `tamaas._tamaas.Kato`, *p0*: `GridBaseWrap<T>`, *r*: float = 0.01) → float

**solveRelaxed** (*self*: `tamaas._tamaas.Kato`, *g0*: `GridBaseWrap<T>`) → float

**property surface**

**property tolerance**

Solver tolerance

**class** tamaas.\_tamaas.KatoSaturatedBases: *PolonskyKeerRey*

Solver for pseudo-plasticity problems where the normal pressure is constrained above by a saturation pressure “pmax”

**\_\_init\_\_** (*self*: *tamaas.\_tamaas.KatoSaturated*, *model*: *tamaas.\_tamaas.Model*, *surface*: *GridBaseWrap<T>*, *tolerance*: *float*, *pmax*: *float*) → None

**addFunctionalTerm** (*self*: *tamaas.\_tamaas.ContactSolver*, *arg0*: *tamaas.\_tamaas.Functional*) → None

Add a term to the contact functional to minimize

**computeError** (*self*: *tamaas.\_tamaas.PolonskyKeerRey*) → float

**property dump\_freq**

Frequency of displaying solver info

**property functional****gap** = <type.gap: 0>**property max\_iter**

Maximum number of iterations

**property model****property pmax**

Saturation normal pressure

**pressure** = <type.pressure: 1>

**setDumpFrequency** (*self*: *tamaas.\_tamaas.ContactSolver*, *dump\_freq*: *int*) → None

**setIntegralOperator** (*self*: *tamaas.\_tamaas.PolonskyKeerRey*, *arg0*: *str*) → None

**setMaxIterations** (*self*: *tamaas.\_tamaas.ContactSolver*, *max\_iter*: *int*) → None

**solve** (*\*args*, *\*\*kwargs*)

Overloaded function.

1. **solve**(*self*: *tamaas.\_tamaas.ContactSolver*, *target\_force*: *list[float]*) -> float

Solve the contact for a mean traction/gap vector

2. **solve**(*self*: *tamaas.\_tamaas.ContactSolver*, *target\_normal\_pressure*: *float*) -> float

Solve the contact for a mean normal pressure/gap

**property surface****property tolerance**

Solver tolerance

**class type**

Bases: pybind11\_object

Members:

gap

pressure

`__init__` (*self*: tamaas.\_tamaas.PolonskyKeerRey.type, *value*: int) → None`gap` = <type.gap: 0>**property name**`pressure` = <type.pressure: 1>**property value****class** tamaas.\_tamaas.LogLevel

Bases: pybind11\_object

Members:

debug

info

warning

error

`__init__` (*self*: tamaas.\_tamaas.LogLevel, *value*: int) → None`debug` = <LogLevel.debug: 0>`error` = <LogLevel.error: 3>`info` = <LogLevel.info: 1>**property name****property value**`warning` = <LogLevel.warning: 2>**class** tamaas.\_tamaas.Logger

Bases: pybind11\_object

`__init__` (*self*: tamaas.\_tamaas.Logger) → None`get` (*self*: tamaas.\_tamaas.Logger, *arg0*: tamaas.\_tamaas.LogLevel) → *tamaas.\_tamaas.Logger*

Get a logger object for a log level

**class** tamaas.\_tamaas.MaugisAdhesionFunctionalBases: *AdhesionFunctional*Cohesive zone potential  $F = H(g - \rho) \cdot \gamma / \rho$ `__init__` (*self*: tamaas.\_tamaas.MaugisAdhesionFunctional, *surface*: GridBaseWrap<T>) → None`computeF` (*self*: tamaas.\_tamaas.Functional, *arg0*: GridBaseWrap<T>, *arg1*: GridBaseWrap<T>) → float

Compute functional value

**computeGradF** (*self*: *tamaas.\_tamaas.Functional*, *arg0*: *GridBaseWrap<T>*, *arg1*: *GridBaseWrap<T>*) → None

Compute functional gradient

**property parameters**

Parameters dictionary

**setParameters** (*self*: *tamaas.\_tamaas.AdhesionFunctional*, *arg0*: *dict[str, float]*) → None

**class** *tamaas.\_tamaas.MaxwellViscoelastic*

Bases: *PolonskyKeerRey*

Viscoelastic, pressure-based normal contact solver, based on a generalized Maxwell model

**\_\_init\_\_** (*self*: *tamaas.\_tamaas.MaxwellViscoelastic*, *model*: *tamaas.\_tamaas.Model*, *surface*: *GridBaseWrap<T>*, *tolerance*: *float*, *time\_step*: *float*, *shear\_moduli*: *list[float]*, *characteristic\_times*: *list[float]*) → None

**addFunctionalTerm** (*self*: *tamaas.\_tamaas.ContactSolver*, *arg0*: *tamaas.\_tamaas.Functional*) → None

Add a term to the contact functional to minimize

**computeError** (*self*: *tamaas.\_tamaas.PolonskyKeerRey*) → float

**property dump\_freq**

Frequency of displaying solver info

**property functional**

**gap** = <type.gap: 0>

**property max\_iter**

Maximum number of iterations

**property model**

**pressure** = <type.pressure: 1>

**reset** (*self*: *tamaas.\_tamaas.MaxwellViscoelastic*) → None

**setDumpFrequency** (*self*: *tamaas.\_tamaas.ContactSolver*, *dump\_freq*: *int*) → None

**setIntegralOperator** (*self*: *tamaas.\_tamaas.PolonskyKeerRey*, *arg0*: *str*) → None

**setMaxIterations** (*self*: *tamaas.\_tamaas.ContactSolver*, *max\_iter*: *int*) → None

**solve** (*\*args*, *\*\*kwargs*)

Overloaded function.

1. *solve(self: tamaas.\_tamaas.ContactSolver, target\_force: list[float]) -> float*

Solve the contact for a mean traction/gap vector

2. *solve(self: tamaas.\_tamaas.ContactSolver, target\_normal\_pressure: float) -> float*

Solve the contact for a mean normal pressure/gap

**property solve\_should\_update**

**property surface**

**property time\_step**

Backwards-Euler time-step

**property tolerance**

Solver tolerance

**class type**Bases: `pybind11_object`

Members:

`gap``pressure``__init__` (*self*: `tamaas._tamaas.PolonskyKeerRey.type`, *value*: `int`) → `None``gap = <type.gap: 0>`**property name**`pressure = <type.pressure: 1>`**property value**`updateState` (*self*: `tamaas._tamaas.MaxwellViscoelastic`) → `None`**class** `tamaas._tamaas.Model`Bases: `FieldContainer`**property E**

Young's modulus

**property E\_star**

Contact (Hertz) modulus

`__init__` (*self*: `tamaas._tamaas.Model`, *arg0*: `tamaas._tamaas.model_type`, *arg1*: `list[float]`, *arg2*: `list[int]`) → `None`Create a new model of a given type, physical size and *global* discretization.**Parameters**

- **model\_type** – the type of desired model
- **system\_size** – the physical size of the domain in each direction
- **global\_discretization** – number of points in each direction

`addDumper` (*self*: `tamaas._tamaas.Model`, *dumper*: `tamaas::ModelDumper`) → `None`

Register a dumper

`applyElasticity` (*self*: `tamaas._tamaas.Model`, *arg0*: `numpy.ndarray[numpy.float64]`, *arg1*: `numpy.ndarray[numpy.float64]`) → `None`

Apply Hooke's law

**property be\_engine**

Boundary element engine

**property boundary\_fields**

**property boundary\_shape**

Number of points on boundary

**property boundary\_system\_size**

Physical size of surface

**property displacement**

Displacement field

**dump** (*self*: tamaas.\_tamaas.Model) → None

Write model data to registered dumpers

**getBEEngine** (*self*: tamaas.\_tamaas.Model) → *tamaas.\_tamaas.BEEngine*

**getBoundaryDiscretization** (*self*: tamaas.\_tamaas.Model) → list[int]

**getBoundarySystemSize** (*self*: tamaas.\_tamaas.Model) → list[float]

**getDiscretization** (*self*: tamaas.\_tamaas.Model) → list[int]

**getDisplacement** (*self*: tamaas.\_tamaas.Model) → GridBaseWrap<T>

**getField** (*self*: tamaas::Model, *field\_name*: str) → GridVariant

**getFields** (*self*: tamaas::Model) → list[str]

Return fields list

**getHertzModulus** (*self*: tamaas.\_tamaas.Model) → float

**getIntegralOperator** (*self*: tamaas.\_tamaas.Model, *operator\_name*: str) → tamaas::IntegralOperator

**getPoissonRatio** (*self*: tamaas.\_tamaas.Model) → float

**getShearModulus** (*self*: tamaas.\_tamaas.Model) → float

**getSystemSize** (*self*: tamaas.\_tamaas.Model) → list[float]

**getTraction** (*self*: tamaas.\_tamaas.Model) → GridBaseWrap<T>

**getYoungModulus** (*self*: tamaas.\_tamaas.Model) → float

**property global\_shape**

Global discretization (in MPI environment)

**property mu**

Shear modulus

**property nu**

Poisson's ratio

**property operators**

Returns a dict-like object allowing access to the model's integral operators

**registerField** (*self*: tamaas::Model, *field\_name*: str, *field*: numpy.ndarray[numpy.float64]) → None

**setElasticity** (*self*: tamaas.\_tamaas.Model, *E*: float, *nu*: float) → None

**setIntegrationMethod** (*self*: tamaas.\_tamaas.Model, *arg0*: tamaas::integration\_method, *arg1*: float) → None

**property shape**

Discretization (local in MPI environment)

**solveDirichlet** (*self*: tamaas.\_tamaas.Model) → None

Solve surface displacements -> tractions

**solveNeumann** (*self*: tamaas.\_tamaas.Model) → None

Solve surface tractions -> displacements

**property system\_size**

Size of physical domain

**property traction**

Surface traction field

**property type**

**class** tamaas.\_tamaas.ModelDumper

Bases: pybind11\_object

**\_\_init\_\_** (*self*: tamaas.\_tamaas.ModelDumper) → None

**dump** (*self*: tamaas.\_tamaas.ModelDumper, *model*: tamaas.\_tamaas.Model) → None

Dump model

**class** tamaas.\_tamaas.ModelFactory

Bases: pybind11\_object

**\_\_init\_\_** (*\*args*, *\*\*kwargs*)

**static createModel** (*\*args*, *\*\*kwargs*)

Overloaded function.

1. createModel(model\_type: tamaas.\_tamaas.model\_type, system\_size: list[float], global\_discretization: list[int]) -> tamaas.\_tamaas.Model

Create a new model of a given type, physical size and *global* discretization.

**Parameters**

- **model\_type** – the type of desired model
- **system\_size** – the physical size of the domain in each direction
- **global\_discretization** – number of points in each direction

2. createModel(model: tamaas.\_tamaas.Model) -> tamaas.\_tamaas.Model

Create a deep copy of a model.

**static createResidual** (*model*: tamaas.\_tamaas.Model, *sigma\_y*: float, *hardening*: float = 0.0) → tamaas::Residual

Create an isotropic linear hardening residual. :param model: the model on which to define the residual :param sigma\_y: the (von Mises) yield stress :param hardening: the hardening modulus

**static registerHookeField** (*model*: tamaas.\_tamaas.Model, *name*: str) → None

Register a HookeField operator

**static registerInverseHookeField** (*model*: tamaas.\_tamaas.Model, *name*: str) → None

Register an InverseHookeField operator

**static registerNonPeriodic** (*model: tamaas.\_tamaas.Model, name: str*) → None

Register non-periodic Boussinesq operator

**static registerVolumeOperators** (*model: tamaas.\_tamaas.Model*) → None

Register Boussinesq and Mindlin operators to model.

**static setIntegrationMethod** (*operator: tamaas::IntegralOperator, method: tamaas::integration\_method, cutoff: float*) → None

Set the integration method (linear or cutoff) for a volume integral operator

**exception** `tamaas._tamaas.ModelTypeError`

Bases: `TypeError`

**\_\_init\_\_** (*\*args, \*\*kwargs*)

**add\_note** ()

Exception.add\_note(note) – add a note to the exception

**args**

**with\_traceback** ()

Exception.with\_traceback(tb) – set self.\_\_traceback\_\_ to tb and return self.

**exception** `tamaas._tamaas.NotImplementedError`

Bases: `NotImplementedError`

**\_\_init\_\_** (*\*args, \*\*kwargs*)

**add\_note** ()

Exception.add\_note(note) – add a note to the exception

**args**

**with\_traceback** ()

Exception.with\_traceback(tb) – set self.\_\_traceback\_\_ to tb and return self.

**class** `tamaas._tamaas.PolonskyKeerRey`

Bases: `ContactSolver`

Main solver class for normal elastic contact problems. Its functional can be customized to add an adhesion term, and its primal variable can be set to either the gap or the pressure.

**\_\_init\_\_** (*self: tamaas.\_tamaas.PolonskyKeerRey, model: tamaas.\_tamaas.Model, surface: GridBaseWrap<T>, tolerance: float, primal\_type: tamaas.\_tamaas.PolonskyKeerRey.type = <type.pressure: 1>, constraint\_type: tamaas.\_tamaas.PolonskyKeerRey.type = <type.pressure: 1>*) → None

**addFunctionalTerm** (*self: tamaas.\_tamaas.ContactSolver, arg0: tamaas.\_tamaas.Functional*) → None

Add a term to the contact functional to minimize

**computeError** (*self: tamaas.\_tamaas.PolonskyKeerRey*) → float

**property** `dump_freq`

Frequency of displaying solver info

**property** `functional`

**gap** = `<type.gap: 0>`

**property max\_iter**

Maximum number of iterations

**property model**

**pressure = <type.pressure: 1>**

**setDumpFrequency** (*self: tamaas.\_tamaas.ContactSolver, dump\_freq: int*) → None

**setIntegralOperator** (*self: tamaas.\_tamaas.PolonskyKeerRey, arg0: str*) → None

**setMaxIterations** (*self: tamaas.\_tamaas.ContactSolver, max\_iter: int*) → None

**solve** (\*args, \*\*kwargs)

Overloaded function.

1. solve(*self: tamaas.\_tamaas.ContactSolver, target\_force: list[float]*) -> float

Solve the contact for a mean traction/gap vector

2. solve(*self: tamaas.\_tamaas.ContactSolver, target\_normal\_pressure: float*) -> float

Solve the contact for a mean normal pressure/gap

**property surface**

**property tolerance**

Solver tolerance

**class type**

Bases: `pybind11_object`

Members:

gap

pressure

**\_\_init\_\_** (*self: tamaas.\_tamaas.PolonskyKeerRey.type, value: int*) → None

**gap = <type.gap: 0>**

**property name**

**pressure = <type.pressure: 1>**

**property value**

**class** `tamaas._tamaas.PolonskyKeerTan`

Bases: `ContactSolver`

**\_\_init\_\_** (*self: tamaas.\_tamaas.PolonskyKeerTan, model: tamaas.\_tamaas.Model, surface: GridBaseWrap<T>, tolerance: float, mu: float*) → None

**addFunctionalTerm** (*self: tamaas.\_tamaas.ContactSolver, arg0: tamaas.\_tamaas.Functional*) → None

Add a term to the contact functional to minimize

**computeCost** (*self: tamaas.\_tamaas.PolonskyKeerTan, use\_tresca: bool = False*) → float

**property dump\_freq**

Frequency of displaying solver info

**property functional**

**property max\_iter**

Maximum number of iterations

**property model**

**setDumpFrequency** (*self*: tamaas.\_tamaas.ContactSolver, *dump\_freq*: int) → None

**setMaxIterations** (*self*: tamaas.\_tamaas.ContactSolver, *max\_iter*: int) → None

**solve** (*self*: tamaas.\_tamaas.PolonskyKeerTan, *p0*: list[float]) → float

**solveTresca** (*self*: tamaas.\_tamaas.PolonskyKeerTan, *p0*: GridBaseWrap<T>) → float

**property surface**

**property tolerance**

Solver tolerance

**class** tamaas.\_tamaas.RegularizedPowerlaw1D

Bases: *Filter1D*

Isotropic regularized powerlaw with a plateau extending to the size of the system

**\_\_init\_\_** (*self*: tamaas.\_tamaas.RegularizedPowerlaw1D) → None

**computeFilter** (*self*: tamaas.\_tamaas.Filter1D, *arg0*: GridWrap<T, dim>) → None

Compute the Fourier coefficient of the surface

**property hurst**

Hurst exponent

**property q1**

Rolloff wavelength

**property q2**

Short wavelength cutoff

**class** tamaas.\_tamaas.RegularizedPowerlaw2D

Bases: *Filter2D*

Isotropic regularized powerlaw with a plateau extending to the size of the system

**\_\_init\_\_** (*self*: tamaas.\_tamaas.RegularizedPowerlaw2D) → None

**computeFilter** (*self*: tamaas.\_tamaas.Filter2D, *arg0*: GridWrap<T, dim>) → None

Compute the Fourier coefficient of the surface

**property hurst**

Hurst exponent

**property q1**

Rolloff wavelength

**property q2**

Short wavelength cutoff

**class** tamaas.\_tamaas.Residual

Bases: pybind11\_object

**\_\_init\_\_** (*self: tamaas.\_tamaas.Residual, model: tamaas.\_tamaas.Model, material: tamaas::Material*) → None

Create a residual object with a material. Defines the following residual equation:

$$\varepsilon - \nabla N[\sigma(\varepsilon)] - \nabla M[t] = 0$$

Where  $\sigma(\varepsilon)$  is the *eigenstress* associated with the constitutive law.

#### Parameters

- **model** – the model on which to define the residual
- **material** – material object which defines a constitutive law

**applyTangent** (*self: tamaas.\_tamaas.Residual, arg0: GridBaseWrap<T>, arg1: GridBaseWrap<T>, arg2: GridBaseWrap<T>*) → None

**computeResidual** (*self: tamaas.\_tamaas.Residual, arg0: GridBaseWrap<T>*) → None

**computeResidualDisplacement** (*self: tamaas.\_tamaas.Residual, arg0: GridBaseWrap<T>*) → None

**getStress** (*self: tamaas.\_tamaas.Residual*) → GridWrap<T, dim>

**getVector** (*self: tamaas.\_tamaas.Residual*) → GridBaseWrap<T>

**property material**

**property model**

**setIntegrationMethod** (*self: tamaas.\_tamaas.Residual, arg0: tamaas::integration\_method, arg1: float*) → None

**updateState** (*self: tamaas.\_tamaas.Residual, arg0: GridBaseWrap<T>*) → None

**property vector**

**class** `tamaas._tamaas.SquaredExponentialAdhesionFunctional`

Bases: `AdhesionFunctional`

Potential of the form  $F = -\gamma \cdot \exp(-0.5 \cdot (g/\rho)^2)$

**\_\_init\_\_** (*self: tamaas.\_tamaas.SquaredExponentialAdhesionFunctional, surface: GridBaseWrap<T>*) → None

**computeF** (*self: tamaas.\_tamaas.Functional, arg0: GridBaseWrap<T>, arg1: GridBaseWrap<T>*) → float  
Compute functional value

**computeGradF** (*self: tamaas.\_tamaas.Functional, arg0: GridBaseWrap<T>, arg1: GridBaseWrap<T>*) → None  
Compute functional gradient

**property parameters**

Parameters dictionary

**setParameters** (*self: tamaas.\_tamaas.AdhesionFunctional, arg0: dict[str, float]*) → None

**class** `tamaas._tamaas.Statistics1D`

Bases: `pybind11_object`

**\_\_init\_\_** (*\*args, \*\*kwargs*)

**static computeAutocorrelation** (*arg0: GridWrap<T, dim>*) → GridWrap<T, dim>  
 Compute autocorrelation of surface

**static computeFDRMSSlope** (*arg0: GridWrap<T, dim>*) → float  
 Compute hrms' with finite differences

**static computeFullContactPressure** (*surface: GridWrap<T, dim>*) → float  
 Compute pressure necessary for full contact

**static computeMoments** (*arg0: GridWrap<T, dim>*) → list[float]  
 Compute spectral moments

**static computePowerSpectrum** (*arg0: GridWrap<T, dim>*) → GridWrap<T, dim>  
 Compute PSD of surface

**static computeRMSHeights** (*arg0: GridWrap<T, dim>*) → float  
 Compute hrms

**static computeSpectralEnergy** (*arg0: GridWrap<T, dim>*) → float  
 Compute the full contact elastic energy in Fourier space

**static computeSpectralRMSSlope** (*arg0: GridWrap<T, dim>*) → float  
 Compute hrms' in Fourier space

**static contact** (*tractions: GridWrap<T, dim>, perimeter: int = 0*) → float  
 Compute the (corrected) contact area. Perimeter is the total contact perimeter in number of segments.

**static graphArea** (*zdisplacement: GridWrap<T, dim>*) → float  
 Compute area of function graph (i.e. area of deformed surface).

**class** tamaas.\_tamaas.Statistics2D

Bases: pybind11\_object

**\_\_init\_\_** (\*args, \*\*kwargs)

**static computeAutocorrelation** (*arg0: GridWrap<T, dim>*) → GridWrap<T, dim>  
 Compute autocorrelation of surface

**static computeFDRMSSlope** (*arg0: GridWrap<T, dim>*) → float  
 Compute hrms' with finite differences

**static computeFullContactPressure** (*surface: GridWrap<T, dim>*) → float  
 Compute pressure necessary for full contact

**static computeMoments** (*arg0: GridWrap<T, dim>*) → list[float]  
 Compute spectral moments

**static computePowerSpectrum** (*arg0: GridWrap<T, dim>*) → GridWrap<T, dim>  
 Compute PSD of surface

**static computeRMSHeights** (*arg0: GridWrap<T, dim>*) → float  
 Compute hrms

**static computeSpectralEnergy** (*arg0: GridWrap<T, dim>*) → float  
 Compute the full contact elastic energy in Fourier space

**static computeSpectralRMSSlope** (*arg0: GridWrap<T, dim>*) → float  
 Compute hrms' in Fourier space

**static contact** (*tractions: GridWrap<T, dim>, perimeter: int = 0*) → float

Compute the (corrected) contact area. Perimeter is the total contact perimeter in number of segments.

**static graphArea** (*zdisplacement: GridWrap<T, dim>*) → float

Compute area of function graph (i.e. area of deformed surface).

**class** `tamaas._tamaas.SurfaceGenerator1D`

Bases: `pybind11_object`

**\_\_init\_\_** (*\*args, \*\*kwargs*)

**buildSurface** (*self: tamaas.\_tamaas.SurfaceGenerator1D*) → `GridWrap<T, dim>`

Generate a surface and return a reference to it

**property random\_seed**

Random generator seed

**setRandomSeed** (*self: tamaas.\_tamaas.SurfaceGenerator1D, arg0: int*) → None

**setSizes** (*self: tamaas.\_tamaas.SurfaceGenerator1D, arg0: Annotated[list[int], FixedSize(1)]*) → None

**property shape**

Global shape of surfaces

**class** `tamaas._tamaas.SurfaceGenerator2D`

Bases: `pybind11_object`

**\_\_init\_\_** (*\*args, \*\*kwargs*)

**buildSurface** (*self: tamaas.\_tamaas.SurfaceGenerator2D*) → `GridWrap<T, dim>`

Generate a surface and return a reference to it

**property random\_seed**

Random generator seed

**setRandomSeed** (*self: tamaas.\_tamaas.SurfaceGenerator2D, arg0: int*) → None

**setSizes** (*self: tamaas.\_tamaas.SurfaceGenerator2D, arg0: Annotated[list[int], FixedSize(2)]*) → None

**property shape**

Global shape of surfaces

**class** `tamaas._tamaas.SurfaceGeneratorFilter1D`

Bases: `SurfaceGenerator1D`

Generates a rough surface with Gaussian noise in the PSD

**\_\_init\_\_** (*\*args, \*\*kwargs*)

Overloaded function.

1. `__init__(self: tamaas._tamaas.SurfaceGeneratorFilter1D) -> None`

Default constructor

2. `__init__(self: tamaas._tamaas.SurfaceGeneratorFilter1D, arg0: Annotated[list[int], FixedSize(1)]) -> None`

Initialize with global surface shape

**buildSurface** (*self: tamaas.\_tamaas.SurfaceGenerator1D*) → `GridWrap<T, dim>`

Generate a surface and return a reference to it

**property random\_seed**

Random generator seed

**setFilter** (*self*: tamaas.\_tamaas.SurfaceGeneratorFilter1D, *filter*: tamaas.\_tamaas.Filter1D) → None

Set PSD filter

**setRandomSeed** (*self*: tamaas.\_tamaas.SurfaceGenerator1D, *arg0*: int) → None**setSize** (*self*: tamaas.\_tamaas.SurfaceGenerator1D, *arg0*: Annotated[list[int], FixedSize(1)]) → None**setSpectrum** (*self*: tamaas.\_tamaas.SurfaceGeneratorFilter1D, *filter*: tamaas.\_tamaas.Filter1D) → None

Set PSD filter

**property shape**

Global shape of surfaces

**property spectrum**

Power spectrum object

**class** tamaas.\_tamaas.SurfaceGeneratorFilter2DBases: *SurfaceGenerator2D*

Generates a rough surface with Gaussian noise in the PSD

**\_\_init\_\_** (\*args, \*\*kwargs)

Overloaded function.

1. **\_\_init\_\_**(*self*: tamaas.\_tamaas.SurfaceGeneratorFilter2D) -> None

Default constructor

2. **\_\_init\_\_**(*self*: tamaas.\_tamaas.SurfaceGeneratorFilter2D, *arg0*: Annotated[list[int], FixedSize(2)]) -> None

Initialize with global surface shape

**buildSurface** (*self*: tamaas.\_tamaas.SurfaceGenerator2D) → GridWrap<T, dim>

Generate a surface and return a reference to it

**property random\_seed**

Random generator seed

**setFilter** (*self*: tamaas.\_tamaas.SurfaceGeneratorFilter2D, *filter*: tamaas.\_tamaas.Filter2D) → None

Set PSD filter

**setRandomSeed** (*self*: tamaas.\_tamaas.SurfaceGenerator2D, *arg0*: int) → None**setSize** (*self*: tamaas.\_tamaas.SurfaceGenerator2D, *arg0*: Annotated[list[int], FixedSize(2)]) → None**setSpectrum** (*self*: tamaas.\_tamaas.SurfaceGeneratorFilter2D, *filter*: tamaas.\_tamaas.Filter2D) → None

Set PSD filter

**property shape**

Global shape of surfaces

**property spectrum**

Power spectrum object

**class** tamaas.\_tamaas.SurfaceGeneratorRandomPhase1D

Bases: *SurfaceGeneratorFilter1D*

Generates a rough surface with uniformly distributed phases and exact prescribed PSD

**\_\_init\_\_** (\*args, \*\*kwargs)

Overloaded function.

1. **\_\_init\_\_**(self: tamaas.\_tamaas.SurfaceGeneratorRandomPhase1D) -> None

Default constructor

2. **\_\_init\_\_**(self: tamaas.\_tamaas.SurfaceGeneratorRandomPhase1D, arg0: Annotated[list[int], FixedSize(1)]) -> None

Initialize with global surface shape

**buildSurface** (self: tamaas.\_tamaas.SurfaceGenerator1D) → GridWrap<T, dim>

Generate a surface and return a reference to it

**property random\_seed**

Random generator seed

**setFilter** (self: tamaas.\_tamaas.SurfaceGeneratorFilter1D, filter: tamaas.\_tamaas.Filter1D) → None

Set PSD filter

**setRandomSeed** (self: tamaas.\_tamaas.SurfaceGenerator1D, arg0: int) → None

**setSize** (self: tamaas.\_tamaas.SurfaceGenerator1D, arg0: Annotated[list[int], FixedSize(1)]) → None

**setSpectrum** (self: tamaas.\_tamaas.SurfaceGeneratorFilter1D, filter: tamaas.\_tamaas.Filter1D) → None

Set PSD filter

**property shape**

Global shape of surfaces

**property spectrum**

Power spectrum object

**class** tamaas.\_tamaas.SurfaceGeneratorRandomPhase2D

Bases: *SurfaceGeneratorFilter2D*

Generates a rough surface with uniformly distributed phases and exact prescribed PSD

**\_\_init\_\_** (\*args, \*\*kwargs)

Overloaded function.

1. **\_\_init\_\_**(self: tamaas.\_tamaas.SurfaceGeneratorRandomPhase2D) -> None

Default constructor

2. **\_\_init\_\_**(self: tamaas.\_tamaas.SurfaceGeneratorRandomPhase2D, arg0: Annotated[list[int], FixedSize(2)]) -> None

Initialize with global surface shape

**buildSurface** (self: tamaas.\_tamaas.SurfaceGenerator2D) → GridWrap<T, dim>

Generate a surface and return a reference to it

**property random\_seed**

Random generator seed

**setFilter** (*self*: tamaas.\_tamaas.SurfaceGeneratorFilter2D, *filter*: tamaas.\_tamaas.Filter2D) → None

Set PSD filter

**setRandomSeed** (*self*: tamaas.\_tamaas.SurfaceGenerator2D, *arg0*: int) → None

**setSize**s (*self*: tamaas.\_tamaas.SurfaceGenerator2D, *arg0*: Annotated[list[int], FixedSize(2)]) → None

**setSpectrum** (*self*: tamaas.\_tamaas.SurfaceGeneratorFilter2D, *filter*: tamaas.\_tamaas.Filter2D) → None

Set PSD filter

**property shape**

Global shape of surfaces

**property spectrum**

Power spectrum object

**class** tamaas.\_tamaas.TamaasInfo

Bases: pybind11\_object

**\_\_init\_\_** (\*args, \*\*kwargs)

**backend** = 'cpp'

**branch** = ''

**build\_type** = 'release'

**commit** = ''

**diff** = ''

**has\_mpi** = False

**has\_petsc** = False

**remotes** = ''

**version** = '2.9.0+10.g3d4b0338'

tamaas.\_tamaas.**finalize**() → None

tamaas.\_tamaas.**get\_log\_level**() → *tamaas.\_tamaas.LogLevel*

tamaas.\_tamaas.**initialize**(*num\_threads*: int = 0) → None

Initialize tamaas with desired number of threads. Automatically called upon import of the tamaas module, but can be manually called to set the desired number of threads.

**class** tamaas.\_tamaas.integration\_method

Bases: pybind11\_object

Integration method used for the computation of volumetric Fourier operators

Members:

linear : No approximation error,  $O(N_1 \cdot N_2 \cdot N_3)$  time complexity, may cause float overflow/underflow

cutoff : Approximation,  $O(\sqrt{N_1^2 + N_2^2} \cdot N_3^2)$  time complexity, no overflow/underflow risk

**\_\_init\_\_** (*self*: tamaas.\_tamaas.integration\_method, *value*: int) → None

**cutoff** = <integration\_method.cutoff: 0>

```
linear = <integration_method.linear: 1>
```

property name

property value

```
class tamaas._tamaas.model_type
```

Bases: `pybind11_object`

Members:

`basic_1d`: Normal contact with 1D interface

`basic_2d`: Normal contact with 2D interface

`surface_1d`: Normal & tangential contact with 1D interface

`surface_2d`: Normal & tangential contact with 2D interface

`volume_1d`: Contact with volumetric representation and 1D interface

`volume_2d`: Contact with volumetric representation and 2D interface

```
__init__ (self: tamaas._tamaas.model_type, value: int) → None
```

```
basic_1d = <model_type.basic_1d: 0>
```

```
basic_2d = <model_type.basic_2d: 1>
```

property name

```
surface_1d = <model_type.surface_1d: 2>
```

```
surface_2d = <model_type.surface_2d: 3>
```

property value

```
volume_1d = <model_type.volume_1d: 4>
```

```
volume_2d = <model_type.volume_2d: 5>
```

```
tamaas._tamaas.set_log_level (arg0: tamaas._tamaas.LogLevel) → None
```

```
tamaas._tamaas.to_voigt (arg0: GridWrap<T, dim>) → GridWrap<T, dim>
```

Convert a 3D tensor field to voigt notation

```
class tamaas._tamaas._DFSANESolver
```

Bases: `EPSolver`

```
__init__ (*args, **kwargs)
```

Overloaded function.

1. `__init__(self: tamaas._tamaas._DFSANESolver, residual: tamaas._tamaas.Residual) -> None`

2. `__init__(self: tamaas._tamaas._DFSANESolver, residual: tamaas._tamaas.Residual, model: tamaas._tamaas.Model) -> None`

```
beforeSolve (self: tamaas._tamaas.EPSolver) → None
```

```
getResidual (self: tamaas._tamaas.EPSolver) → tamaas._tamaas.Residual
```

```
getStrainIncrement (self: tamaas._tamaas.EPSolver) → GridBaseWrap<T>
```

**property** `max_iter`

**setToleranceManager** (*self*: `tamaas._tamaas.EPSolver`, *arg0*: `tamaas._tamaas._tolerance_manager`) → None

**solve** (*self*: `tamaas._tamaas.EPSolver`) → None

**property** `tolerance`

**updateState** (*self*: `tamaas._tamaas.EPSolver`) → None

Module defining convenience MPI routines.

`tamaas._tamaas.mpi.gather` (*arg0*: `GridWrap<T, dim>`) → `GridWrap<T, dim>`

Gather 2D surfaces

`tamaas._tamaas.mpi.global_shape` (*local\_shape*: `list[int]`) → `list[int]`

Gives the global shape of a 1D/2D local shape

`tamaas._tamaas.mpi.local_offset` (*global\_shape*: `list[int]`) → `int`

Gives the local offset of a 1D/2D global shape

`tamaas._tamaas.mpi.local_shape` (*global\_shape*: `list[int]`) → `list[int]`

Gives the local size of a 1D/2D global shape

`tamaas._tamaas.mpi.rank` () → `int`

Returns the rank of the local process

`tamaas._tamaas.mpi.scatter` (*arg0*: `GridWrap<T, dim>`) → `GridWrap<T, dim>`

Scatter 2D surfaces

**class** `tamaas._tamaas.mpi.sequential`

Bases: `pybind11_object`

**\_\_init\_\_** (*self*: `tamaas._tamaas.mpi.sequential`) → None

`tamaas._tamaas.mpi.size` () → `int`

Returns the number of MPI processes

Module defining basic computations on fields.

`tamaas._tamaas.compute.deviatoric` (*model\_type*: `tamaas._tamaas.model_type`, *deviatoric*: `GridWrap<T, dim>`, *field*: `GridWrap<T, dim>`) → None

Compute the deviatoric part of a tensor field

`tamaas._tamaas.compute.eigenvalues` (*model\_type*: `tamaas._tamaas.model_type`, *eigenvalues\_out*: `GridWrap<T, dim>`, *field*: `GridWrap<T, dim>`) → None

Compute eigenvalues of a tensor field

`tamaas._tamaas.compute.from_voigt` (*arg0*: `GridWrap<T, dim>`) → `GridWrap<T, dim>`

Convert a 3D tensor field to voigt notation

`tamaas._tamaas.compute.to_voigt` (*arg0*: `GridWrap<T, dim>`) → `GridWrap<T, dim>`

Convert a 3D tensor field to voigt notation

`tamaas._tamaas.compute.von_mises` (*model\_type*: `tamaas._tamaas.model_type`, *von\_mises*: `GridWrap<T, dim>`, *field*: `GridWrap<T, dim>`) → None

Compute the Von Mises invariant of a tensor field

### 11.1.3 Tamaas Dumpers for Model

Dumpers for the class *Model*.

```
class tamaas.dumpers.JSONDumper (file_descriptor: Union[str, PathLike, IOBase])
```

Bases: *ModelDumper*

Dumper to JSON.

```
__init__ (file_descriptor: Union[str, PathLike, IOBase])
```

Construct with file handle.

```
dump (model: Model)
```

Dump model.

```
classmethod read (fd: IO[str])
```

Read model from file.

```
class tamaas.dumpers.FieldDumper (basename: Union[str, PathLike], *fields, **kwargs)
```

Bases: *ModelDumper*

Abstract dumper for python classes using fields.

```
extension = ''
```

```
name_format = '{basename}{postfix}.{extension}'
```

```
__init__ (basename: Union[str, PathLike], *fields, **kwargs)
```

Construct with desired fields.

```
add_field (field: str)
```

Add another field to the dump.

```
get_fields (model: Model)
```

Get the desired fields.

```
dump (model: Model)
```

Dump model.

```
classmethod read (file_descriptor: Union[str, PathLike, IOBase])
```

Read model from file.

```
classmethod read_sequence (glob_pattern)
```

Read models from a file sequence.

```
property file_path
```

Get the default filename.

```
class tamaas.dumpers.NumpyDumper (basename: Union[str, PathLike], *fields, **kwargs)
```

Bases: *FieldDumper*

Dumper to compressed numpy files.

```
extension = 'npz'
```

```
classmethod read (file_descriptor: Union[str, PathLike, IOBase])
```

Create model from Numpy file.

```
__init__ (basename: Union[str, PathLike], *fields, **kwargs)
```

Construct with desired fields.

**add\_field** (*field: str*)

Add another field to the dump.

**dump** (*model: Model*)

Dump model.

**property file\_path**

Get the default filename.

**get\_fields** (*model: Model*)

Get the desired fields.

**name\_format** = '{**basename**}{**postfix**}.{**extension**}'

**classmethod read\_sequence** (*glob\_pattern*)

Read models from a file sequence.

**class** `tamaas.dumpers.H5Dumper` (*basename: Union[str, PathLike], \*fields, \*\*kwargs*)

Bases: *FieldDumper*

Dumper to HDF5 file format.

**extension** = 'h5'

**\_\_init\_\_** (*basename: Union[str, PathLike], \*fields, \*\*kwargs*)

Construct with desired fields.

**classmethod read** (*file\_descriptor: Union[str, PathLike, IOBase]*)

Create model from HDF5 file.

**add\_field** (*field: str*)

Add another field to the dump.

**dump** (*model: Model*)

Dump model.

**property file\_path**

Get the default filename.

**get\_fields** (*model: Model*)

Get the desired fields.

**name\_format** = '{**basename**}{**postfix**}.{**extension**}'

**classmethod read\_sequence** (*glob\_pattern*)

Read models from a file sequence.

**class** `tamaas.dumpers.UVWDumper` (*basename: Union[str, PathLike], \*fields, \*\*kwargs*)

Bases: *FieldDumper*

Dumper to VTK files for elasto-plastic calculations.

**extension** = 'vtr'

**\_\_init\_\_** (*basename: Union[str, PathLike], \*fields, \*\*kwargs*)

Construct with desired fields.

**add\_field** (*field: str*)

Add another field to the dump.

**dump** (*model: Model*)

Dump model.

**property file\_path**

Get the default filename.

**get\_fields** (*model: Model*)

Get the desired fields.

**name\_format** = '{basename}{postfix}.{extension}'

**classmethod read** (*file\_descriptor: Union[str, PathLike, IOBase]*)

Read model from file.

**classmethod read\_sequence** (*glob\_pattern*)

Read models from a file sequence.

**class** `tamaas.dumpers.UVWGroupDumper` (*basename: Union[str, PathLike], \*fields, \*\*kwargs*)

Bases: *FieldDumper*

Dumper to ParaViewData files.

**extension** = 'pvd'

**\_\_init\_\_** (*basename: Union[str, PathLike], \*fields, \*\*kwargs*)

Construct with desired fields.

**add\_field** (*field: str*)

Add another field to the dump.

**dump** (*model: Model*)

Dump model.

**property file\_path**

Get the default filename.

**get\_fields** (*model: Model*)

Get the desired fields.

**name\_format** = '{basename}{postfix}.{extension}'

**classmethod read** (*file\_descriptor: Union[str, PathLike, IOBase]*)

Read model from file.

**classmethod read\_sequence** (*glob\_pattern*)

Read models from a file sequence.

### 11.1.4 Tamaas Nonlinear solvers

Nonlinear solvers for plasticity problems.

Solvers in this module use `scipy.optimize` to solve the implicit non-linear equation for plastic deformations with fixed contact pressures.

**exception** `tamaas.nonlinear_solvers.NLNoConvergence`

Bases: `RuntimeError`

Convergence not reached exception.

`__init__` (\*args, \*\*kwargs)

`add_note` ()

Exception.add\_note(note) – add a note to the exception

**args**

`with_traceback` ()

Exception.with\_traceback(tb) – set self.\_\_traceback\_\_ to tb and return self.

**class** tamaas.nonlinear\_solvers.DFSANESolver (residual, model=None, callback=None)

Bases: ScipySolver

Solve using a spectral residual jacobianless method.

See doi:10.1090/S0025-5718-06-01840-0 for details on method and the relevant Scipy documentation for details on parameters.

`__init__` (residual, model=None, callback=None)

Construct nonlinear solver with residual.

#### Parameters

- **residual** – plasticity residual object
- **model** – Deprecated
- **callback** – passed on to the Scipy solver

`beforeSolve` (self: tamaas.\_tamaas.EPSolver) → None

`getResidual` (self: tamaas.\_tamaas.EPSolver) → *tamaas.\_tamaas.Residual*

`getStrainIncrement` (self: tamaas.\_tamaas.EPSolver) → GridBaseWrap<T>

`reset` ()

Set solution vector to zero.

`setToleranceManager` (self: tamaas.\_tamaas.EPSolver, arg0: tamaas.\_tamaas.\_tolerance\_manager) → None

`solve` ()

Solve  $R(\delta\epsilon) = 0$  using a Scipy function.

**property tolerance**

`updateState` (self: tamaas.\_tamaas.EPSolver) → None

tamaas.nonlinear\_solvers.DFSANECXXSolver

alias of *\_DFSANESolver*

**class** tamaas.nonlinear\_solvers.NewtonKrylovSolver (residual, model=None, callback=None)

Bases: ScipySolver

Solve using a finite-difference Newton-Krylov method.

`__init__` (residual, model=None, callback=None)

Construct nonlinear solver with residual.

#### Parameters

- **residual** – plasticity residual object

- **model** – Deprecated
- **callback** – passed on to the Scipy solver

**beforeSolve** (*self*: `tamaas._tamaas.EPSolver`) → None

**getResidual** (*self*: `tamaas._tamaas.EPSolver`) → `tamaas._tamaas.Residual`

**getStrainIncrement** (*self*: `tamaas._tamaas.EPSolver`) → `GridBaseWrap<T>`

**reset** ()

Set solution vector to zero.

**setToleranceManager** (*self*: `tamaas._tamaas.EPSolver`, *arg0*: `tamaas._tamaas._tolerance_manager`) → None

**solve** ()

Solve  $R(\delta\epsilon) = 0$  using a Scipy function.

**property tolerance**

**updateState** (*self*: `tamaas._tamaas.EPSolver`) → None

`tamaas.nonlinear_solvers.ToleranceManager` (*start*, *end*, *rate*)

Decorate solver to manage tolerance of non-linear solve step.

### 11.1.5 Tamaas utilities

Convenience utilities.

`tamaas.utils.log_context` (*log\_level*: `LogLevel`)

Context manager to easily control Tamaas' logging level.

`tamaas.utils.publications` (*format\_str*: `str = '{pub.citation}\n\t{pub.doi}'`)

Print publications associated with objects in use.

`tamaas.utils.load_path` (*solver*: `ContactSolver`, *loads*: `Iterable[Union[float, ndarray]]`, *verbose*: `bool = False`, *callback*=None) → `Iterable[Model]`

Generate model objects solutions for a sequence of applied loads.

#### Parameters

- **solver** – a contact solver object
- **loads** – an iterable sequence of loads
- **verbose** – print info output of solver
- **callback** – a callback executed after the yield

`tamaas.utils.seeded_surfaces` (*generator*: `Union[SurfaceGenerator1D, SurfaceGenerator2D]`, *seeds*: `Iterable[int]`) → `Iterable[ndarray]`

Generate rough surfaces with a prescribed seed sequence.

#### Parameters

- **generator** – surface generator object
- **seeds** – random seed sequence

`tamaas.utils.hertz_surface` (*system\_size: Iterable[float], shape: Iterable[int], radius: float*) → ndarray

Construct a parabolic surface.

#### Parameters

- **system\_size** – size of the domain in each direction
- **shape** – number of points in each direction
- **radius** – radius of surface

`tamaas.utils.radial_average` (*x: ndarray, y: ndarray, values: ndarray, r: ndarray, theta: ndarray, method: str = 'linear', endpoint: bool = False*) → ndarray

Compute the radial average of a 2D field.

Averages radially for specified r values. See `scipy.interpolate.RegularGridInterpolator` for more details.

## 11.2 C++ API

```
template<typename Iterator>
```

```
struct acc_range
```

```
    #include <accumulator.hh> Range for convenience.
```

#### Public Functions

```
inline Iterator begin () const
```

```
inline Iterator end () const
```

#### Public Members

```
Iterator _begin
```

```
Iterator _end
```

```
template<model_type type, typename Source, typename = std::enable_if_t<is_proxy<Source>::value>>
```

```
class Accumulator
```

```
    #include <accumulator.hh> Accumulation integral manager.
```

## Public Types

enum class **direction**

Direction flag.

*Values:*

enumerator **forward**

enumerator **backward**

## Public Functions

inline **Accumulator** ()

Constructor.

inline void **makeUniformMesh** (*UInt* N, *Real* domain\_size)

Initialize uniform mesh.

inline const *std::vector*<*Real*> &**nodePositions** () const

inline acc\_range<iterator<*direction::forward*>> **forward** (*std::vector*<*BufferType*> &nvalues, const *Grid*<*Real*, *trait::boundary\_dimension*> &wvectors)

Prepare forward loop.

inline acc\_range<iterator<*direction::backward*>> **backward** (*std::vector*<*BufferType*> &nvalues, const *Grid*<*Real*, *trait::boundary\_dimension*> &wvectors)

Prepare backward loop.

inline void **reset** (*std::vector*<*BufferType*> &nvalues, const *Grid*<*Real*, *trait::boundary\_dimension*> &wvectors)

inline *std::vector*<*BufferType*> &**nodeValue** ()

inline const *Grid*<*Real*, *trait::boundary\_dimension*> &**waveVectors** ()

inline auto **elements** ()

Create a range over the elements in the mesh.

## Private Types

using **trait** = *model\_type\_traits*<*type*>

using **BufferType** = *GridHermitian*<*Real*, *trait::boundary\_dimension*>

## Private Members

*std::array<BufferType, 2>* **accumulator**

*std::vector<Real>* **node\_positions**

*std::vector<BufferType>* \***node\_values**

const *Grid<Real, trait::boundary\_dimension>* \***wavevectors**

class **AdhesionFunctional** : public *tamaas::functional::Functional*

*#include <adhesion\_functional.hh>* *Functional* class for adhesion energy.

Subclassed by *tamaas::functional::ExponentialAdhesionFunctional*, *tamaas::functional::MaugisAdhesionFunctional*, *tamaas::functional::SquaredExponentialAdhesionFunctional*

## Public Functions

inline const *std::map<std::string, Real>* &**getParameters** () const

Get parameters.

inline void **setParameters** (*std::map<std::string, Real>* other)

Set parameters.

## Protected Functions

inline **AdhesionFunctional** (const *GridBase<Real>* &surface)

Constructor.

## Protected Attributes

*GridBase<Real>* **surface**

*std::map<std::string, Real>* **parameters**

class **AndersonMixing** : public *tamaas::EPICSolver*

*#include <anderson.hh>*

## Public Functions

**AndersonMixing** (*ContactSolver* &csolver, *EPSolver* &epsolver, *Real* tolerance = 1e-10, *UInt* memory = 5)

virtual *Real* **solve** (const *std::vector*<*Real*> &load) override

## Private Types

using **memory\_t** = *std::deque*<*GridBase*<*Real*>>

## Private Members

*UInt* **M**

## Private Static Functions

static *std::vector*<*Real*> **computeGamma** (const *memory\_t* &residual)

static *GridBase*<*Real*> **mixingUpdate** (*GridBase*<*Real*> x, *std::vector*<*Real*> gamma, const *memory\_t* &memory, const *memory\_t* &residual\_memory, *Real* relaxation)

template<size\_t nargs>

struct **Apply**

*#include* <apply.hh> Helper function for application of a functor on a *thrust::tuple*.

## Public Static Functions

template<typename **Functor**, typename **Tuple**, typename ...**Args**>  
static inline auto **apply** (*Functor* &&func, *Tuple* &&t, *Args*&&... args) -> decltype(*Apply*<nargs - 1>::apply(*std::forward*<*Functor*>(func), *std::forward*<*Tuple*>(t), *thrust::get*<nargs - 1>(t), *std::forward*<*Args*>(args)...))

template<>

struct **Apply**<0>

*#include* <apply.hh>

## Public Static Functions

template<typename **Functor**, typename **Tuple**, typename ...**Args**>  
static inline auto **apply** (*Functor* &&func, *Tuple*&&, *Args*&&... args) -> decltype(func(*std::forward*<*Args*>(args)...))

template<typename **Functor**, typename **ret\_type** = void>

class **ApplyFunctor**

*#include* <apply.hh> Helper class for functor application in *thrust*.

### Public Functions

```
inline ApplyFunctor (const Functor &functor)
```

```
inline ApplyFunctor (const ApplyFunctor &o)
```

```
template<typename Tuple>
```

```
inline ret_type operator () (Tuple &&t) const
```

### Private Members

```
const Functor &functor
```

```
template<typename T>
```

```
class arange
```

```
#include <loop.hh> Helper class to count iterations within lambda-loop.
```

### Public Types

```
using it_type = thrust::counting_iterator<T>
```

```
using reference = typename it_type::reference
```

### Public Functions

```
inline arange (T start, T size)
```

```
inline it_type begin (UInt = 1) const
```

```
inline it_type end (UInt = 1) const
```

```
inline UInt getNbComponents () const
```

### Private Members

```
T start
```

```
T range_size
```

```
template<typename T>
```

```
struct Array
```

```
#include <array.hh> Generic storage class with wrapping capacities.
```

## Public Functions

**Array** () = default

Default.

inline **Array** (*UInt* size)

Empty array of given size.

inline **Array** (const *Array* &v)

Copy constructor (deep)

inline **Array** (*Array* &&v) noexcept

Move constructor (transfers data ownership)

inline **Array** (*T* \*data, *UInt* size) noexcept

Wrap array on data.

inline **Array** (*span*<*T*> view) noexcept

Wrap on span.

inline **~Array** ()

Destructor.

inline *Array* &**operator=** (const *Array* &v)

Copy operator.

inline *Array* &**operator=** (*Array* &&v) noexcept

Move operator.

inline *Array* &**operator=** (*span*<*T*> v) noexcept

Wrap on view.

inline void **wrap** (const *Array* &other) noexcept

Wrap array.

inline void **wrap** (*span*<*T*> view) noexcept

Wrap view.

inline void **wrap** (*T* \*data, *UInt* size) noexcept

Wrap a memory pointer.

inline const *T* \***data** () const

Data pointer access (const)

inline *T* \***data** ()

Data pointer access (non-const)

inline void **resize** (*UInt* new\_size, const *T* &value = *T*())

Resize array.

inline void **reserve** (*UInt* size)

Reserve storage space.

inline *T* &**operator** [] (*UInt* i)

Access operator.

inline const *T* &**operator** [] (*UInt* i) const

Access operator (const)

```
inline UInt size () const
    Get size of array.
inline span<T> view () const
```

## Private Members

```
span<T> view_

span<T>::size_type reserved_ = 0

bool wrapped_ = false

Allocator<T> alloc_
```

```
class assertion_error : public std::invalid_argument
    #include <errors.hh>
```

```
class BeckTeboulle : public tamaas::Kato
    #include <beck_teboulle.hh>
```

## Public Functions

```
BeckTeboulle (Model &model, const GridBase<Real> &surface, Real tolerance, Real mu)
    Constructor.

virtual Real solve (std::vector<Real> g0) override
    Solve.
```

## Private Functions

```
template<model_type type>
Real solveTmpl (GridBase<Real> &g0)
    Template for solve function.
```

```
class BEEngine
    #include <be_engine.hh> Boundary equation engine class. Solves the Neumann/Dirichlet problem This class should
    be dimension and model-type agnostic.

    Subclassed by tamaas::BEEngineTmpl<type >
```

## Public Functions

```
inline BEEngine (Model *model)

virtual ~BEEngine () = default
    Destructor.

virtual void solveNeumann (GridBase<Real> &neumann, GridBase<Real> &dirichlet) const = 0
    Solve Neumann problem (expects boundary data)

virtual void solveDirichlet (GridBase<Real> &dirichlet, GridBase<Real> &neumann) const = 0
    Solve Dirichlet problem (expects boundary data)

virtual void registerNeumann () = 0
    Register neumann operator.

virtual void registerDirichlet () = 0
    Register dirichlet operator.

inline const Model &getModel () const
    Get model.

inline Real getNeumannNorm ()
    Compute L2 norm of influence functions.
```

## Protected Attributes

```
Model *model
```

```
std::map<IntegralOperator::kind, std::shared_ptr<IntegralOperator>> operators
```

```
template<model_type type>
```

```
class BEEngineTmpl : public tamaas::BEEngine
    #include <be_engine.hh>
```

## Public Functions

```
inline BEEngineTmpl (Model *model)

virtual void solveNeumann (GridBase<Real> &neumann, GridBase<Real> &dirichlet) const override
    Solve Neumann problem (expects boundary data)

virtual void solveDirichlet (GridBase<Real> &dirichlet, GridBase<Real> &neumann) const override
    Solve Dirichlet problem (expects boundary data)

virtual void registerNeumann () override
    Register neumann operator.

virtual void registerDirichlet () override
    Register dirichlet operator.

template<UInt m, UInt j>

struct boundary_fft_helper
```

## Public Static Functions

```
template<typename Buffer, typename Out>
static inline void backwardTransform (FFTEngine &e, Buffer &&buffer, Out &&out)
```

```
template<UInt m>
```

```
struct boundary_fft_helper<m, m>
```

## Public Static Functions

```
template<typename Buffer, typename Out>
static inline void backwardTransform (FFTEngine &e, Buffer &&buffer, Out &&out)
```

```
template<model_type type, UInt derivative>
```

```
class Boussinesq : public tamaas::VolumePotential<type>
```

```
    #include <boussinesq.hh> Boussinesq tensor.
```

## Public Functions

```
Boussinesq (Model *model)
```

Constructor.

```
virtual void apply (GridBase<Real> &source, GridBase<Real> &out) const override
```

Apply the *Boussinesq* operator.

## Protected Functions

```
void initialize (UInt source_components, UInt out_components)
```

## Private Types

```
using trait = model_type_traits<type>
```

```
using parent = VolumePotential<type>
```

```
template<UInt dim, UInt derivative_order>
```

```
class Boussinesq
```

Class for the *Boussinesq* tensor.

```
template<>
```

```
class Boussinesq<3, 0>
```

```
    #include <influence.hh> Subclassed by tamaas::influence::Boussinesq<3, 1 >
```

## Public Functions

```
inline Boussinesq (Real mu, Real nu)
```

Constructor.

```
template<bool apply_q_power = false, typename ST>
```

```
inline Vector<Complex, dim> applyU0 (const StaticVector<Complex, ST, dim> &t, const VectorProxy<const Real, dim - 1> &q) const
```

```
template<bool apply_q_power = false, typename ST>
```

```
inline Vector<Complex, dim> applyU1 (const StaticVector<Complex, ST, dim> &t, const VectorProxy<const Real, dim - 1> &q) const
```

## Protected Attributes

```
const Real mu
```

```
const Real nu
```

```
const Real lambda
```

## Protected Static Attributes

```
static constexpr UInt dim = 3
```

```
static constexpr UInt order = 0
```

```
template<>
```

```
class Boussinesq<3, 1> : protected tamaas::influence::Boussinesq<3, 0>
```

```
    #include <influence.hh> Boussinesq first gradient.
```

## Public Functions

```
template<bool apply_q_power = false, typename ST>
```

```
inline Matrix<Complex, dim, dim> applyU0 (const StaticVector<Complex, ST, dim> &t, const VectorProxy<const Real, dim - 1> &q) const
```

```
template<bool apply_q_power = false, typename ST>
```

```
inline Matrix<Complex, dim, dim> applyU1 (const StaticVector<Complex, ST, dim> &t, const VectorProxy<const Real, dim - 1> &q) const
```

## Protected Types

```
using parent = Boussinesq<3, 0>
```

## Protected Static Attributes

```
static constexpr UInt dim = parent::dim
```

```
static constexpr UInt order = parent::order + 1
```

```
template<model_type type, typename boussinesq_t>
```

```
struct BoussinesqHelper
```

```
    #include <boussinesq_helper.hh>
```

## Public Types

```
using trait = model_type_traits<type>
```

```
using BufferType = GridHermitian<Real, bdim>
```

```
using source_t = typename KelvinTrait<boussinesq_t>::source_t
```

```
using out_t = typename KelvinTrait<boussinesq_t>::out_t
```

## Public Functions

```
template<bool apply_q_power>
```

```
inline void apply (BufferType &tractions, std::vector<BufferType> &out, const Grid<Real, bdim>
    &wavevectors, Real domain_size, const boussinesq_t &boussinesq)
```

```
template<bool apply_q_power>
```

```
inline void apply (BufferType &tractions, BufferType &out, UInt layer, const Grid<Real, bdim> &wavevectors,
    UInt discretization, Real domain_size, const boussinesq_t &boussinesq)
```

```
inline void makeFundamentalModeGreatAgain (BufferType&, std::vector<BufferType>&,
    influence::ElasticHelper<dim>&)
```

```
template<typename ST>
```

```
inline void makeFundamentalModeGreatAgain (StaticVector<Complex, ST, dim>&, out_t&,
    influence::ElasticHelper<dim>&)
```

## Public Static Attributes

static constexpr *UInt* **dim** = *trait*::dimension

static constexpr *UInt* **bdim** = *trait*::boundary\_dimension

## Protected Attributes

Accumulator<*type*, *source\_t*> **accumulator**

really only here for mesh

template<*UInt* **dim**>

class **Cluster**

*#include* <flood\_fill.hh>

## Public Functions

**Cluster** (*Point* start, const *Grid*<bool, *dim*> &map, *Grid*<bool, *dim*> &visited, bool diagonal)

Constructor.

**Cluster** (const *Cluster* &other)

Copy constructor.

**Cluster** () = default

Default constructor.

inline *UInt* **getArea** () const

Get area of cluster.

inline *UInt* **getPerimeter** () const

Get perimeter of cluster.

inline const auto &**getPoints** () const

Get contact points.

*BBox* **boundingBox** () const

Get bounding box.

*std*::array<*Int*, *dim*> **extent** () const

Get bounding box extent.

auto **getNextNeighbors** (const *std*::array<*Int*, *dim*> &p)

Assign next neighbors.

auto **getDiagonalNeighbors** (const *std*::array<*Int*, *dim*> &p)

Assign diagonal neighbors.

auto **getNextNeighbors** (const *std*::array<*Int*, 1> &p)

auto **getDiagonalNeighbors** (const *std*::array<*Int*, 1>&)

```

auto getNextNeighbors (const std::array<Int, 2> &p)
auto getDiagonalNeighbors (const std::array<Int, 2> &p)
auto getNextNeighbors (const std::array<Int, 3> &p)
auto getDiagonalNeighbors (const std::array<Int, 3> &p)

```

## Private Types

```

using Point = std::array<Int, dim>

using BBox = std::pair<std::array<Int, dim>, std::array<Int, dim>>

```

## Private Members

```

std::vector<Point> points
    List of points in the cluster.

UInt perimeter = 0
    Perimeter size (number of segments)

```

```

struct comm
    #include <mpi_interface.hh>

```

## Public Functions

```

inline operator MPI_Comm () const

```

## Public Members

```

MPI_Comm _comm

```

## Public Static Functions

```

static comm &world ()

```

```

template<class Compute_t>
class ComputeOperator : public tamaas::IntegralOperator

```

## Public Functions

inline **ComputeOperator** (*Model* \*model)

Constructor.

inline virtual *IntegralOperator::kind* **getKind** () const override

Kind.

inline virtual *model\_type* **getType** () const override

Type.

inline virtual void **updateFromModel** () override

Update any data dependent on model parameters.

inline virtual void **apply** (*GridBase<Real>* &in, *GridBase<Real>* &out) const override

*Apply* functor.

class **Condat** : public *tamaas::Kato*

*#include* <condat.hh>

## Public Functions

**Condat** (*Model* &model, const *GridBase<Real>* &surface, *Real* tolerance, *Real* mu)

Constructor.

virtual *Real* **solve** (*std::vector<Real>* p0) override

Solve.

template<*model\_type type*>

*Real* **solveTpl** (*GridBase<Real>* &p0, *Real* grad\_step)

Template for solve function.

template<*UInt comp*>

void **updateGap** (*Real* sigma, *Real* grad\_step, *GridBase<Real>* &q)

Update gap.

template<*UInt comp*>

void **updateLagrange** (*GridBase<Real>* &q, *GridBase<Real>* &p0)

Update Lagrange multiplier q.

inline void **setGradStep** (*Real* gstep)

## Private Members

*std::unique\_ptr<GridBase<Real>>* **pressure\_old** = nullptr

*Real* **grad\_step** = 0.9

class **ContactSolver**

*#include* <contact\_solver.hh> Subclassed by *tamaas::Kato*, *tamaas::PolonskyKeerRey*

## Public Functions

**ContactSolver** (*Model* &model, const *GridBase<Real>* &surface, *Real* tolerance)

Constructor.

virtual **~ContactSolver** () = default

Destructor.

virtual void **printStats** (*UInt* iter, *Real* cost\_f, *Real* error) const

Print state of solve.

virtual void **logIteration** (*UInt* iter, *Real* cost\_f, *Real* error) const

Log iteration info.

inline auto **getMaxIterations** () const

Get maximum number of iterations.

inline void **setMaxIterations** (*UInt* n)

Set maximum number of iterations.

inline auto **getDumpFrequency** () const

Get dump\_frequency.

inline void **setDumpFrequency** (*UInt* n)

Set dump\_frequency.

void **addFunctionalTerm** (*std::shared\_ptr<functional::Functional>* func)

Add term to functional.

inline const *functional::Functional* &**getFunctional** () const

Returns functional object.

void **setFunctional** (*std::shared\_ptr<functional::Functional>* func)

Sets functional sum to a single term.

virtual void **updateState** ()

Update internal variables (if any)

inline virtual *Real* **solve** (*std::vector<Real>*)

Solve for a mean traction vector.

inline virtual *Real* **solve** (*Real* load)

Solve for normal pressure.

**TAMAAS\_ACCESSOR** (*tolerance*, *Real*, Tolerance)

Accessor for tolerance.

inline *GridBase<Real>* &**getSurface** ()

inline *Model* &**getModel** ()

## Protected Functions

void **warnToleranceExceeded** (*Real* error) const

## Protected Attributes

*Model* &**model**

*GridBase*<*Real*> **surface**

*std::shared\_ptr*<*GridBase*<*Real*>> **\_gap** = nullptr

*functional::MetaFunctional* **functional**

*Real* **tolerance**

*UInt* **max\_iterations** = 1000

*Real* **surface\_stddev**

*UInt* **dump\_frequency** = 100

```
class CuFFTEngine : public tamaas::FFTEngine  
    #include <cufft_engine.hh>
```

## Public Functions

inline explicit **CuFFTEngine** (unsigned int flags = FFTW\_ESTIMATE) noexcept  
 Initialize with flags.

inline virtual void **forward** (const *Grid*<*Real*, 1> &real, *GridHermitian*<*Real*, 1> &spectral) override  
 Execute a forward plan on real and spectral 1D.

inline virtual void **forward** (const *Grid*<*Real*, 2> &real, *GridHermitian*<*Real*, 2> &spectral) override  
 Execute a forward plan on real and spectral 2D.

inline virtual void **backward** (*Grid*<*Real*, 1> &real, *GridHermitian*<*Real*, 1> &spectral) override  
 Execute a backward plan on real and spectral 1D.

inline virtual void **backward** (*Grid*<*Real*, 2> &real, *GridHermitian*<*Real*, 2> &spectral) override  
 Execute a backward plan on real and spectral 2D.

inline unsigned int **flags** () const

## Public Static Functions

static inline auto **cast** (*Complex* \*data)

Cast to FFTW complex type.

static inline auto **cast** (const *Complex* \*data)

## Protected Attributes

unsigned int **\_flags**

FFTW flags.

*std::map*<key\_t, *plan\_t*> **plans**

plans corresponding to signatures

## Private Types

using **plan\_t** = *std::pair*<*cufft::plan*, *cufft::plan*>

## Private Functions

template<*UInt* dim>

void **forwardImpl** (const *Grid*<*Real*, dim> &real, *GridHermitian*<*Real*, dim> &spectral)

Perform forward (R2C) transform.

template<*UInt* dim>

void **backwardImpl** (*Grid*<*Real*, dim> &real, const *GridHermitian*<*Real*, dim> &spectral)

Perform backward (C2R) transform.

*plan\_t* &**getPlans** (key\_t key)

Return the plans pair for a given transform signature.

template<bool **upper**>

struct **cutoff\_functor**

*#include* <kelvin\_helper.hh>

## Public Functions

inline void **operator** () (*VectorProxy*<const *Real*, bdim> qv, source\_t wj0, source\_t wj1, out\_t out\_i) const

## Public Members

*Real* **x**

*Real* **xc**

*Real* **dx**

*Real* **cutoff**

kelvin\_t **kelvin**

```
class DCFFT : public tamaas::Westergaard<model_type::basic_2d, IntegralOperator::neumann>
  #include <dcfft.hh> Non-periodic Boussinesq operator, computed with padded FFT.
```

## Public Functions

**DCFFT** (*Model* \*model)

virtual void **apply** (*GridBase*<*Real*> &input, *GridBase*<*Real*> &output) const override  
Apply influence coefficients in Fourier domain.

## Private Types

```
using trait = model_type_traits<model_type::basic_2d>
```

## Private Functions

void **initInfluence** ()  
Init influence with real-space square patch solution.

## Private Members

```
mutable Grid<Real, bdim> extended_buffer
```

## Private Static Attributes

```
static constexpr UInt dim = trait::dimension
```

```
static constexpr UInt bdim = trait::boundary_dimension
```

```
static constexpr UInt comp = trait::components
```

```
template<UInt derivative>
```

```
struct derivative_traits
```

Trait type for component management.

```
template<>
```

```
struct derivative_traits<0>
```

```
#include <volume_potential.hh>
```

### Public Static Attributes

```
template<model_type type>
```

```
static constexpr UInt source_components = model_type_traits<type>::components
```

```
template<model_type type>
```

```
static constexpr UInt out_components = model_type_traits<type>::components
```

```
template<>
```

```
struct derivative_traits<1>
```

```
#include <volume_potential.hh>
```

### Public Static Attributes

```
template<model_type type>
```

```
static constexpr UInt source_components = model_type_traits<type>::voigt
```

```
template<model_type type>
```

```
static constexpr UInt out_components = model_type_traits<type>::components
```

```
template<>
```

```
struct derivative_traits<2>
```

```
#include <volume_potential.hh>
```

### Public Static Attributes

```
template<model_type type>
```

```
static constexpr UInt source_components = model_type_traits<type>::voigt
```

```
template<model_type type>
```

```
static constexpr UInt out_components = model_type_traits<type>::voigt
```

```
struct Deviatoric
```

```
#include <computes.hh> Compute deviatoric of tensor field.
```

## Public Static Functions

```
template<UInt dim>
static inline void call (Grid<Real, dim> &dev, const Grid<Real, dim> &field)
```

```
class DFSANESolver : public tamaas::EPSolver
```

```
#include <dfsane_solver.hh> Derivative-free non-linear solver.
```

This algorithm is based on W. La Cruz, J. Martínez, and M. Raydan, “Spectral residual method without gradient information for solving large-scale nonlinear systems of equations,” *Math. Comp.*, vol. 75, no. 255, pp. 1429–1448, 2006, doi: 10.1090/S0025-5718-06-01840-0.

The same algorithm is available in `scipy.optimize`, but this version is robustly parallel by default (i.e. does not depend on BLAS’s parallelism and is future-proof for MPI parallelism).

## Public Functions

```
DFSANESolver (Residual &residual)
```

```
virtual void solve () override
```

```
TAMAAS_ACCESSOR (max_iterations, UInt, MaxIterations)
```

## Protected Functions

```
Real computeSpectralCoeff (const std::pair<Real, Real> &bounds)
```

```
void computeSearchDirection (Real sigma)
```

```
void lineSearch (Real eta_k)
```

## Protected Attributes

```
GridBase<Real> search_direction
```

```
GridBase<Real> previous_residual
```

```
GridBase<Real> current_x
```

```
GridBase<Real> delta_x
```

```
GridBase<Real> delta_residual
```

```
std::deque<Real> previous_merits
```

```
std::function<Real(UInt)> eta
```

```
UInt max_iterations = 100
```

### Protected Static Functions

```
static Real computeAlpha (Real alpha, Real f, Real fk, const std::pair<Real, Real> &bounds)
```

```
struct Eigenvalues
```

```
#include <computes.hh> Compute eigenvalues of a symmetric matrix field.
```

### Public Static Functions

```
template<UInt dim>
static inline void call (Grid<Real, dim> &eigs, const Grid<Real, dim> &field)
```

```
class ElasticFunctional : public tamaas::functional::Functional
```

```
#include <elastic_functional.hh> Generic functional for elastic energy.
```

```
Subclassed by tamaas::functional::ElasticFunctionalGap, tamaas::functional::ElasticFunctionalPressure
```

### Public Functions

```
inline ElasticFunctional (const IntegralOperator &op, const GridBase<Real> &surface)
```

### Protected Attributes

```
const IntegralOperator &op
```

```
GridBase<Real> surface
```

```
mutable std::unique_ptr<GridBase<Real>> buffer
```

```
class ElasticFunctionalGap : public tamaas::functional::ElasticFunctional
```

```
#include <elastic_functional.hh> Functional with gap as primal field.
```

### Public Functions

```
virtual Real computeF (GridBase<Real> &gap, GridBase<Real> &dual) const override
    Compute functional with input gap.
```

```
virtual void computeGradF (GridBase<Real> &gap, GridBase<Real> &gradient) const override
    Compute functional gradient with input gap.
```

```
inline ElasticFunctional (const IntegralOperator &op, const GridBase<Real> &surface)
```

```
class ElasticFunctionalPressure : public tamaas::functional::ElasticFunctional
```

```
#include <elastic_functional.hh> Functional with pressure as primal field.
```

## Public Functions

virtual *Real* **computeF** (*GridBase<Real>* &pressure, *GridBase<Real>* &dual) const override

Compute functional with input pressure.

virtual void **computeGradF** (*GridBase<Real>* &pressure, *GridBase<Real>* &gradient) const override

Compute functional gradient with input pressure.

inline **ElasticFunctional** (const *IntegralOperator* &op, const *GridBase<Real>* &surface)

template<*UInt* dim>

struct **ElasticHelper**

*#include* <influence.hh> Functor to apply *Hooke's* tensor.

## Public Functions

inline **ElasticHelper** (*Real* mu, *Real* nu)

template<typename **DT**, typename **ST**>

inline *Matrix*<*std::remove\_cv\_t*<*DT*>, *dim*, *dim*> **operator** () (const *StaticMatrix*<*DT*, *ST*, *dim*, *dim*> &gradu) const

template<typename **DT**, typename **ST**>

inline *SymMatrix*<*std::remove\_cv\_t*<*DT*>, *dim*> **operator** () (const *StaticSymMatrix*<*DT*, *ST*, *dim*> &eps) const

template<typename **DT**, typename **ST**>

inline *Matrix*<*std::remove\_cv\_t*<*DT*>, *dim*, *dim*> **inverse** (const *StaticMatrix*<*DT*, *ST*, *dim*, *dim*> &sigma) const

template<typename **DT**, typename **ST**>

inline *SymMatrix*<*std::remove\_cv\_t*<*DT*>, *dim*> **inverse** (const *StaticSymMatrix*<*DT*, *ST*, *dim*> &sigma) const

## Public Members

const *Real* **mu**

const *Real* **nu**

const *Real* **lambda**

const *Real* **E**

class **EPICSolver**

*#include* <epic.hh> Subclassed by *tamaas::AndersonMixing*

## Public Functions

**EPICSolver** (*ContactSolver* &csolver, *EPSolver* &epsolver, *Real* tolerance = 1e-10, *Real* relaxation = 0.3)  
 Constructor.

virtual *Real* **solve** (const *std::vector<Real>* &load)

*Real* **acceleratedSolve** (const *std::vector<Real>* &load)

*Real* **computeError** (const *GridBase<Real>* &current, const *GridBase<Real>* &prev, *Real* factor) const

void **fixedPoint** (*GridBase<Real>* &result, const *GridBase<Real>* &x, const *GridBase<Real>* &initial\_surface, *std::vector<Real>* load)

template<*model\_type type*>

void **setViews** ()

**TAMAAS\_ACCESSOR** (*tolerance, Real*, Tolerance)

**TAMAAS\_ACCESSOR** (*relaxation, Real*, Relaxation)

**TAMAAS\_ACCESSOR** (*max\_iterations, UInt*, MaxIterations)

inline const *Model* &**getModel** () const

## Protected Attributes

*GridBase<Real>* **surface**

corrected surface

*GridBase<Real>* **pressure**

current pressure

*std::unique\_ptr<GridBase<Real>>* **residual\_disp**

plastic residual disp

*std::unique\_ptr<GridBase<Real>>* **pressure\_inc**

pressure increment

*ContactSolver* &**csolver**

*EPSolver* &**epsolver**

*Real* **tolerance**

*Real* **relaxation**

*UInt* **max\_iterations** = 1000

class **EPSolver**

*#include <ep\_solver.hh>* Subclassed by *tamaas::DFSANESolver*, *tamaas::petsc::NonlinearSolver*

## Public Functions

**EPSolver** (*Residual* &residual)

Constructor.

virtual **~EPSolver** () = default

Destructor.

virtual void **solve** () = 0

virtual void **updateState** ()

virtual void **beforeSolve** ()

inline *GridBase<Real>* &**getStrainIncrement** ()

inline *Residual* &**getResidual** ()

inline *Real* **getTolerance** () const

inline void **setTolerance** (*Real* tol)

inline void **setToleranceManager** (*ToleranceManager* manager)

## Protected Attributes

*std::shared\_ptr<GridBase<Real>>* **\_x**

*Residual* &**\_residual**

*ToleranceManager* **abs\_tol** = {1e-9, 1e-9, 1}

class **Exception** : public *std::exception*

*#include <tamaas.hh>* Generic exception class.

## Public Functions

inline **Exception** (*std::string* mesg)

Constructor.

inline const char \***what** () const noexcept override

**~Exception** () override = default

## Private Members

*std::string* **msg**  
message of exception

class **ExponentialAdhesionFunctional** : public *tamaas::functional::AdhesionFunctional*  
*#include* <adhesion\_functional.hh> Exponential adhesion functional.

## Public Functions

inline **ExponentialAdhesionFunctional** (const *GridBase<Real>* &surface)  
Explicit declaration of constructor for swig.

virtual *Real* **computeE** (*GridBase<Real>* &gap, *GridBase<Real>* &pressure) const override  
Compute the total adhesion energy.

virtual void **computeGradE** (*GridBase<Real>* &gap, *GridBase<Real>* &gradient) const override  
Compute the gradient of the adhesion functional.

template<*UInt* **interpolation\_order**>

struct **ExponentialElement**

template<>

struct **ExponentialElement**<1>

*#include* <element.hh>

## Public Static Functions

template<*UInt* **shape**>  
static inline constexpr *Polynomial<Real, 1>* **shapes** ()

static inline constexpr auto **sign** (bool upper)

template<bool **upper**, *UInt* **shape**>  
static inline constexpr auto **g0** (*Real* q)

template<bool **upper**, *UInt* **shape**>  
static inline constexpr auto **g1** (*Real* q)

class **FFTEngine**

*#include* <fft\_engine.hh> Subclassed by *tamaas::CuFFTEngine*, *tamaas::FFTWEngine*

## Public Functions

virtual **~FFTEngine** () noexcept = default

virtual void **forward** (const *Grid*<*Real*, 1> &real, *GridHermitian*<*Real*, 1> &spectral) = 0  
Execute a forward plan on real and spectral 1D.

virtual void **forward** (const *Grid*<*Real*, 2> &real, *GridHermitian*<*Real*, 2> &spectral) = 0  
Execute a forward plan on real and spectral 2D.

virtual void **backward** (*Grid*<*Real*, 1> &real, *GridHermitian*<*Real*, 1> &spectral) = 0  
Execute a backward plan on real and spectral 1D.

virtual void **backward** (*Grid*<*Real*, 2> &real, *GridHermitian*<*Real*, 2> &spectral) = 0  
Execute a backward plan on real and spectral 2D.

## Public Static Functions

template<typename **T**, *UInt* **dim**, bool **hermitian**>  
static *Grid*<**T**, **dim**> **computeFrequencies** (const *std::array*<*UInt*, **dim**> &sizes)  
Fill a grid with wavevector values in appropriate ordering.

template<*UInt* **dim**>  
static *std::vector*<*std::array*<*UInt*, **dim**>> **realCoefficients** (const *std::array*<*UInt*, **dim**> &sizes)  
Return the grid indices that contain real coefficients (see R2C transform)

static *std::unique\_ptr*<*FFTEngine*> **makeEngine** (unsigned int flags = FFTW\_ESTIMATE)  
Instantiate an appropriate *FFTEngine* subclass.

template<>  
static *std::vector*<*std::array*<*UInt*, 2>> **realCoefficients** (const *std::array*<*UInt*, 2> &local\_sizes)

template<>  
static *std::vector*<*std::array*<*UInt*, 1>> **realCoefficients** (const *std::array*<*UInt*, 1> &local\_sizes)

## Protected Types

using **key\_t** = *std::basic\_string*<*UInt*>

## Protected Static Functions

template<*UInt* **dim**>  
static *key\_t* **make\_key** (const *Grid*<*Real*, **dim**> &real, const *GridHermitian*<*Real*, **dim**> &spectral)  
Make a transform signature from a pair of grids.

template<typename **T**>

struct **FFTWAllocator**

*#include* <*fftw\_allocator.hh*> Class allocating **SIMD** aligned memory

## Public Static Functions

static inline *span*<*T*> **allocate** (typename *span*<*T*>::size\_type n) noexcept  
Allocate memory.

static inline void **deallocate** (*span*<*T*> view) noexcept  
Free memory.

class **FFTWEngine** : public *tamaas::FFTEngine*  
*#include* <*fftw\_engine.hh*> Subclassed by *tamaas::FFTWMPIEngine*

## Public Functions

inline explicit **FFTWEngine** (unsigned int flags = FFTW\_ESTIMATE) noexcept  
Initialize with flags.

inline virtual void **forward** (const *Grid*<*Real*, 1> &real, *GridHermitian*<*Real*, 1> &spectral) override  
Execute a forward plan on real and spectral 1D.

inline virtual void **forward** (const *Grid*<*Real*, 2> &real, *GridHermitian*<*Real*, 2> &spectral) override  
Execute a forward plan on real and spectral 2D.

inline virtual void **backward** (*Grid*<*Real*, 1> &real, *GridHermitian*<*Real*, 1> &spectral) override  
Execute a backward plan on real and spectral 1D.

inline virtual void **backward** (*Grid*<*Real*, 2> &real, *GridHermitian*<*Real*, 2> &spectral) override  
Execute a backward plan on real and spectral 2D.

inline unsigned int **flags** () const

## Public Static Functions

static inline auto **cast** (*Complex* \*data)  
Cast to FFTW complex type.

static inline auto **cast** (const *Complex* \*data)

## Protected Types

using **plan\_t** = *std::pair*<*fftw::plan*<*Real*>, *fftw::plan*<*Real*>>

using **complex\_t** = *fftw::helper*<*Real*>::complex

## Protected Functions

template<U**Int** **dim**>  
void **forwardImpl** (const *Grid<Real, dim>* &real, *GridHermitian<Real, dim>* &spectral)  
    Perform forward (R2C) transform.

template<U**Int** **dim**>  
void **backwardImpl** (*Grid<Real, dim>* &real, const *GridHermitian<Real, dim>* &spectral)  
    Perform backward (C2R) transform.

*plan\_t* &**getPlans** (key\_t key)  
    Return the plans pair for a given transform signature.

## Protected Attributes

unsigned int **\_flags**  
    FFTW flags.

*std::map<key\_t, plan\_t>* **plans**  
    plans corresponding to signatures

class **FFTWMPIDeEngine** : public *tamaas::FFTWEngine*  
    #include <fftw\_mpi\_engine.hh>

## Public Functions

inline virtual void **forward** (const *Grid<Real, 1>&*, *GridHermitian<Real, 1>&*) override  
    Execute a forward plan on real and spectral 1D.

inline virtual void **backward** (*Grid<Real, 1>&*, *GridHermitian<Real, 1>&*) override  
    Execute a backward plan on real and spectral 1D.

virtual void **forward** (const *Grid<Real, 2>* &real, *GridHermitian<Real, 2>* &spectral) override  
    FFTW/MPI forward (r2c) transform.

virtual void **backward** (*Grid<Real, 2>* &real, *GridHermitian<Real, 2>* &spectral) override  
    FFTW/MPI backward (c2r) transform.

inline explicit **FFTWEngine** (unsigned int flags = FFTW\_ESTIMATE) noexcept  
    Initialize with flags.

## Protected Functions

*plan\_t* &**getPlans** (key\_t key)  
    Return the plans pair for a given transform signature.

## Protected Attributes

`std::map<key_t, Grid<Real, 2>> workspaces`

Buffer for real data because of FFTW/MPI layout.

## Protected Static Functions

static key\_t **make\_key** (const *Grid<Real, 2>* &real, const *GridHermitian<Real, 2>* &spectral)

Make a transform signature from a pair of grids.

static auto **local\_size** (const key\_t &key)

Get FFTW local sizes from an hermitian grid.

struct **FieldContainer**

*#include <field\_container.hh>* Subclassed by *tamaas::IntegralOperator*, *tamaas::Model*

## Public Types

using **Key** = *std::string*

template<class **T**>

using **GridBasePtr** = *std::shared\_ptr<GridBase<T>>*

using **Value** = *boost::variant<GridBasePtr<Real>, GridBasePtr<UInt>, GridBasePtr<Int>, GridBasePtr<Complex>, GridBasePtr<bool>>*

using **FieldsMap** = *std::unordered\_map<Key, Value>*

## Public Functions

virtual **~FieldContainer** () = default

Destructor.

inline const *Value* &**at** (const *Key* &name) const

Access field pointer in const context.

inline *Value* &**operator[]** (const *Key* &name)

Access/insert new pointer.

template<class **T**>

inline auto &**field** (const *Key* &name)

Access field of given type (non-const)

template<class **T**>

inline const auto &**field** (const *Key* &name) const

Access field of given type (const)

```
inline decltype(auto) fields () const
```

Return field keys.

```
inline const auto &fields_map () const
```

Return pointer map to fields.

```
template<model_type type, bool boundary, typename T, template<typename, UInt> class GridType = Grid, class Container = void>
```

```
inline std::shared_ptr<GridType<T, detail::dim_choice<type, boundary>::value>> request (const Key &name, Container &&n, UInt nc)
```

Return a field with given dimension, create if not in container.

```
template<bool boundary, typename T, typename Container>
```

```
inline decltype(auto) request (const Key &name, model_type type, Container &&n, UInt nc)
```

Return a field with given dimension, create if not in container.

## Private Members

*FieldsMap* **fields\_**

```
template<UInt dim>
```

```
class Filter
```

*#include* <filter.hh> Subclassed by *tamaas::Isopowerlaw*< *dim* >, *tamaas::RegularizedPowerlaw*< *dim* >

## Public Functions

```
Filter () = default
```

Default constructor.

```
virtual ~Filter () = default
```

Destructor.

```
virtual void computeFilter (GridHermitian<Real, dim> &filter_coefficients) const = 0
```

Compute *Filter* coefficients.

## Protected Functions

```
template<typename T>
```

```
void computeFilter (T &&f, GridHermitian<Real, dim> &filter) const
```

Compute filter coefficients using lambda.

```
class FloodFill
```

*#include* <flood\_fill.hh>

## Public Static Functions

static *List*<1> **getSegments** (const *Grid*<bool, 1> &map)

Return a list of connected segments.

static *List*<2> **getClusters** (const *Grid*<bool, 2> &map, bool diagonal)

Return a list of connected areas.

static *List*<3> **getVolumes** (const *Grid*<bool, 3> &map, bool diagonal)

Return a list of connected volumes.

## Private Types

template<*UInt* dim>

using **List** = *std::vector*<*Cluster*<dim>>

template<template<typename> class **Trait**, typename ...**T**>

struct **fold\_trait** : public *tamaas::detail::fold\_trait\_tail\_rec*<true, *Trait*, *T*...>

*#include* <tamaas.hh>

template<bool **acc**, template<typename> class **Trait**, typename **Head**, typename ...**Tail**>

struct **fold\_trait\_tail\_rec** : public *std::integral\_constant*<bool, *fold\_trait\_tail\_rec*<**acc** and *Trait*<**Head**>::value, *Trait*, *Tail*...>::value>

*#include* <tamaas.hh>

template<bool **acc**, template<typename> class **Trait**, typename **Head**>

struct **fold\_trait\_tail\_rec**<**acc**, *Trait*, *Head*> : public *std::integral\_constant*<bool, **acc** and *Trait*<**Head**>::value>

*#include* <tamaas.hh>

class **Functional**

*#include* <functional.hh> Generic functional class for the cost function of the optimization problem.

Subclassed by *tamaas::functional::AdhesionFunctional*, *tamaas::functional::ElasticFunctional*, *tamaas::functional::MetaFunctional*

## Public Functions

virtual ~**Functional** () = default

Destructor.

virtual *Real* **computeF** (*GridBase*<*Real*> &variable, *GridBase*<*Real*> &dual) const = 0

Compute functional.

virtual void **computeGradF** (*GridBase*<*Real*> &variable, *GridBase*<*Real*> &gradient) const = 0

Compute functional gradient.

template<*UInt* **N**, *UInt*... **ns**>

```
struct get : public detail::get_rec<N, ns...>
    #include <static_types.hh>
template<UInt n, UInt... ns>
struct get_rec<0, n, ns...> : public std::integral_constant<UInt, n>
    #include <static_types.hh>
template<typename T, UInt dim>
class Grid : public tamaas::GridBase<T>
```

#include <grid.hh> Multi-dimensional & multi-component array class.

This class is a container for multi-component data stored on a multi-dimensional grid.

The access function is the parenthesis operator. For a grid of dimension *d*, the operator takes *d*+1 arguments: the first *d* arguments are the position on the grid and the last one is the component of the stored data.

It is also possible to use the access operator with only one argument, it is then considering the grid as a flat array, accessing the given cell of the array.

Subclassed by *tamaas::GridHermitian*<*Real*, *bdim*>, *tamaas::GridHermitian*<*Real*, *trait::boundary\_dimension*>, *tamaas::GridHermitian*<*Real*, *dim*>

## Public Types

```
using value_type = T
```

```
using reference = value_type&
```

## Public Functions

```
Grid ()
```

Constructor by default (empty array)

```
template<typename RandomAccessIterator>
```

```
Grid (RandomAccessIterator begin, RandomAccessIterator end, UInt nb_components)
```

Constructor with shape from iterators.

```
template<typename RandomAccessIterator>
```

```
Grid (RandomAccessIterator begin, RandomAccessIterator end, UInt nb_components, span<value_type> data)
```

Construct with shape from iterators on data view.

```
template<typename Container>
```

```
inline Grid (Container &&n, UInt nb_components)
```

Constructor with container as shape.

```
template<typename Container>
```

```
inline Grid (Container &&n, UInt nb_components, span<value_type> data)
```

Constructor with shape and wrapped data.

```
inline Grid (const std::initializer_list<UInt> &n, UInt nb_components)
```

Constructor with initializer list.

```

inline Grid (const Grid &o)
    Copy constructor.

inline Grid (Grid &&o) noexcept
    Move constructor (transfers data ownership)

~Grid () override = default
    Destructor.

void resize (const std::array<UInt, dim> &n)
    Resize array.

void resize (const std::vector<UInt> &n)
    Resize array (from std::vector)

void resize (std::initializer_list<UInt> n)
    Resize array (from initializer list)

template<typename ForwardIt>
void resize (ForwardIt begin, ForwardIt end)
    Resize array (from iterators)

inline UInt computeSize () const
    Compute size.

inline virtual UInt getDimension () const override
    Get grid dimension.

void computeStrides ()
    Compute strides.

virtual void printself (std::ostream &str) const
    Print.

inline const std::array<UInt, dim> &sizes () const
    Get sizes.

inline const std::array<UInt, dim + 1> &getStrides () const
    Get strides.

template<typename ...T1>
inline std::enable_if_t<is_valid_index<T1...>::value, T&> operator () (T1... args)
    Variadic access operator (non-const)

template<typename ...T1>
inline std::enable_if_t<is_valid_index<T1...>::value, const T&> operator () (T1... args) const
    Variadic access operator.

template<std::size_t tdim>
inline T &operator () (std::array<UInt, tdim> tuple)
    Tuple index access operator.

template<std::size_t tdim>
inline const T &operator () (std::array<UInt, tdim> tuple) const

Grid &operator= (const Grid &other)

```

```
Grid &operator= (Grid &&other) noexcept

template<typename T1>
void copy (const Grid<T1, dim> &other)

template<typename T1>
void move (Grid<T1, dim> &&other) noexcept

template<typename Container>
inline void wrap (GridBase<T> &other, Container &&n)

template<typename Container>
inline void wrap (const GridBase<T> &other, Container &&n)

inline void wrap (Grid &other)

inline void wrap (const Grid &other)
```

### Public Static Attributes

```
static constexpr UInt dimension = dim
```

### Protected Attributes

```
std::array<UInt, dim> n
    shape of grid: size per dimension
```

```
std::array<UInt, dim + 1> strides
    strides for access
```

### Private Types

```
template<typename ...D>
using is_valid_index = fold_trait<std::is_integral, D...>
```

### Private Functions

```
template<typename Container>
void init (const Container &n, UInt nb_components)
    Init from standard container.

template<typename ...T1>
inline UInt unpackOffset (UInt offset, UInt index_pos, UInt index, T1... rest) const
    Unpacking the arguments of variadic ()

template<typename ...T1>
inline UInt unpackOffset (UInt offset, UInt index_pos, UInt index) const
    End case for recursion.

template<std::size_t tdim>
```

```
inline UInt computeOffset (std::array<UInt, tdim> tuple) const
```

Computing offset for a tuple index.

```
template<typename T>
```

```
class GridBase
```

*#include <grid\_base.hh>* Dimension agnostic grid with components stored per points.

Subclassed by *tamaas::Grid< complex< Real >, dim >*, *tamaas::Grid< complex< T >, dim >*, *tamaas::Grid< Real, trait::boundary\_dimension >*, *tamaas::Grid< Real, bdim >*, *tamaas::Grid< Real, dim >*, *tamaas::Grid< T, dim >*

## Public Types

```
using iterator = iterator_::iterator<T>
```

```
using const_iterator = iterator_::iterator<const T>
```

```
using value_type = T
```

```
using reference = value_type&
```

## Public Functions

```
GridBase () = default
```

Constructor by default.

```
inline GridBase (const GridBase &o)
```

Copy constructor.

```
inline GridBase (GridBase &&o) noexcept
```

Move constructor (transfers data ownership)

```
inline explicit GridBase (UInt nb_points, UInt nb_components = 1)
```

Initialize with size.

```
virtual ~GridBase () = default
```

Destructor.

```
inline virtual UInt getDimension () const
```

Get grid dimension.

```
inline const T *getInternalData () const
```

Get internal data pointer (const)

```
inline T *getInternalData ()
```

Get internal data pointer (non-const)

```
inline UInt getNbComponents () const
```

Get number of components.

```
inline void setNbComponents (UInt n)
```

Set number of components.

```
inline virtual UInt dataSize () const
    Get total size.

inline UInt globalDataSize () const
    Get global data size.

inline UInt getNbPoints () const
    Get number of points.

inline UInt getGlobalNbPoints () const
    Get global number of points.

void uniformSetComponents (const GridBase<T> &vec)
    Set components.

inline void resize (UInt size)
    Resize.

inline void reserve (UInt size)
    Reserve storage w/o changing data logic.

inline virtual iterator begin (UInt n = 1)

inline virtual iterator end (UInt n = 1)

inline virtual const_iterator begin (UInt n = 1) const

inline virtual const_iterator end (UInt n = 1) const

inline decltype(auto) view () const

inline T &operator () (UInt i)

inline const T &operator () (UInt i) const

template<typename T1>
GridBase &operator+= (const GridBase<T1> &other)

template<typename T1>
GridBase &operator*= (const GridBase<T1> &other)

template<typename T1>
GridBase &operator--= (const GridBase<T1> &other)

template<typename T1>
GridBase &operator/= (const GridBase<T1> &other)

template<typename T1>
T dot (const GridBase<T1> &other) const

inline GridBase &operator+= (const T &e)

inline GridBase &operator*= (const T &e)

inline GridBase &operator--= (const T &e)

inline GridBase &operator/= (const T &e)
```

```

inline GridBase &operator= (const T &e)

template<typename DT, typename ST, UInt size>
GridBase &operator+= (const StaticArray<DT, ST, size> &b)

template<typename DT, typename ST, UInt size>
GridBase &operator-= (const StaticArray<DT, ST, size> &b)

template<typename DT, typename ST, UInt size>
GridBase &operator*= (const StaticArray<DT, ST, size> &b)

template<typename DT, typename ST, UInt size>
GridBase &operator/= (const StaticArray<DT, ST, size> &b)

template<typename DT, typename ST, UInt size>
GridBase &operator= (const StaticArray<DT, ST, size> &b)

inline T min () const

inline T max () const

inline T sum () const

inline T mean () const

inline T var () const

inline T l2norm () const

inline GridBase &operator= (const GridBase &o)

inline GridBase &operator= (GridBase &o)

inline GridBase &operator= (GridBase &&o) noexcept

template<typename T1>
inline void copy (const GridBase<T1> &other)

template<typename T1>
inline void move (GridBase<T1> &&other) noexcept

inline GridBase &wrap (GridBase &o)

inline GridBase &wrap (const GridBase &o)

template<typename T1>
inline GridBase<T> &operator+= (const GridBase<T1> &other)

template<typename T1>
inline GridBase<T> &operator-= (const GridBase<T1> &other)

template<typename T1>
inline GridBase<T> &operator*= (const GridBase<T1> &other)

template<typename T1>
inline GridBase<T> &operator/= (const GridBase<T1> &other)

template<typename DT, typename ST, UInt size>

```

```
GridBase<T> &operator+= (const StaticArray<DT, ST, size> &b)
```

```
template<typename DT, typename ST, UInt size>  
GridBase<T> &operator-= (const StaticArray<DT, ST, size> &b)
```

```
template<typename DT, typename ST, UInt size>  
GridBase<T> &operator*-= (const StaticArray<DT, ST, size> &b)
```

```
template<typename DT, typename ST, UInt size>  
GridBase<T> &operator/= (const StaticArray<DT, ST, size> &b)
```

```
template<typename DT, typename ST, UInt size>  
GridBase<T> &operator= (const StaticArray<DT, ST, size> &b)
```

## Protected Attributes

```
Array<T> data
```

```
UInt nb_components = 1
```

```
template<typename T, UInt dim>
```

```
class GridHermitian : public tamaas::Grid<complex<T>, dim>
```

```
#include <grid_hermitian.hh> Multi-dimensional, multi-component hermitian array.
```

This class represents an array of hermitian data, meaning it has dimensions of:  $n_1 * n_2 * n_3 * \dots * (n_x / 2 + 1)$

However, it acts as a fully dimensioned array, returning a dummy reference for data outside its real dimension, allowing one to write full (and inefficient) loops without really worrying about the reduced dimension.

It would however be better to just use the true dimensions of the surface for all intents and purposes, as it saves computation time.

## Public Types

```
using value_type = complex<T>
```

## Public Functions

```
GridHermitian () = default
```

```
GridHermitian (const GridHermitian &o) = default
```

```
GridHermitian (GridHermitian &&o) noexcept = default
```

```
template<typename ...T1>  
inline complex<T> &operator () (T1... args)
```

```
template<typename ...T1>  
inline const complex<T> &operator () (T1... args) const
```

## Public Static Functions

```
static inline std::array<UInt, dim> hermitianDimensions (std::array<UInt, dim> n)
```

```
template<typename Int, typename = std::enable_if_t<std::is_arithmetic<Int>::value>>
```

```
static inline std::vector<Int> hermitianDimensions (std::vector<Int> n)
```

## Private Functions

```
template<typename ...T1>
```

```
inline void packTuple (UInt *t, UInt i, T1... args) const
```

```
template<typename ...T1>
```

```
inline void packTuple (UInt *t, UInt i) const
```

```
template<template<typename, UInt> class Base, typename T, UInt base_dim, UInt dim>
```

```
class GridView : public Base<T, dim>
```

```
#include <grid_view.hh> View type on grid This is a view on a contiguous chunk of data defined by a grid.
```

## Public Types

```
using iterator = typename Base<T, dim>::iterator
```

```
using const_iterator = typename Base<T, dim>::const_iterator
```

```
using value_type = typename Base<T, dim>::value_type
```

```
using reference = typename Base<T, dim>::reference
```

## Public Functions

```
GridView (GridBase<typename Base<T, dim>::value_type> &grid_base, const std::vector<UInt>
    &multi_index, Int component = -1)
```

Constructor.

```
inline GridView (GridView &&o) noexcept
```

Move constructor.

```
~GridView () override = default
```

Destructor.

```
inline UInt dataSize () const override
```

```
void reserve (UInt size) = delete
```

```
void resize (UInt size) = delete
```

```
inline iterator begin (UInt = 1) override
```

Iterators.

```
inline iterator end (UInt = 1) override  
inline const_iterator begin (UInt = 1) const override  
inline const_iterator end (UInt = 1) const override
```

### Protected Attributes

```
Base<T, base_dim> *grid
```

```
template<typename T>
```

```
struct helper
```

Allocation helper for different float types.

```
template<>
```

```
struct helper<double>
```

```
  #include <interface_impl.hh>
```

### Public Types

```
using complex = fftw_complex
```

```
using plan = fftw_plan
```

### Public Static Functions

```
static inline auto alloc_real (std::size_t size)
```

```
static inline auto alloc_complex (std::size_t size)
```

```
template<>
```

```
struct helper<float>
```

```
  #include <interface_impl.hh>
```

### Public Types

```
using complex = fftwf_complex
```

```
using plan = fftwf_plan
```

## Public Static Functions

```
static inline auto alloc_real (std::size_t size)
static inline auto alloc_complex (std::size_t size)
```

```
template<>
```

```
struct helper<long double>
  #include <interface_impl.hh>
```

## Public Types

```
using complex = fftwl_complex
using plan = fftwl_plan
```

## Public Static Functions

```
static inline auto alloc_real (std::size_t size)
static inline auto alloc_complex (std::size_t size)
```

```
template<model_type type>
```

```
class Hooke : public tamaas::IntegralOperator
  #include <hooke.hh> Applies Hooke's law of elasticity.
  Subclassed by tamaas::HookeField< type >, tamaas::InverseHooke< type >
```

## Public Functions

```
inline virtual model_type getType () const override
  Type of underlying model.
inline virtual IntegralOperator::kind getKind () const override
  Operator is local in real space.
inline virtual void updateFromModel () override
  Does not update.
virtual void apply (GridBase<Real> &strain, GridBase<Real> &stress) const override
  Apply Hooke's tensor.
virtual std::pair<UInt, UInt> matvecShape () const override
  LinearOperator shape.
virtual GridBase<Real> matvec (GridBase<Real> &X) const override
  LinearOperator interface.
inline IntegralOperator (Model *model)
  Constructor.
```

### Public Static Attributes

static constexpr *UInt* **dim** = *model\_type\_traits*<*type*>::dimension

### Protected Functions

*influence*::*ElasticHelper*<*dim*> **elasticHelper** () const

virtual void **applySymTensor** (*GridBase*<*Real*> &strain, *GridBase*<*Real*> &stress) const

virtual void **applyTensor** (*GridBase*<*Real*> &strain, *GridBase*<*Real*> &stress) const

template<*model\_type* **type**>

class **HookeField** : public *tamaas*::*Hooke*<*type*>

*#include* <hooke.hh> Subclassed by *tamaas*::*InverseHookeField*< *type* >

### Public Functions

**HookeField** (*Model* \*model)

virtual void **apply** (*GridBase*<*Real*> &strain, *GridBase*<*Real*> &stress) const override

Apply *Hooke*'s tensor.

### Public Static Attributes

static constexpr *UInt* **dim** = *model\_type\_traits*<*type*>::dimension

### Protected Functions

*std*::vector<*influence*::*ElasticHelper*<*dim*>> **elasticHelperArray** () const

virtual void **applySymTensor** (*GridBase*<*Real*> &strain, *GridBase*<*Real*> &stress) const override

virtual void **applyTensor** (*GridBase*<*Real*> &strain, *GridBase*<*Real*> &stress) const override

class **IntegralOperator** : public *tamaas*::*FieldContainer*

*#include* <integral\_operator.hh> Generic class for integral operators.

Subclassed by *tamaas*::*Westergaard*< *model\_type*::*basic\_2d*, *IntegralOperator*::*neumann* >, *tamaas*::*Hooke*< *type* >, *tamaas*::*VolumePotential*< *type* >, *tamaas*::*Westergaard*< *mtype*, *otype* >, *tamaas*::*detail*::*ComputeOperator*< *Compute\_1* >

## Public Types

enum **kind**

Kind of operator.

*Values:*

enumerator **neumann**

enumerator **dirichlet**

enumerator **dirac**

## Public Functions

inline **IntegralOperator** (*Model* \*model)

Constructor.

virtual void **apply** (*GridBase<Real>* &input, *GridBase<Real>* &output) const = 0

Apply operator on input.

inline virtual void **applyIf** (*GridBase<Real>* &input, *GridBase<Real>* &output, const *std::function<bool(UInt)>* &) const

Apply operator on filtered input.

inline virtual void **updateFromModel** ()

Update any data dependent on model parameters.

inline const *Model* &**getModel** () const

Get model.

inline virtual *kind* **getKind** () const

Kind.

virtual *model\_type* **getType** () const

Type.

inline virtual *Real* **getOperatorNorm** ()

Norm.

inline virtual *std::pair<UInt, UInt>* **matvecShape** () const

Dense shape (for Scipy integration)

inline virtual *GridBase<Real>* **matvec** (*GridBase<Real>* &) const

matvec definition

## Protected Attributes

```
Model *model = nullptr
```

```
template<UInt interpolation_order>
```

```
class Integrator
```

```
    #include <integrator.hh>
```

## Public Static Functions

```
template<bool upper, UInt shape>
```

```
static inline Real G0 (Real q, Real r, Real xc)
```

Standard integral of  $\exp(\pm qy)\phi(y)$  over an element of radius  $r$  and center  $x_c$

```
template<bool upper, UInt shape>
```

```
static inline Real G1 (Real q, Real r, Real xc)
```

Standard integral of  $qy \exp(\pm qy)\phi(y)$  over an element of radius  $r$  and center  $x_c$

```
template<UInt shape>
```

```
static inline constexpr Real F (Real r)
```

Standard integral of  $\phi(y)$  over an element of radius  $r$  and center  $x_c$ . Used for fundamental mode

## Private Types

```
using element = ExponentialElement<interpolation_order>
```

## Private Static Attributes

```
static constexpr std::pair<Real, Real> bounds = {-1, 1}
```

```
template<typename T, UInt dim>
```

```
struct Internal
```

```
    #include <internal.hh>
```

## Public Functions

```
inline void initialize ()
```

Initialize previous field.

```
inline void update ()
```

Update the field previous state.

```
inline void reset ()
```

Reset the current field.

```
inline void operator= (decltype(field) &&field)
```

Assign the field pointer.

```
inline decltype(field) ::element_type & operator* ()
```

Dereference the field pointer.

```
inline const decltype(field) ::element_type & operator* () const
```

Dereference the field pointer (const version)

```
inline operator std::shared_ptr<GridBase<T>> ()
```

Upcast to *GridBase* pointer.

## Public Members

```
std::shared_ptr<Grid<T, dim>> field
```

Stored field.

```
decltype(field) previous
```

```
template<model_type type>
```

```
class InverseHooke : public tamaas::Hooke<type>
```

```
#include <hooke.hh>
```

## Protected Functions

```
virtual void applySymTensor (GridBase<Real> &strain, GridBase<Real> &stress) const override
```

```
virtual void applyTensor (GridBase<Real> &strain, GridBase<Real> &stress) const override
```

```
template<model_type type>
```

```
class InverseHookeField : public tamaas::HookeField<type>
```

```
#include <hooke.hh>
```

## Protected Functions

```
virtual void applySymTensor (GridBase<Real> &stress, GridBase<Real> &strain) const override
```

```
virtual void applyTensor (GridBase<Real> &stress, GridBase<Real> &strain) const override
```

```
template<typename T>
```

```
struct is_arithmetic : public std::is_arithmetic<T>
```

```
#include <static_types.hh>
```

```
template<typename T>
```

```
struct is_arithmetic<complex<T>> : public std::true_type
```

```
#include <static_types.hh>
```

```
template<typename T>
```

```
struct is_policy : public std::false_type
    #include <loop.hh>
template<>
struct is_policy<const thrust::detail::host_t&> : public std::true_type
    #include <loop.hh>
template<>
struct is_policy<const thrust::detail::host_t> : public std::true_type
    #include <loop.hh>
template<>
struct is_policy<thrust::detail::host_t> : public std::true_type
    #include <loop.hh>
template<class Type>
struct is_proxy : public std::false_type
    #include <static_types.hh>
template<typename T, UInt n, UInt m>
struct is_proxy<MatrixProxy<T, n, m>> : public std::true_type
    #include <static_types.hh>
template<typename T, UInt n>
struct is_proxy<SymMatrixProxy<T, n>> : public std::true_type
    #include <static_types.hh>
template<template<typename, typename, UInt...> class StaticParent, typename T, UInt... dims>
struct is_proxy<TensorProxy<StaticParent, T, dims...>> : public std::true_type
    #include <static_types.hh>
template<typename T, UInt n>
struct is_proxy<VectorProxy<T, n>> : public std::true_type
    #include <static_types.hh>
template<typename Container>
struct is_valid_container : public std::is_same<std::remove_cv_t<std::decay_t<Container>::value_type>,
std::remove_cv_t<ValueType>>
    #include <ranges.hh>
template<UInt dim>
class Isopowerlaw : public tamaas::Filter<dim>
    #include <isopowerlaw.hh> Class representing an isotropic power law spectrum.
```

## Public Functions

virtual void **computeFilter** (*GridHermitian*<*Real*, *dim*> &filter\_coefficients) const override

Compute filter coefficients.

inline *Real* **operator** () (const *VectorProxy*<*Real*, *dim*> &q\_vec) const

Compute a point of the PSD.

*Real* **rmsHeights** () const

Analytical rms of heights.

*std::vector*<*Real*> **moments** () const

Analytical moments.

*Real* **alpha** () const

Analytical Nayak's parameter.

*Real* **rmsSlopes** () const

Analytical RMS slopes.

*Real* **radialPSDMoment** (*Real* q) const

Computes  $\int k^q \phi(k) k dk$  from 0 to  $\infty$

*Real* **elasticEnergy** () const

Compute full contact energy (unscaled by  $E^* / L$ )

**TAMAAS\_ACCESSOR** (*q0*, *UInt*, Q0)

**TAMAAS\_ACCESSOR** (*q1*, *UInt*, Q1)

**TAMAAS\_ACCESSOR** (*q2*, *UInt*, Q2)

**TAMAAS\_ACCESSOR** (*hurst*, *Real*, Hurst)

*Real* **radialPSDMoment** (*Real* q) const

*Real* **radialPSDMoment** (*Real*) const

## Protected Attributes

*UInt* **q0**

*UInt* **q1**

*UInt* **q2**

*Real* **hurst**

class **IsotropicHardening** : public *tamaas::Material*

*#include* <isotropic\_hardening.hh>

## Public Functions

**IsotropicHardening** (*Model* \*model, *Real* sigma\_0, *Real* h)

Constructor.

void **computeInelasticDeformationIncrement** (*View* &increment, const *View* &strain, const *View* &strain\_increment)

Compute plastic strain increment with radial return algorithm.

virtual void **computeStress** (*Field* &stress, const *Field* &strain, const *Field* &strain\_increment) override

Compute stress.

virtual void **computeEigenStress** (*Field* &stress, const *Field* &strain, const *Field* &strain\_increment) override

Compute stress due to plastic strain increment:  $\tau = \mathbb{C} : \Delta \epsilon^P$

virtual void **update** () override

Update internal variables.

virtual void **applyTangent** (*Field* &output, const *Field* &input, const *Field* &strain, const *Field* &strain\_increment) override

Applt consistent tangent.

inline *Real* **getHardeningModulus** () const

inline *Real* **getYieldStress** () const

inline const *GridBase*<*Real*> &**getPlasticStrain** () const

inline *GridBase*<*Real*> &**getPlasticStrain** ()

inline void **setHardeningModulus** (*Real* h\_)

inline void **setYieldStress** (*Real* sigma\_0\_)

## Public Static Functions

static inline *Real* **hardening** (*Real* p, *Real* h, *Real* sigma\_0)

Linear hardening function.

## Protected Attributes

*Real* **sigma\_0**

*Real* **h**

< initial yield stress

*Internal*<*Real*, *dim*> **plastic\_strain**

< hardening modulus

*Internal*<*Real*, *dim*> **cumulated\_plastic\_strain**

## Private Types

```
using parent = Material

using trait = model_type_traits<type>

using Field = typename parent::Field

using Mat = SymMatrixProxy<Real, dim>

using CMat = SymMatrixProxy<const Real, dim>

using View = Grid<Real, dim>
```

## Private Static Attributes

```
static constexpr auto type = model_type::volume_2d

static constexpr UInt dim = trait::dimension

template<direction dir>

struct iterator
    #include <accumulator.hh> Forward/Backward iterator for integration passes.
```

## Public Types

```
using integ = Integrator<1>
```

## Public Functions

```
inline iterator (Accumulator &acc, Int k)
    Constructor.

inline iterator (const iterator &o)
    Copy constructor.

inline bool operator!= (const iterator &o) const
    Compare.

inline iterator &operator++ ()
    Increment.

inline std::tuple<Int, Real, BufferType&, BufferType&> operator* ()
    Dereference iterator (TODO uniformize tuple types)
```

## Public Static Attributes

static constexpr bool **upper** = *dir* == direction::backward

## Protected Functions

inline bool **setup** ()

Update index layer and element info.

inline void **next** ()

Set current layer and update element index.

## Protected Attributes

Accumulator &**acc**

*Int* **k** = 0

accumulator holder

element index

*Int* **l** = 0

layer index

*Real* **r** = 0

element radius

*Real* **xc** = 0

element center

## Protected Static Functions

static inline *Int* **layer** (*Int* element)

Element index => layer index.

static inline *Int* **nextElement** (*Int* element)

Next element index in right direction.

template<typename **T**>

class **iterator**

*#include* <iterator.hh> Subclassed by *tamaas::iterator\_::iterator\_view*< *T* >

## Public Types

using **value\_type** = *T*

using **difference\_type** = *std::ptrdiff\_t*

using **pointer** = *T\**

using **reference** = *T&*

using **iterator\_category** = *thrust::random\_access\_device\_iterator\_tag*

## Public Functions

inline **iterator** (*pointer* data, *difference\_type* step\_size)  
    constructor

inline **iterator** (const *iterator* &o)  
    copy constructor

inline **iterator** (*iterator* &&o) noexcept  
    move constructor

template<typename **U**, typename = *std::enable\_if\_t<std::is\_convertible<T, U>::value>>*  
inline **iterator** (const *iterator*<*U*> &o)  
    copy from a different qualified type

template<typename **U**, typename = *std::enable\_if\_t<std::is\_convertible<T, U>::value>>*  
inline **iterator** (*iterator*<*U*> &&o)  
    move from a different qualified type

inline *iterator* &**operator**= (const *iterator* &o)

inline *iterator* &**operator**= (*iterator* &&o) noexcept

inline *reference* **operator\*** ()  
    dereference iterator

inline *reference* **operator\*** () const  
    dereference iterator

inline *iterator* &**operator**+= (*difference\_type* a)  
    increment with given offset

inline *iterator* &**operator**++ ()  
    increment iterator

inline bool **operator**< (const *iterator* &a) const  
    comparison

inline bool **operator**!= (const *iterator* &a) const  
    inequality

```
inline bool operator== (const iterator &a) const
    equality
inline difference_type operator- (const iterator &a) const
    needed for OpenMP range calculations
inline void setStep (difference_type s)
```

## Protected Attributes

*T* \***data**

*difference\_type* **step**

## Friends

**friend class** iterator

```
class iterator : public tamaas::iterator_::iterator<ValueType>
    #include <ranges.hh>
```

## Public Types

using **value\_type** = LocalType

using **reference** = *value\_type*

## Public Functions

```
inline iterator (const parent &o)
```

```
inline reference operator* ()
```

```
inline reference operator* () const
```

## Private Types

using **parent** = *iterator\_::iterator*<ValueType>

```
template<typename T>
```

```
class iterator_view : private tamaas::iterator_::iterator<T>
    #include <iterator.hh>
```

## Public Types

```
using value_type = T
```

```
using difference_type = std::ptrdiff_t
```

```
using pointer = T*
```

```
using reference = T&
```

## Public Functions

```
inline iterator_view (pointer data, std::size_t start, ptrdiff_t offset, std::vector<UInt> strides,  
                    std::vector<UInt> sizes)
```

Constructor.

```
inline iterator_view (const iterator_view &o)
```

```
inline iterator_view &operator= (const iterator_view &o)
```

## Protected Functions

```
inline void computeAccessOffset ()
```

## Protected Attributes

```
std::vector<UInt> strides
```

```
std::vector<UInt> n
```

```
std::vector<UInt> tuple
```

```
class Kato : public tamaas::ContactSolver
```

```
    #include <kato.hh> Subclassed by tamaas::BeckTeboulle, tamaas::Condat, tamaas::PolonskyKeerTan
```

## Public Functions

```
Kato (Model &model, const GridBase<Real> &surface, Real tolerance, Real mu)
```

Constructor.

```
virtual Real solve (std::vector<Real> p0) override
```

Solve.

```
Real solveRelaxed (GridBase<Real> &g0)
```

Solve relaxed problem.

*Real* **solveRegularized** (*GridBase*<*Real*> &p0, *Real* r)

Solve regularized problem.

*Real* **computeCost** (bool use\_tresca = false)

Compute cost function.

Compute mean of the field taking each component separately.

template<*model\_type* **type**>

*Real* **solveTmp1** (*GridBase*<*Real*> &p0, *UInt* proj\_iter)

Template for solve function.

template<*model\_type* **type**>

*Real* **solveRelaxedTmp1** (*GridBase*<*Real*> &g0)

Template for solveRelaxed function.

template<*model\_type* **type**>

*Real* **solveRegularizedTmp1** (*GridBase*<*Real*> &p0, *Real* r)

Template for solveRegularized function.

template<*model\_type* **type**>

void **initSurfaceWithComponents** ()

Creates surfaceComp form surface.

template<*UInt* **comp**>

void **computeGradient** (bool use\_tresca = false)

Compute gradient of functional.

template<*UInt* **comp**>

void **enforcePressureConstraints** (*GridBase*<*Real*> &p0, *UInt* proj\_iter)

Project pressure on friction cone.

Projects  $\vec{p}$  on  $\mathcal{C}$  and  $\mathcal{D}$ . Projects  $\vec{p}$  on  $\mathcal{C}$  and  $\mathcal{D}$ .

template<*UInt* **comp**>

void **enforcePressureMean** (*GridBase*<*Real*> &p0)

Project on C.

template<*UInt* **comp**>

void **enforcePressureCoulomb** ()

Project on D.

template<*UInt* **comp**>

void **enforcePressureTresca** ()

Project on D (Tresca)

template<*UInt* **comp**>

*Vector*<*Real*, *comp*> **computeMean** (*GridBase*<*Real*> &field)

Compute mean value of field.

Compute mean of the field taking each component separately.

template<*UInt* **comp**>

void **addUniform** (*GridBase*<*Real*> &field, *GridBase*<*Real*> &vec)

Add vector to each point of field.

template<*model\_type* **type**>

```
void computeValuesForCost (GridBase<Real> &lambda, GridBase<Real> &eta, GridBase<Real> &p_N,
                          GridBase<Real> &p_C)
```

Compute grids of dual and primal variables.

```
template<model_type type>
void computeValuesForCostTresca (GridBase<Real> &lambda, GridBase<Real> &eta,
                                GridBase<Real> &p_N, GridBase<Real> &p_C)
```

Compute dual and primal variables with Tresca friction.

```
template<UInt comp>
void computeFinalGap ()
```

Compute total displacement.

```
inline void setProjectionIterations (UInt niter)
```

## Public Static Functions

```
static Real regularize (Real x, Real r)
```

Regularization function with factor r (0 -> unregularized)

## Protected Attributes

```
BEngine &engine
```

```
GridBase<Real> *gap = nullptr
```

```
GridBase<Real> *pressure = nullptr
```

```
std::unique_ptr<GridBase<Real>> surfaceComp = nullptr
```

```
Real mu = 0
```

```
UInt N = 0
```

```
UInt proj_iter = 50
```

```
class KatoSaturated : public tamaas::PolonskyKeerRey
```

```
    #include <kato_saturated.hh> Polonsky-Keer algorithm with saturation of the pressure.
```

## Public Functions

**KatoSaturated** (*Model* &model, const *GridBase*<*Real*> &surface, *Real* tolerance, *Real* pmax)

Constructor.

**~KatoSaturated** () override = default

virtual *Real* **solve** (*std::vector*<*Real*> load) override

Solve.

virtual *Real* **meanOnUnsaturated** (const *GridBase*<*Real*> &field) const override

Mean on unsaturated constraint zone.

virtual *Real* **computeSquaredNorm** (const *GridBase*<*Real*> &field) const override

Compute squared norm.

virtual void **updateSearchDirection** (*Real* factor) override

Update search direction.

virtual *Real* **computeCriticalStep** (*Real* target = 0) override

Compute critical step.

virtual bool **updatePrimal** (*Real* step) override

Update primal and check non-admissible state.

virtual *Real* **computeError** () const override

Compute error/stopping criterion.

virtual void **enforceMeanValue** (*Real* mean) override

Enforce mean value constraint.

virtual void **enforceAdmissibleState** () override

Enforce contact constraints on final state.

inline *Real* **getPMax** () const

Access to pmax.

inline void **setPMax** (*Real* p)

Set pax.

## Protected Attributes

*Real* **pmax** = *std::numeric\_limits*<*Real*>::max()

saturation pressure

template<*UInt* dim, *UInt* derivative\_order>

class **Kelvin**

Class for the *Kelvin* tensor.

template<*model\_type* type, *UInt* derivative>

class **Kelvin** : public *tamaas::VolumePotential*<type>

*#include* <kelvin.hh> *Kelvin* tensor.

Subclassed by *tamaas::Mindlin*<type, derivative >

## Public Functions

**Kelvin** (*Model* \*model)

Constructor.

void **applyIf** (*GridBase*<*Real*> &source, *GridBase*<*Real*> &out, *filter\_t* pred) const override

Apply the Kelvin-tensor\_order operator.

void **setIntegrationMethod** (*integration\_method* method, *Real* cutoff)

Set the integration method for volume operator.

virtual *std*::pair<*UInt*, *UInt*> **matvecShape** () const override

Dense shape (for Scipy integration)

virtual *GridBase*<*Real*> **matvec** (*GridBase*<*Real*> &X) const override

matvec definition

## Protected Types

using **KelvinInfluence** = *influence*::*Kelvin*<*trait*::dimension, *derivative*>

using **ktrait** = *detail*::*KelvinTrait*<*KelvinInfluence*>

using **Source** = typename *ktrait*::source\_t

using **Out** = typename *ktrait*::out\_t

using **filter\_t** = typename *parent*::filter\_t

## Protected Attributes

*integration\_method* **method** = *integration\_method*::*linear*

*Real* **cutoff**

## Private Types

using **trait** = *model\_type\_traits*<*type*>

using **dtrait** = *derivative\_traits*<*derivative*>

using **parent** = *VolumePotential*<*type*>

### Private Functions

void **linearIntegral** (*GridBase*<*Real*> &out, *KelvinInfluence* &kelvin) const

void **cutoffIntegral** (*GridBase*<*Real*> &out, *KelvinInfluence* &kelvin) const

template<>

class **Kelvin**<3, 0>

*#include* <influence.hh> *Kelvin* base tensor See arXiv:1811.11558 for details.

Subclassed by *tamaas::influence::Kelvin*<3, 1 >

### Public Functions

inline **Kelvin** (*Real* mu, *Real* nu)

template<bool **upper**, bool **apply\_q\_power** = false, typename **ST**>

inline *Vector*<*Complex*, *dim*> **applyU0** (const *VectorProxy*<const *Real*, *dim* - 1> &q, const *StaticVector*<*Complex*, *ST*, *dim*> &f) const

template<bool **upper**, bool **apply\_q\_power** = false, typename **ST**>

inline *Vector*<*Complex*, *dim*> **applyU1** (const *VectorProxy*<const *Real*, *dim* - 1> &q, const *StaticVector*<*Complex*, *ST*, *dim*> &f) const

### Protected Attributes

const *Real* **mu**

const *Real* **b**

### Protected Static Attributes

static constexpr *UInt* **dim** = 3

static constexpr *UInt* **order** = 0

template<>

class **Kelvin**<3, 1> : protected *tamaas::influence::Kelvin*<3, 0>

*#include* <influence.hh> *Kelvin* first derivative.

Subclassed by *tamaas::influence::Kelvin*<3, 2 >

## Public Functions

```
template<bool upper, bool apply_q_power = false, typename ST>
inline Vector<Complex, dim> applyU0 (const VectorProxy<const Real, dim - 1> &q, const
    StaticMatrix<Complex, ST, dim, dim> &f) const
```

```
template<bool upper, bool apply_q_power = false, typename ST>
inline Vector<Complex, dim> applyU1 (const VectorProxy<const Real, dim - 1> &q, const
    StaticMatrix<Complex, ST, dim, dim> &f) const
```

## Protected Static Attributes

```
static constexpr UInt dim = parent::dim
```

```
static constexpr UInt order = parent::order + 1
```

## Private Types

```
using parent = Kelvin<3, 0>
```

```
template<>
```

```
class Kelvin<3, 2> : protected tamaas::influence::Kelvin<3, 1>
    #include <influence.hh> Kelvin second derivative.
```

## Public Functions

```
template<bool upper, bool apply_q_power = false, typename ST>
inline Matrix<Complex, dim, dim> applyU0 (const VectorProxy<const Real, dim - 1> &q, const
    StaticMatrix<Complex, ST, dim, dim> &f) const
```

```
template<bool upper, bool apply_q_power = false, typename ST>
inline Matrix<Complex, dim, dim> applyU1 (const VectorProxy<const Real, dim - 1> &q, const
    StaticMatrix<Complex, ST, dim, dim> &f) const
```

```
template<typename ST>
inline Matrix<Complex, dim, dim> applyDiscontinuityTerm (const StaticMatrix<Complex, ST, dim,
    dim> &f) const
```

## Private Types

```
using parent = Kelvin<3, 1>
```

## Private Static Attributes

```
static constexpr UInt dim = parent::dim
```

```
static constexpr UInt order = parent::order + 1
```

```
template<model_type type, typename kelvin_t, typename = typename KelvinTrait<kelvin_t::source_t>
```

```
struct KelvinHelper
```

```
    #include <kelvin_helper.hh> Helper to apply integral representation on output.
```

## Public Types

```
using trait = model_type_traits<type>
```

```
using BufferType = GridHermitian<Real, bdim>
```

```
using source_t = typename KelvinTrait<kelvin_t::source_t
```

```
using out_t = typename KelvinTrait<kelvin_t::out_t
```

## Public Functions

```
virtual ~KelvinHelper () = default
```

```
inline void applyIntegral (std::vector<BufferType> &source, std::vector<BufferType> &out, const  
    Grid<Real, bdim> &wavevectors, Real domain_size, const kelvin_t &kelvin)
```

*Apply* the regular part of *Kelvin* to source and sum into output.

This function performs the linear integration algorithm using the accumulator.

```
inline void applyIntegral (std::vector<BufferType> &source, BufferType &out, UInt layer, const Grid<Real,  
    bdim> &wavevectors, Real domain_size, Real cutoff, const kelvin_t &kelvin)
```

*Apply* the regular part of *Kelvin* to source and sum into output.

This function performs the cutoff integration algorithm. Not to be confused with its overload above.

```
inline void applyFreeTerm (std::vector<BufferType> &source, std::vector<BufferType> &out, const kelvin_t  
    &kelvin)
```

*Apply* free term of distribution derivative.

```
inline void applyFreeTerm (BufferType&, BufferType&, const kelvin_t&)
```

*Apply* free term of distribution derivative (layer)

```
inline void makeFundamentalGreatAgain (std::vector<BufferType> &out)
```

Making the output free of communist NaN.

```
inline void makeFundamentalGreatAgain (BufferType&)
```

Making the output free of communist NaN (layer)

```
inline void applyFreeTerm (BufferType &source, BufferType &out, const influence::Kelvin<3, 2> &kelvin)
```

Applying free term for double gradient of *Kelvin*.

## Public Static Attributes

```
static constexpr UInt dim = trait::dimension
```

```
static constexpr UInt bdim = trait::boundary_dimension
```

## Protected Attributes

```
Accumulator<type, source_t> accumulator
```

```
template<typename T>
```

```
struct KelvinTrait
```

Trait for kelvin local types.

```
template<UInt dim>
```

```
struct KelvinTrait<influence::Boussinesq<dim, 0>>
```

```
  #include <kelvin_helper.hh>
```

## Public Types

```
using source_t = VectorProxy<Complex, dim>
```

```
using out_t = VectorProxy<Complex, dim>
```

```
template<UInt dim>
```

```
struct KelvinTrait<influence::Boussinesq<dim, 1>>
```

```
  #include <kelvin_helper.hh>
```

## Public Types

```
using source_t = VectorProxy<Complex, dim>
```

```
using out_t = SymMatrixProxy<Complex, dim>
```

```
template<UInt dim>
```

```
struct KelvinTrait<influence::Kelvin<dim, 0>>
```

```
  #include <kelvin_helper.hh>
```

## Public Types

```
using source_t = VectorProxy<Complex, dim>

using out_t = VectorProxy<Complex, dim>

template<UInt dim>
struct KelvinTrait<influence::Kelvin<dim, 1>>
    #include <kelvin_helper.hh>
```

## Public Types

```
using source_t = SymMatrixProxy<Complex, dim>

using out_t = VectorProxy<Complex, dim>

template<UInt dim>
struct KelvinTrait<influence::Kelvin<dim, 2>>
    #include <kelvin_helper.hh>
```

## Public Types

```
using source_t = SymMatrixProxy<Complex, dim>

using out_t = SymMatrixProxy<Complex, dim>

class LinearElastic : public tamaas::Material
    #include <linear_elastic.hh>
```

## Public Functions

```
LinearElastic (Model *model, std::string operator_name)

virtual void computeStress (Field &stress, const Field &strain, const Field &strain_increment) override
    Compute the stress from total strain and strain increment.

virtual void computeEigenStress (Field &stress, const Field &strain, const Field &strain_increment)
    override
    Compute stress due to inelastic increment.

virtual void applyTangent (Field &output, const Field &input, const Field &strain, const Field
    &strain_increment) override
    Applt consistent tangent.

virtual void update () override
    Update internal variables.
```

## Protected Attributes

```
std::string operator_name
```

## Private Types

```
using parent = Material
```

```
using Field = parent::Field
```

```
using trait = model_type_traits<model_type::volume_2d>
```

## Private Static Attributes

```
static constexpr UInt dim = trait::dimension
```

```
static constexpr UInt comp = trait::voigt
```

```
class Logger
```

```
#include <logger.hh> Logging class Inspired from https://www.drdobbs.com/cpp/logging-in-c/201804215 by  
Petru Marginean.
```

## Public Functions

```
~Logger () noexcept
```

```
    Writing to stderr.
```

```
std::ostream &get (LogLevel level = LogLevel::debug)
```

```
    Get stream.
```

```
inline decltype(auto) getWishLevel () const
```

```
    Get wish log level.
```

## Public Static Functions

```
static inline decltype(auto) getCurrentLevel ()
```

```
    Get current log level.
```

```
static void setLevel (LogLevel level)
```

```
    Set acceptable logging level.
```

## Private Members

```
std::ostream stream
```

```
LogLevel wish_level = LogLevel::debug
```

## Private Static Attributes

```
static LogLevel current_level = LogLevel::info
```

## class **Loop**

*#include* <loop.hh> Singleton class for automated loops using lambdas.

This class is sweet candy :) It provides abstraction of the parallelism paradigm used in loops and allows simple and less error-prone loop syntax, with minimum boiler plate. I love it <3

## Public Functions

**Loop** () = delete  
Constructor.

## Public Static Functions

```
template<typename T>  
static inline arange<T> range (T size)
```

```
template<typename T, typename U>  
static inline arange<T> range (U start, T size)
```

```
template<typename Functor, typename ...Ranges>  
static inline auto loop (Functor &&func, Ranges&&... ranges) -> typename std::enable_if<not  
    is_policy<Functor>::value, void>::type
```

*Loop* functor over ranges.

```
template<typename DerivedPolicy, typename Functor, typename ...Ranges>  
static inline void loop (const thrust::execution_policy<DerivedPolicy> &policy, Functor &&func, Ranges&&...  
    ranges)
```

*Loop* over ranges with non-default policy.

```
template<operation op = operation::plus, typename Functor, typename ...Ranges>  
static inline auto reduce (Functor &&func, Ranges&&... ranges) -> typename std::enable_if<not  
    is_policy<Functor>::value,  
    decltype(func(std::declval<reference_type<Ranges>>()...))>::type
```

Reduce functor over ranges.

```
template<operation op = operation::plus, typename DerivedPolicy, typename Functor, typename  
...Ranges>  
static inline auto reduce (const thrust::execution_policy<DerivedPolicy> &policy, Functor &&func,  
    Ranges&&... ranges) -> decltype(func(std::declval<reference_type<Ranges>>()...))
```

Reduce over ranges with non-default policy.

## Private Types

```
template<typename T>
using reference_type = typename std::decay<T>::type::reference
```

## Private Static Functions

```
template<typename DerivedPolicy, typename Functor, typename ...Ranges>
static void loopImpl (const thrust::execution_policy<DerivedPolicy> &policy, Functor &&func, Ranges&&...
                    ranges)
```

*Loop* over ranges and apply functor.

```
template<operation op, typename DerivedPolicy, typename Functor, typename ...Ranges>
static auto reduceImpl (const thrust::execution_policy<DerivedPolicy> &policy, Functor &&func,
                        Ranges&&... ranges) -> decltype(func(std::declval<reference_type<Ranges>>()...))
```

*Loop* over ranges, apply functor and reduce result.

class **Material**

*#include* <material.hh> Subclassed by *tamaas::IsotropicHardening*, *tamaas::LinearElastic*

## Public Functions

```
inline Material (Model *model)
```

Constructor.

```
virtual ~Material () = default
```

Destructor.

```
virtual void computeStress (Field &stress, const Field &strain, const Field &strain_increment) = 0
```

Compute the stress from total strain and strain increment.

```
virtual void computeEigenStress (Field &stress, const Field &strain, const Field &strain_increment) = 0
```

Compute stress due to inelastic increment.

```
virtual void update () = 0
```

Update internal variables.

```
inline virtual void applyTangent (Field&, const Field&, const Field&, const Field&)
```

Appl consistent tangent.

## Protected Types

```
using Field = GridBase<Real>
```

## Protected Attributes

*Model* \*model

class **MaugisAdhesionFunctional** : public *tamaas::functional::AdhesionFunctional*  
*#include* <adhesion\_functional.hh> Constant adhesion functional.

## Public Functions

inline **MaugisAdhesionFunctional** (const *GridBase<Real>* &surface)

Explicit declaration of constructor for swig.

virtual *Real* **computeF** (*GridBase<Real>* &gap, *GridBase<Real>* &pressure) const override

Compute the total adhesion energy.

virtual void **computeGradF** (*GridBase<Real>* &gap, *GridBase<Real>* &gradient) const override

Compute the gradient of the adhesion functional.

class **MaxwellViscoelastic** : public *tamaas::PolonskyKeerRey*

*#include* <maxwell\_viscoelastic.hh> Viscoelastic, pressure-based normal contact solver, based on a generalized Maxwell model.

## Public Functions

**MaxwellViscoelastic** (*Model* &model, const *GridBase<Real>* &surface, *Real* tolerance, *Real* time\_step,  
*std::vector<Real>* shear\_moduli\_maxwell, *std::vector<Real>*  
characteristic\_times)

Constructor.

**~MaxwellViscoelastic** () override = default

virtual *Real* **solve** (*std::vector<Real>* target) override

Main solve function with backward euler scheme.

void **reset** ()

Reset function, reset the global displacement and the partial displacement.

virtual void **updateState** () override

Update internal variables.

**TAMAAS\_ACCESSOR** (*time\_step\_*, *Real*, TimeStep)

## Public Members

bool **solve\_should\_update** = true  
update at the end of a solve step

## Protected Attributes

*Real* **time\_step\_**

*std::vector<Real>* **shear\_moduli\_**  
list of shear moduli

*std::vector<Real>* **characteristic\_times\_**  
list of characteristic relaxation times

*std::vector<GridBase<Real>>* **M**  
partial displacements

*GridBase<Real>* **U**

*GridBase<Real>* **U\_new**  
global viscoelastic displacement

## Private Functions

*Real* **computeGtilde** (const *std::vector<Real>* &shear\_moduli, const *std::vector<Real>* &gamma) const  
Compute the effective shear moduli for maxwell branches.

*std::vector<Real>* **computeGamma** (const *Real* &time\_step, const *std::vector<Real>* &characteristic\_times)  
const  
Compute the partial displacement coefficient for each maxwell branch to update surface

class **MetaFunctional** : public *tamaas::functional::Functional*  
*#include <meta\_functional.hh>* Meta functional that contains list of functionals.

## Public Functions

virtual *Real* **computeF** (*GridBase<Real>* &variable, *GridBase<Real>* &dual) const override  
Compute functional.

virtual void **computeGradF** (*GridBase<Real>* &variable, *GridBase<Real>* &gradient) const override  
Compute functional gradient.

void **addFunctionalTerm** (*std::shared\_ptr<Functional>* functional)  
Add functional to the list.

void **clear** ()  
Clears the functional list.

## Protected Attributes

*FunctionalList* **functionals**

## Private Types

```
using FunctionalList = std::list<std::shared_ptr<Functional>>
```

```
template<model_type type, U derivative>
```

```
class Mindlin : public tamaas::Kelvin<type, derivative>  
    #include <mindlin.hh> Mindlin tensor.
```

## Public Functions

```
Mindlin (Model *model)
```

Constructor.

```
void applyIf (GridBase<Real> &source, GridBase<Real> &out, filter_t pred) const override
```

Apply the Mindlin-tensor\_order operator.

## Protected Functions

```
void linearIntegral (GridBase<Real> &out) const
```

```
void cutoffIntegral (GridBase<Real> &out) const
```

## Protected Attributes

```
mutable GridHermitian<Real, trait::boundary_dimension> surface_tractions
```

## Private Types

```
using trait = model_type_traits<type>
```

```
using parent = Kelvin<type, derivative>
```

```
using filter_t = typename parent::filter_t
```

```
class Model : public tamaas::FieldContainer
```

*#include* <model.hh> *Model* containing pressure and displacement This class is a container for the model fields. It is supposed to be dimension agnostic, hence the *GridBase* members.

Subclassed by *tamaas::ModelTemplate< type >*

## Public Functions

```

void setElasticity (Real E, Real nu)
    Set elasticity parameters.

inline Real getHertzModulus () const
    Get Hertz contact modulus.

inline Real getYoungModulus () const
    Get Young's modulus.

inline Real getPoissonRatio () const
    Get Poisson's ratio.

inline Real getShearModulus () const
    Get shear modulus.

inline void setYoungModulus (Real E_)
    Set Young's modulus.

inline void setPoissonRatio (Real nu_)
    Set Poisson's ratio.

virtual model_type getType () const = 0
    Get model type.

const std::vector<Real> &getSystemSize () const
    Get system physical size.

virtual std::vector<Real> getBoundarySystemSize () const = 0
    Get boundary system physical size.

const std::vector<UInt> &getDiscretization () const
    Get discretization.

virtual std::vector<UInt> getGlobalDiscretization () const = 0
    Get discretization of global MPI system.

virtual std::vector<UInt> getBoundaryDiscretization () const = 0
    Get boundary discretization.

inline BEEngine &getBEEngine ()
    Get boundary element engine.

void applyElasticity (GridBase<Real> &stress, const GridBase<Real> &strain) const
    Apply Hooke's law.

void applyInverseElasticity (GridBase<Real> &strain, const GridBase<Real> &stress) const
    Apply inverse Hooke's law.

void solveNeumann ()
    Solve Neumann problem using default neumann operator.

void solveDirichlet ()
    Solve Dirichlet problem using default dirichlet operator.

template<typename Operator>

```

*std::shared\_ptr<IntegralOperator>* **registerIntegralOperator** (const *std::string* &name)  
Register a new integral operator.

void **registerIntegralOperator** (const *std::string* &name, *std::shared\_ptr<IntegralOperator>* op)  
Register external operator.

*std::shared\_ptr<IntegralOperator>* **getIntegralOperator** (const *std::string* &name) const  
Get a registered integral operator.

*std::vector<std::string>* **getIntegralOperators** () const  
Get list of integral operators.

inline const auto &**getIntegralOperatorsMap** () const  
Get operators mapcar.

void **updateOperators** ()  
Tell operators to update their cache.

virtual void **setIntegrationMethod** (*integration\_method* method, *Real* cutoff) = 0  
Set integration method for registered volume operators.

*GridBase<Real>* &**getTraction** ()  
Get pressure.

const *GridBase<Real>* &**getTraction** () const  
Get pressure.

*GridBase<Real>* &**getDisplacement** ()  
Get displacement.

const *GridBase<Real>* &**getDisplacement** () const  
Get displacement.

template<class T>  
inline bool **isBoundaryField** (const *GridBase<T>* &field) const  
Determine if a field is defined on boundary.

*std::vector<std::string>* **getBoundaryFields** () const  
Return list of fields defined on boundary.

void **addDumper** (*std::shared\_ptr<ModelDumper>* dumper)  
Set the dumper object.

void **dump** () const  
Dump the model.

## Protected Functions

inline **Model** (*std::vector<Real>* system\_size, *std::vector<UInt>* discretization)  
Constructor.

## Protected Attributes

*Real* **E** = 1

*Real* **nu** = 0

*std::vector<Real>* **system\_size**

*std::vector<UInt>* **discretization**

*std::unique\_ptr<BEEngine>* **engine** = nullptr

*std::unordered\_map<std::string, std::shared\_ptr<IntegralOperator>>* **operators**

*std::vector<std::shared\_ptr<ModelDumper>>* **dumpers**

## Friends

friend *std::ostream* &**operator**<< (*std::ostream* &o, const *Model* &\_this)

```
class model_type_error : public std::domain_error
```

```
    #include <errors.hh>
```

```
template<model_type type>
```

```
struct model_type_traits
```

```
    #include <model_type.hh> Trait class to store physical dimension of domain, of boundary and number of components
```

```
template<>
```

```
struct model_type_traits<model_type::basic_1d>
```

```
    #include <model_type.hh>
```

## Public Static Attributes

```
static constexpr char repr[] = {"basic_1d"}
```

```
static constexpr UInt dimension = 1
```

```
static constexpr UInt components = 1
```

```
static constexpr UInt boundary_dimension = 1
```

```
static constexpr UInt voigt = voigt_size<1>::value
```

```
static const std::vector<UInt> indices = {}
```

```
template<>
```

```
struct model_type_traits<model_type::basic_2d>  
    #include <model_type.hh>
```

### Public Static Attributes

```
static constexpr char repr[] = {"basic_2d"}
```

```
static constexpr UInt dimension = 2
```

```
static constexpr UInt components = 1
```

```
static constexpr UInt boundary_dimension = 2
```

```
static constexpr UInt voigt = voigt_size<1>::value
```

```
static const std::vector<UInt> indices = {}
```

```
template<>
```

```
struct model_type_traits<model_type::surface_1d>  
    #include <model_type.hh>
```

### Public Static Attributes

```
static constexpr char repr[] = {"surface_1d"}
```

```
static constexpr UInt dimension = 1
```

```
static constexpr UInt components = 2
```

```
static constexpr UInt boundary_dimension = 1
```

```
static constexpr UInt voigt = voigt_size<2>::value
```

```
static const std::vector<UInt> indices = {}
```

```
template<>
```

```
struct model_type_traits<model_type::surface_2d>  
    #include <model_type.hh>
```

### Public Static Attributes

```
static constexpr char repr[] = {"surface_2d"}
```

```
static constexpr UInt dimension = 2
```

```
static constexpr UInt components = 3
```

```
static constexpr UInt boundary_dimension = 2
```

```
static constexpr UInt voigt = voigt_size<3>::value
```

```
static const std::vector<UInt> indices = {}
```

```
template<>
```

```
struct model_type_traits<model_type::volume_1d>
  #include <model_type.hh>
```

### Public Static Attributes

```
static constexpr char repr[] = {"volume_1d"}
```

```
static constexpr UInt dimension = 2
```

```
static constexpr UInt components = 2
```

```
static constexpr UInt boundary_dimension = 1
```

```
static constexpr UInt voigt = voigt_size<2>::value
```

```
static const std::vector<UInt> indices = {0}
```

```
template<>
```

```
struct model_type_traits<model_type::volume_2d>
  #include <model_type.hh>
```

### Public Static Attributes

```
static constexpr char repr[] = {"volume_2d"}
```

```
static constexpr UInt dimension = 3
```

```
static constexpr UInt components = 3
```

```
static constexpr UInt boundary_dimension = 2
```

```
static constexpr UInt voigt = voigt_size<3>::value
```

```
static const std::vector<UInt> indices = {0}
```

```
class ModelDumper
```

```
  #include <model_dumper.hh>
```

### Public Functions

```
virtual ~ModelDumper () = default
```

```
virtual void dump (const Model &model) = 0
```

```
class ModelFactory
```

```
  #include <model_factory.hh> Factory class for model.
```

### Public Static Functions

```
static std::unique_ptr<Model> createModel (model_type type, const std::vector<Real> &system_size, const  
                                         std::vector<UInt> &discretization)
```

Create new model.

```
static std::unique_ptr<Model> createModel (const Model &model)
```

Make a deep copy of existing model.

```
static std::unique_ptr<Residual> createResidual (Model &model, Real sigma_y, Real hardening)
```

Create a plasticity residual.

```
static void registerVolumeOperators (Model &m)
```

Register volume integral operators in a model.

```
static void registerNonPeriodic (Model &m, std::string name)
```

```
static void setIntegrationMethod (IntegralOperator &op, integration_method method, Real cutoff)
```

Set integration method for a volume integral operator.

```
template<model_type type>
```

class **ModelTemplate** : public *tamaas::Model*

*#include <model\_template.hh>* *Model* class templated with model type Specializations of this class should take care of dimension specific code.

### Public Functions

**ModelTemplate** (*std::vector<Real>* system\_size, *std::vector<UInt>* discretization)

Constructor.

inline virtual *model\_type* **getType** () const override

Get model type.

virtual *std::vector<UInt>* **getGlobalDiscretization** () const override

Get discretization of global MPI system.

virtual *std::vector<UInt>* **getBoundaryDiscretization** () const override

Get boundary discretization.

virtual *std::vector<Real>* **getBoundarySystemSize** () const override

Get boundary system physical size.

virtual void **setIntegrationMethod** (*integration\_method* method, *Real* cutoff) override

Set integration method for registered volume operators.

### Protected Functions

void **initializeBEEngine** ()

### Protected Attributes

*std::unique\_ptr<ViewType>* **displacement\_view** = nullptr

*std::unique\_ptr<ViewType>* **traction\_view** = nullptr

### Private Types

using **trait** = *model\_type\_traits<type>*

using **ViewType** = *GridView<Grid, Real, dim, trait::boundary\_dimension>*

### Private Static Attributes

```
static constexpr UInt dim = trait::dimension
```

```
struct MPI_Comm
```

```
    #include <mpi_interface.hh>
```

```
class nan_error : public std::runtime_error
```

```
    #include <errors.hh>
```

```
struct no_convergence_error : public std::runtime_error
```

```
    #include <errors.hh>
```

### Public Functions

```
inline no_convergence_error (const std::string &what, double error, double tolerance)
```

```
inline const char *what () const noexcept override
```

### Public Members

```
std::string what_member
```

```
class NonlinearSolver : public tamaas::EPSolver
```

```
    #include <snesc.hh> Wrapper to PETSc SNES abstract solver.
```

### Public Types

```
using residual_ctx = std::pair<Residual*, GridBase<Real>*>
```

### Public Functions

```
NonlinearSolver (Residual &residual, std::string petsc_args)
```

```
~NonlinearSolver () override
```

```
virtual void solve () override
```

## Private Members

PetscOptions **snes\_options**

Vec **\_xvec**

Vec **\_rvec**

Mat **J**

SNES **snes**

*residual\_ctx* **res\_ctx**

```
class not_implemented_error : public std::runtime_error
    #include <errors.hh>
```

```
class OptimizationSolver : public tamaas::PolonskyKeerRey
    #include <tao.hh> Wrapper to PETSc TAO abstract solver.
```

## Public Types

```
using gradient_context = std::tuple<std::vector<UInt>, model_type, functional::MetaFunctional*>
```

## Public Functions

```
OptimizationSolver (Model &model, const GridBase<Real> &surface, Real tolerance, std::string
    petsc_args)
```

```
~OptimizationSolver () override
```

```
virtual Real solve (std::vector<Real> target_gap) override
    Solve for a mean traction vector.
```

## Private Members

PetscOptions **tao\_options**

Vec **\_primal\_vec**

Vec **\_dual\_vec**

Vec **\_lower\_b**

Vec **\_upper\_b**

Mat **H**

Mat **P**

Tao **tao**

*gradient\_context* **grad\_ctx**

template<U**Int** **dim**>

struct **Partitioner**

*#include* <partitioner.hh>

### Public Static Functions

template<typename **Container**>

static inline decltype(auto) **global\_size** (*Container* local)

template<typename **T**>

static inline decltype(auto) **global\_size** (const *Grid*<**T**, *dim*> &grid)

template<typename **Container**>

static inline decltype(auto) **local\_size** (*Container* global)

template<typename **T**>

static inline decltype(auto) **local\_size** (const *Grid*<**T**, *dim*> &grid)

static inline decltype(auto) **local\_size** (*std::initializer\_list*<U**Int**> list)

template<typename **Container**>

static inline decltype(auto) **local\_offset** (const *Container* &global)

template<typename **T**>

static inline decltype(auto) **local\_offset** (const *Grid*<**T**, *dim*> &grid)

static inline decltype(auto) **local\_offset** (*std::initializer\_list*<U**Int**> list)

template<typename **Container**>

static inline decltype(auto) **cast\_size** (const *Container* &s)

static inline decltype(auto) **alloc\_size** (const *std::array*<U**Int**, *dim*> &global, U**Int** howmany)

template<typename **T**>

static inline *Grid*<**T**, *dim*> **gather** (const *Grid*<**T**, *dim*> &send)

template<typename **T**>

static inline *Grid*<**T**, *dim*> **scatter** (const *Grid*<**T**, *dim*> &send)

struct **plan**

*#include* <cufft\_engine.hh>

## Public Functions

```

plan () = default
inline plan (plan &&o) noexcept
inline plan &operator= (plan &&o) noexcept
inline ~plan () noexcept
    Destroy plan.
inline operator cufftHandle () const
    For seamless use with fftw api.

```

## Public Members

```

cufftHandle _plan
template<typename T>
struct plan
    #include <interface_impl.hh> Holder type for fftw plans.

```

## Public Functions

```

inline explicit plan (typename helper<T>::plan _plan = nullptr)
    Create from plan.
inline plan (plan &&o) noexcept
    Move constructor to avoid accidental plan destruction.
inline plan &operator= (plan &&o) noexcept
    Move operator.
inline ~plan () noexcept
    Destroy plan.
inline operator typename helper<T>::plan () const
    For seamless use with fftw api.

```

## Public Members

```

helper<T>::plan _plan
class PolonskyKeerRey : public tamaas::ContactSolver
    #include <polonsky_keer_rey.hh> Subclassed by tamaas::KatoSaturated, tamaas::MaxwellViscoelastic,
    tamaas::petsc::OptimizationSolver

```

## Public Types

enum **type**

Types of algorithm (primal/dual) or constraint.

Values:

enumerator **gap**

enumerator **pressure**

## Public Functions

**PolonskyKeerRey** (*Model* &model, const *GridBase*<*Real*> &surface, *Real* tolerance, *type* variable\_type, *type* constraint\_type)

Constructor.

**~PolonskyKeerRey** () override = default

virtual *Real* **solve** (*std::vector*<*Real*> target) override

Solve.

virtual *Real* **meanOnUnsaturated** (const *GridBase*<*Real*> &field) const

Mean on unsaturated constraint zone.

Computes  $\frac{1}{\text{card}(\{p>0\})} \sum_{\{p>0\}} f_i$

virtual *Real* **computeSquaredNorm** (const *GridBase*<*Real*> &field) const

Compute squared norm.

Computes  $\sum_{\{p>0\}} f_i^2$

virtual void **updateSearchDirection** (*Real* factor)

Update search direction.

Do  $\mathbf{t} = \mathbf{q}' + \delta \frac{R}{R_{\text{old}}} \mathbf{t}$

virtual *Real* **computeCriticalStep** (*Real* target = 0)

Compute critical step.

Computes  $\tau = \frac{\sum_{\{p>0\}} q'_i t_i}{\sum_{\{p>0\}} r'_i t_i}$

virtual bool **updatePrimal** (*Real* step)

Update primal and check non-admissible state.

Update steps:

- i.  $\mathbf{p} = \mathbf{p} - \tau \mathbf{t}$
- ii. Truncate all  $p$  negative
- iii. For all points in  $I_{\text{na}} = \{p = 0 \wedge q < 0\}$  do  $p_i = p_i - \tau q_i$

virtual *Real* **computeError** () const  
 Compute error/stopping criterion.  
 Error is based on  $\sum p_i q_i$

virtual void **enforceAdmissibleState** ()  
 Enforce contact constraints on final state.

virtual void **enforceMeanValue** (*Real* mean)  
 Enfore mean value constraint.

void **setIntegralOperator** (*std::string* name)  
 Set integral operator for gradient computation.

void **setupFunctional** ()  
 Set functionals for contact.

### Protected Attributes

*type* **variable\_type**

*type* **constraint\_type**

*model\_type* **operation\_type**

*GridBase<Real>* \***primal** = nullptr  
 non-owning pointer for primal variable

*GridBase<Real>* \***dual** = nullptr  
 non-owning pointer for dual variable

*std::unique\_ptr<GridBase<Real>>* **search\_direction** = nullptr  
 CG search direction.

*std::unique\_ptr<GridBase<Real>>* **projected\_search\_direction** = nullptr  
 Projected CG search direction.

*std::unique\_ptr<GridBase<Real>>* **pressure\_view**  
 View on normal pressure, gap, displacement.

*std::unique\_ptr<GridBase<Real>>* **gap\_view**

*std::unique\_ptr<GridBase<Real>>* **displacement\_view** = nullptr

*std::shared\_ptr<IntegralOperator>* **integral\_op** = nullptr  
 Integral operator for gradient computation.

## Private Functions

```
template<model_type type>
void setViews ()
```

Set correct views on normal traction and gap.

```
template<model_type type>
void defaultOperator ()
```

Set the default integral operator.

```
class PolonskyKeerTan : public tamaas::Kato
  #include <polonsky_keer_tan.hh>
```

## Public Functions

```
PolonskyKeerTan (Model &model, const GridBase<Real> &surface, Real tolerance, Real mu)
```

Constructor.

```
virtual Real solve (std::vector<Real> p0) override
```

Solve with Coulomb friction.

```
Real solveTresca (GridBase<Real> &p0)
```

Solve with Tresca friction.

```
template<model_type type>
Real solveTpl (GridBase<Real> &p0, bool use_tresca = false)
```

Template for solve function.

```
template<UInt comp>
void enforcePressureMean (GridBase<Real> &p0)
```

Enforce pressure mean.

```
template<UInt comp>
Vector<Real, comp> computeMean (GridBase<Real> &field, bool on_c)
```

Compute mean of field (only on I\_c)

```
Real computeSquaredNorm (GridBase<Real> &field)
```

Compute squared norm.

```
template<UInt comp>
void truncateSearchDirection (bool on_c)
```

Restrict search direction on I\_c.

```
template<UInt comp>
Real computeStepSize (bool on_c)
  Compute optimal step size (only on I_c)
```

## Private Members

```
std::unique_ptr<GridBase<Real>> search_direction = nullptr
```

```
std::unique_ptr<GridBase<Real>> search_direction_backup = nullptr
```

```
std::unique_ptr<GridBase<Real>> projected_search_direction = nullptr
```

```
template<UInt... ns>
```

```
struct product : public detail::product_tail_rec<1, ns...>
```

```
    #include <static_types.hh>
```

```
template<UInt acc, UInt n>
```

```
struct product_tail_rec<acc, n> : public std::integral_constant<UInt, acc * n>
```

```
    #include <static_types.hh>
```

```
template<typename T>
```

```
struct ptr
```

```
    #include <interface_impl.hh> RAII helper for fftw_free.
```

## Public Functions

```
inline ~ptr () noexcept
```

```
inline operator T* ()
```

## Public Members

```
T *_ptr
```

```
template<typename LocalType, typename ValueType, UInt local_size>
```

```
class Range
```

```
    #include <ranges.hh> Range class for complex iterators.
```

## Public Types

```
using value_type = LocalType
```

```
using reference = value_type&&
```

## Public Functions

```
template<class Container>
inline Range (Container &&cont)
    Construct from a container.

inline Range (iterator _begin, iterator _end)
    Construct from two iterators.

inline iterator begin ()

inline iterator end ()

inline Range headless () const
```

## Private Members

```
iterator _begin
```

```
iterator _end
```

```
template<operation op, typename ReturnType>
```

```
struct reduction_helper
```

```
template<typename ReturnType>
```

```
struct reduction_helper<operation::max, ReturnType> : public thrust::maximum<ReturnType>
    #include <loop_utils.hh>
```

## Public Functions

```
inline ReturnType init () const
```

```
template<typename ReturnType>
```

```
struct reduction_helper<operation::min, ReturnType> : public thrust::minimum<ReturnType>
    #include <loop_utils.hh>
```

## Public Functions

```
inline ReturnType init () const
```

```
template<typename ReturnType>
```

```
struct reduction_helper<operation::plus, ReturnType> : public thrust::plus<ReturnType>
    #include <loop_utils.hh>
```

### Public Functions

```
inline ReturnType init () const
```

```
template<typename ReturnType>
```

```
struct reduction_helper<operation::times, ReturnType> : public thrust::multiplies<ReturnType>
    #include <loop_utils.hh>
```

### Public Functions

```
inline ReturnType init () const
```

```
template<UInt dim>
```

```
class RegularizedPowerlaw : public tamaas::Filter<dim>
    #include <regularized_powerlaw.hh> Class representing an isotropic power law spectrum.
```

### Public Functions

```
virtual void computeFilter (GridHermitian<Real, dim> &filter_coefficients) const override
    Compute filter coefficients.
```

```
inline Real operator () (const VectorProxy<Real, dim> &q_vec) const
    Compute a point of the PSD.
```

```
TAMAAS_ACCESSOR (q1, UInt, Q1)
```

```
TAMAAS_ACCESSOR (q2, UInt, Q2)
```

```
TAMAAS_ACCESSOR (hurst, Real, Hurst)
```

### Protected Attributes

```
UInt q1
```

```
UInt q2
```

```
Real hurst
```

```
class Residual
    #include <residual.hh> Residual manager.
```

## Public Functions

**Residual** (*Model* &model, *std::shared\_ptr<Material>* material)

Constructor.

virtual **~Residual** () = default

Destructor.

virtual void **computeResidual** (*GridBase<Real>* &strain\_increment)

Compute the residual vector for a given strain increment.

virtual void **computeResidualDisplacement** (*GridBase<Real>* &strain\_increment)

Compute residual surface displacement.

virtual void **applyTangent** (*GridBase<Real>* &output, *GridBase<Real>* &input, *GridBase<Real>* &strain\_increment)

Apply tangent to arbitrary increment.

virtual void **updateState** (*GridBase<Real>* &converged\_strain\_increment)

Update the plastic state.

inline const *Model* &**getModel** () const

Return model reference.

inline *Model* &**getModel** ()

Return model reference (non-const)

inline const *GridBase<Real>* &**getVector** () const

Return residual vector.

inline const *Material* &**getMaterial** () const

Return material.

## Protected Attributes

*Model* &**model**

*std::shared\_ptr<Material>* **material**

*std::shared\_ptr<Grid<Real, 3>>* **strain**

*std::shared\_ptr<Grid<Real, 3>>* **stress**

*std::shared\_ptr<Grid<Real, 3>>* **residual**

*std::shared\_ptr<Grid<Real, 3>>* **tmp**

*std::unordered\_set<UInt>* **plastic\_layers**

*std::function<bool(UInt)>* **plastic\_filter**

### Private Functions

inline const *IntegralOperator* &**integralOperator** (const *std::string* &name) const  
 Convenience function.

void **updateFilter** (*Grid<Real, dim>* &plastic\_strain\_increment)  
 Add non-zero layers of plastic strain into the filter.

### Private Static Attributes

static constexpr auto **type** = *model\_type::volume\_2d*

static constexpr auto **dim** = *model\_type\_traits<type>::dimension*

static constexpr auto **voigt** = *model\_type\_traits<type>::voigt*

struct **sequential**  
*#include <mpi\_interface.hh>*

### Public Static Functions

static inline void **enter** ()

static inline void **exit** ()

struct **sequential\_guard**  
*#include <mpi\_interface.hh>*

### Public Functions

inline **sequential\_guard** ()

inline ~**sequential\_guard** ()

template<typename T>

struct **span**  
*#include <span.hh>*

### Public Types

using **element\_type** = *T*

using **value\_type** = *std::remove\_cv\_t<T>*

using **size\_type** = *std::size\_t*

```
using difference_type = std::ptrdiff_t

using pointer = T*

using const_pointer = const T*

using reference = T&

using const_reference = const T&

using iterator = T*

using reverse_iterator = std::reverse_iterator<iterator>
```

### Public Functions

```
inline constexpr size_type size () const noexcept
inline constexpr pointer data () const noexcept
inline constexpr iterator begin () const noexcept
inline constexpr iterator end () const noexcept
inline constexpr iterator begin () noexcept
inline constexpr iterator end () noexcept
inline reference operator [] (size_type idx)
inline const_reference operator [] (size_type idx) const
```

### Public Members

```
pointer data_ = nullptr
```

```
size_type size_ = 0
```

```
class SquaredExponentialAdhesionFunctional : public tamaas::functional::AdhesionFunctional
    #include <adhesion_functional.hh> Squared exponential adhesion functional.
```

## Public Functions

inline **SquaredExponentialAdhesionFunctional** (const *GridBase<Real>* &surface)

Explicit declaration of constructor for swig.

virtual *Real* **computeF** (*GridBase<Real>* &gap, *GridBase<Real>* &pressure) const override

Compute the total adhesion energy.

virtual void **computeGradF** (*GridBase<Real>* &gap, *GridBase<Real>* &gradient) const override

Compute the gradient of the adhesion functional.

template<template<typename, typename, *UInt...*> class **StaticParent**, *UInt... dims*>

struct **static\_size\_helper** : public *tamaas::product<dims...>*

*#include* <static\_types.hh>

template<*UInt n*>

struct **static\_size\_helper**<*StaticSymMatrix, n*> : public *tamaas::voigt\_size<n>*

*#include* <static\_types.hh>

template<typename **DataType**, typename **SupportType**, *UInt \_size*>

class **StaticArray**

*#include* <static\_types.hh> *Static Array.*

This class is meant to be a small and fast object for intermediate calculations, possibly on wrapped memory belonging to a grid. Support type should be either a pointer or a C array. It should not contain any virtual method.

Subclassed by *tamaas::StaticTensor< DataType, SupportType, dims >*

## Public Types

using **value\_type** = *T*

## Public Functions

**StaticArray** () = default

**~StaticArray** () = default

**StaticArray** (const *StaticArray*&) = delete

**StaticArray** (*StaticArray*&&) = delete

*StaticArray* &**operator=** (*StaticArray*&&) = delete

inline auto **operator** () (*UInt i*) -> *T*&

Access operator.

inline auto **operator** () (*UInt i*) const -> const *T*&

Access operator.

template<typename **DT**, typename **ST**>

```
inline auto dot (const StaticArray<DT, ST, size> &o) const -> T_bare  
    Scalar product.  
  
inline T_bare l2squared () const  
    L2 norm squared.  
  
inline T_bare l2norm () const  
    L2 norm.  
  
inline T_bare sum () const  
    Sum of all elements.  
  
template<typename DT, typename ST>  
inline void operator+= (const StaticArray<DT, ST, size> &o)  
  
template<typename DT, typename ST>  
inline void operator-= (const StaticArray<DT, ST, size> &o)  
  
template<typename DT, typename ST>  
inline void operator*= (const StaticArray<DT, ST, size> &o)  
  
template<typename DT, typename ST>  
inline void operator/= (const StaticArray<DT, ST, size> &o)  
  
template<typename T1>  
inline std::enable_if_t<is_arithmetic<T1>::value, StaticArray&> operator+= (const T1 &x)  
  
template<typename T1>  
inline std::enable_if_t<is_arithmetic<T1>::value, StaticArray&> operator-= (const T1 &x)  
  
template<typename T1>  
inline std::enable_if_t<is_arithmetic<T1>::value, StaticArray&> operator*= (const T1 &x)  
  
template<typename T1>  
inline std::enable_if_t<is_arithmetic<T1>::value, StaticArray&> operator/= (const T1 &x)  
  
template<typename T1>  
inline std::enable_if_t<is_arithmetic<T1>::value, StaticArray&> operator= (const T1 &x)  
  
inline StaticArray &operator= (const StaticArray &o)  
    Overriding the implicit copy operator.  
  
template<typename DT, typename ST>  
inline void operator= (const StaticArray<DT, ST, size> &o)  
  
template<typename DT, typename ST>  
inline StaticArray &copy (const StaticArray<DT, ST, size> &o)  
  
inline T *begin ()  
  
inline const T *begin () const  
  
inline T *end ()  
  
inline const T *end () const  
  
inline valid_size_t<T&> front ()  
  
inline valid_size_t<const T&> front () const
```

```
inline valid_size_t<T&> back ()
inline valid_size_t<const T&> back () const
```

## Public Static Attributes

```
static constexpr UInt size = _size
```

## Protected Attributes

```
SupportType _mem
```

## Private Types

```
using T = DataType
```

```
using T_bare = typename std::remove_cv_t<T>
```

```
template<typename U>
```

```
using valid_size_t = std::enable_if_t<(size > 0), U>
```

```
template<typename DataType, typename SupportType, UInt n, UInt m>
```

```
class StaticMatrix : public tamaas::StaticTensor<DataType, SupportType, n, m>
    #include <static_types.hh>
```

## Public Functions

```
template<typename DT, typename ST>
std::enable_if_t<n == m> fromSymmetric (const StaticSymMatrix<DT, ST, n> &o)
```

```
template<typename DT1, typename ST1, typename DT2, typename ST2>
void outer (const StaticVector<DT1, ST1, n> &a, const StaticVector<DT2, ST2, m> &b)
```

Outer product of two vectors.

```
template<typename DT1, typename ST1, typename DT2, typename ST2, UInt l>
inline void mul (const StaticMatrix<DT1, ST1, n, l> &a, const StaticMatrix<DT2, ST2, l, m> &b)
```

```
inline std::enable_if_t<n == m, T_bare> trace () const
```

```
template<typename DT1, typename ST1>
inline std::enable_if_t<n == m> deviatoric (const StaticMatrix<DT1, ST1, n, m> &mat, Real factor = n)
```

## Private Types

```
using T = DataType
```

```
using T_bare = typename std::remove_cv_t<T>
```

```
template<typename DataType, typename SupportType, UInt n>
```

```
class StaticSymMatrix : public tamaas::StaticVector<DataType, SupportType, voigt_size<n>::value>  
    #include <static_types.hh> Symmetric matrix in Voigt notation.
```

## Public Functions

```
template<typename DT, typename ST>  
inline void symmetrize (const StaticMatrix<DT, ST, n, n> &m)  
    Copy values from matrix and symmetrize.
```

```
template<typename DT, typename ST>  
inline void operator+= (const StaticMatrix<DT, ST, n, n> &m)  
    Add values from symmetrized matrix.
```

```
inline auto trace () const
```

```
template<typename DT, typename ST>  
inline void deviatoric (const StaticSymMatrix<DT, ST, n> &m, Real factor = n)
```

## Private Types

```
using parent = StaticVector<DataType, SupportType, voigt_size<n>::value>
```

```
using T = std::remove_cv_t<DataType>
```

## Private Functions

```
template<typename DT, typename ST, typename BinOp>  
inline void sym_binary (const StaticMatrix<DT, ST, n, n> &m, BinOp &&op)
```

```
template<typename DataType, typename SupportType = DataType*, UInt... dims>
```

```
class StaticTensor : public tamaas::StaticArray<DataType, DataType*, product<dims...>::value>  
    #include <static_types.hh> Static Tensor.
```

This class implements a multi-dimensional tensor behavior.

## Public Functions

```
template<typename ...Idx>
inline const T &operator () (Idx... idx) const
```

```
template<typename ...Idx>
inline T &operator () (Idx... idx)
```

## Public Static Attributes

```
static constexpr UInt dim = sizeof...(dims)
```

## Private Types

```
using parent = StaticArray<DataType, SupportType, product<dims...>::value>
```

```
using T = DataType
```

## Private Static Functions

```
template<typename ...Idx>
static inline UInt unpackOffset (UInt offset, UInt index, Idx... rest)
```

```
template<typename ...Idx>
static inline UInt unpackOffset (UInt offset, UInt index)
```

```
template<typename DataType, typename SupportType, UInt n>
```

```
class StaticVector : public tamaas::StaticTensor<DataType, SupportType, n>
#include <static_types.hh> Vector class with size determined at compile-time.
```

## Public Functions

```
template<bool transpose, typename DT1, typename ST1, typename DT2, typename ST2, UInt m>
inline void mul (const StaticMatrix<DT1, ST1, n, m> &mat, const StaticVector<DT2, ST2, m> &vec)
Matrix-vector product.
```

## Private Types

```
using T = std::remove_cv_t<DataType>
```

```
template<UInt dim>
```

```
struct Statistics
```

```
#include <statistics.hh> Suitcase class for all statistics related functions.
```

## Public Types

using **PVector** = *VectorProxy*<Real, dim>

## Public Functions

*std::vector*<Real> **computeMoments** (*Grid*<Real, 1> &surface)

*std::vector*<Real> **computeMoments** (*Grid*<Real, 2> &surface)

## Public Static Functions

static Real **computeRMSHeights** (*Grid*<Real, dim> &surface)

Compute hrms.

static Real **computeSpectralRMSSlope** (*Grid*<Real, dim> &surface)

Compute hrms' in fourier space.

static Real **computeSpectralEnergy** (*Grid*<Real, dim> &surface)

Compute the full contact elastic energy (unscaled by E\* / L)

static Real **computeFullContactPressure** (*Grid*<Real, dim> &surface)

Compute the full contact pressure (unscaled by E\*)

static Real **computeFDRMSSlope** (*Grid*<Real, dim> &surface)

Compute hrms' with finite differences.

static *GridHermitian*<Real, dim> **computePowerSpectrum** (*Grid*<Real, dim> &surface)

Compute PSD of surface.

static *Grid*<Real, dim> **computeAutocorrelation** (*Grid*<Real, dim> &surface)

Compute autocorrelation.

static *std::vector*<Real> **computeMoments** (*Grid*<Real, dim> &surface)

Compute spectral moments.

static Real **contact** (const *Grid*<Real, dim> &tractions, *UInt* perimeter = 0)

Compute (corrected) contact area fraction.

static Real **graphArea** (const *Grid*<Real, dim> &displacement)

Compute the area scaling factor of a periodic graph.

## Private Static Functions

template<class T>

static Real **rmsSlopesFromPSD** (const *GridHermitian*<Real, dim> &psd, const *Grid*<T, dim> &diff)

template<*UInt* dim>

class **SurfaceGenerator**

*#include* <surface\_generator.hh> Class generating random surfaces.

Subclassed by *tamaas::SurfaceGeneratorFilter*< dim >

## Public Functions

**SurfaceGenerator** () = default  
Default constructor.

inline **SurfaceGenerator** (*std::array<UInt, dim>* global\_size)  
Construct with surface global size.

virtual **~SurfaceGenerator** () = default  
Default destructor.

virtual *Grid<Real, dim>* &**buildSurface** () = 0  
Build surface profile (array of heights)

void **setSize**s (*std::array<UInt, dim>* n)  
Set surface sizes.

void **setSize**s (const *UInt* n[*dim*])  
Set surface sizes.

inline auto **getS**izes () const  
Get surface sizes.

inline long **getRandomSeed** () const

void **setRandomSeed** (long seed)

## Protected Attributes

*Grid<Real, dim>* **grid**

*std::array<UInt, dim>* **global\_size** = {0}

long **random\_seed** = 0

template<*UInt dim*>

class **SurfaceGeneratorFilter** : public *tamaas::SurfaceGenerator<dim>*  
*#include <surface\_generator\_filter.hh>* Subclassed by *tamaas::SurfaceGeneratorRandomPhase<dim >*

## Public Functions

virtual *Grid<Real, dim>* &**buildSurface** () override  
Construct with surface size.  
Build surface with Hu & Tonder algorithm

inline void **setFilter** (*std::shared\_ptr<Filter<dim>>* new\_filter)  
Set filter object.

inline void **setSpectrum** (*std::shared\_ptr<Filter<dim>>* spectrum)  
Set spectrum.

inline const *Filter<dim>* \***getSpectrum** () const  
Get spectrum.

### Protected Functions

```
void applyFilterOnSource ()  
    Apply filter coefficients on white noise.  
  
template<typename T>  
void generateWhiteNoise ()  
    Generate white noise with given distribution.
```

### Protected Attributes

```
std::shared_ptr<Filter<dim>> filter = nullptr  
  
GridHermitian<Real, dim> filter_coefficients  
  
Grid<Real, dim> white_noise  
  
std::unique_ptr<FFTEngine> engine = FFTEngine::makeEngine()  
  
template<UInt dim>  
class SurfaceGeneratorRandomPhase : public tamaas::SurfaceGeneratorFilter<dim>  
    #include <surface_generator_random_phase.hh>
```

### Public Functions

```
virtual Grid<Real, dim> &buildSurface () override  
    Build surface with uniform random phase.  
  
template<model_type type>  
struct SurfaceTractionHelper  
    #include <kelvin_helper.hh>
```

### Public Types

```
using trait = model_type_traits<type>  
  
using BufferType = GridHermitian<Real, bdim>  
  
using kelvin_t = influence::Kelvin<3, 2>  
  
using source_t = typename KelvinTrait<kelvin_t>::source_t  
  
using out_t = typename KelvinTrait<kelvin_t>::out_t
```

## Public Functions

```
template<bool apply_q_power>
inline void computeSurfaceTractions (std::vector<BufferType> &source, BufferType &tractions, const
                                     Grid<Real, bdim> &wavevectors, Real domain_size, const
                                     kelvin_t &kelvin, const influence::ElasticHelper<dim> &el)
```

Compute surface tractions due to eigenstress distribution.

## Public Static Attributes

```
static constexpr UInt dim = trait::dimension
```

```
static constexpr UInt bdim = trait::boundary_dimension
```

## Protected Attributes

```
Accumulator<type, source_t> accumulator
```

```
struct TamaasInfo
```

```
    #include <tamaas_info.hh>
```

## Public Static Attributes

```
static const std::string version
```

```
static const std::string build_type
```

```
static const std::string branch
```

```
static const std::string commit
```

```
static const std::string remotes
```

```
static const std::string diff
```

```
static const std::string backend
```

```
static const bool has_mpi
```

```
static const bool has_petsc
```

```
template<template<typename, typename, UInt...> class StaticParent, typename T, UInt... dims>
```

```
class Tensor : public StaticParent<T, T[static_size_helper<StaticParent, dims...>::value], dims...>
```

```
    #include <static_types.hh>
```

## Public Functions

```
Tensor () = default
    Default constructor.

inline Tensor (T val)
    Construct with default value.

inline Tensor (const std::array<T, size> &arr)
    Construct from array.

inline Tensor &operator= (const std::array<T, size> &arr)
    Copy from array.

template<typename DT, typename ST>
inline Tensor (const StaticParent<DT, ST, dims...> &o)
    Construct by copy from static tensor.

inline Tensor (const Tensor &o)

inline Tensor &operator= (const Tensor &o)

inline Tensor (Tensor &&o) noexcept
```

## Private Types

```
using parent = StaticParent<T, T[size], dims...>
```

## Private Static Attributes

```
static constexpr UInt size = static_size_helper<StaticParent, dims...>::value

template<template<typename, typename, UInt...> class StaticParent, typename T, UInt... dims>
class TensorProxy : public StaticParent<T, T*, dims...>
    #include <static_types.hh> Proxy type for tensor.
```

## Public Types

```
using stack_type = Tensor<StaticParent, T, dims...>
```

## Public Functions

```
inline explicit TensorProxy (T *spot)
    Explicit construction from data location.

inline explicit TensorProxy (T &spot)
    Explicit construction from lvalue-reference.

template<typename DataType, typename SupportType>
inline TensorProxy (StaticParent<DataType, SupportType, dims...> &o)
    Construction from static tensor.

inline TensorProxy (const TensorProxy &o)

inline TensorProxy &operator= (const TensorProxy &o)

inline TensorProxy (TensorProxy &&o) noexcept
```

## Private Types

```
using parent = StaticParent<T, T*, dims...>
```

```
struct ToleranceManager
```

```
#include <ep_solver.hh>
```

## Public Functions

```
inline ToleranceManager (Real start, Real end, Real rate)

inline void step ()

inline void reset ()
```

## Public Members

```
Real start_tol
```

```
Real end_tol
```

```
Real rate
```

```
Real tolerance
```

```
template<typename Iterator, typename Functor, typename Value>
class transform_iterator : public thrust::iterator_adaptor<transform_iterator<Iterator, Functor, Value>,
Iterator, Value, thrust::use_default, thrust::use_default, Value>
    #include <loop.hh> Replacement for thrust::transform_iterator which copies values.
```

## Public Types

```
using super_t = thrust::iterator_adaptor<transform_iterator<Iterator, Functor, Value>, Iterator, Value, thrust::use_default, thrust::use_default, Value>
```

## Public Functions

```
inline transform_iterator (const Iterator &x, const Functor &func)
```

## Private Functions

```
inline auto dereference () const -> decltype(func(*this->base()))
```

## Private Members

```
Functor func
```

## Friends

```
friend class thrust::iterator_core_access
```

```
template<typename T>
```

```
struct UnifiedAllocator
```

```
#include <unified_allocator.hh> Class allocating unified memory
```

## Public Static Functions

```
static inline span<T> allocate (typename span<T>::size_type n) noexcept  
    Allocate memory.
```

```
static inline void deallocate (span<T> view) noexcept  
    Free memory.
```

```
template<UInt dim>
```

```
struct voigt_size
```

```
template<>
```

```
struct voigt_size<1> : public std::integral_constant<UInt, 1>  
    #include <static_types.hh>
```

```
template<>
```

```
struct voigt_size<2> : public std::integral_constant<UInt, 3>  
    #include <static_types.hh>
```

```
template<>
```

```
struct voigt_size<3> : public std::integral_constant<Unt, 6>
    #include <static_types.hh>
```

```
template<model_type type>
```

```
class VolumePotential : public tamaas::IntegralOperator
```

#include <volume\_potential.hh> Volume potential operator class. Applies the operators for computation of displacements and strains due to residual/eigen strains.

Subclassed by *tamaas::Boussinesq*< *type*, *derivative* >, *tamaas::Kelvin*< *type*, *derivative* >

## Public Functions

**VolumePotential** (*Model* \*model)

inline virtual void **updateFromModel** () override

Update from model (does nothing)

inline virtual *IntegralOperator::kind* **getKind** () const override

Kind.

virtual *model\_type* **getType** () const override

Type.

inline virtual void **apply** (*GridBase*<*Real*> &input, *GridBase*<*Real*> &output) const override

Apply to all of the source layers.

## Protected Types

```
using filter_t = const std::function<bool(Unt)>&
```

```
using BufferType = GridHermitian<Real, trait::boundary_dimension>
```

## Protected Functions

void **transformSource** (*GridBase*<*Real*> &in, *filter\_t* pred) const

Transform source layer-by-layer.

inline void **transformSource** (*GridBase*<*Real*> &in) const

Transform all source.

```
template<typename Func>
```

void **transformOutput** (*Func* func, *GridBase*<*Real*> &out) const

Transform output layer-by-layer.

void **initialize** (*U*nt source\_components, *U*nt out\_components, *U*nt out\_buffer\_size)

Initialize fourier buffers.

## Protected Attributes

*Grid*<*Real*, *trait*::*boundary\_dimension*> **wavevectors**

mutable *std*::*vector*<*BufferType*> **source\_buffer**

mutable *std*::*vector*<*BufferType*> **out\_buffer**

mutable *std*::*unique\_ptr*<*FFTEngine*> **engine**

## Private Types

using **trait** = *model\_type\_traits*<*type*>

struct **VonMises**

*#include* <*computes.hh*> Compute von Mises stress on a tensor field.

## Public Static Functions

template<*UInt dim*>

static inline void **call** (*Grid*<*Real*, *dim*> &*vm*, const *Grid*<*Real*, *dim*> &*stress*)

template<*model\_type mtype*, *IntegralOperator*::*kind otype*>

class **Westergaard** : public *tamaas*::*IntegralOperator*

*#include* <*westergaard.hh*> Operator based on *Westergaard* solution and the Discrete Fourier Transform. This class is templated with model type to allow efficient storage of the influence coefficients. The integral operator is only applied to surface pressure/displacements, even for volume models.

## Public Functions

**Westergaard** (*Model* \**model*)

Constructor: initializes influence coefficients and allocates buffer.

inline const *GridHermitian*<*Real*, *bdim*> &**getInfluence** () const

Get influence coefficients.

virtual void **apply** (*GridBase*<*Real*> &*input*, *GridBase*<*Real*> &*output*) const override

Apply influence coefficients to input.

inline virtual void **updateFromModel** () override

Update the influence coefficients.

inline virtual *IntegralOperator*::*kind* **getKind** () const override

Kind.

inline virtual *model\_type* **getType** () const override

Type.

```

void initInfluence ()
    Initialize influence coefficients.

template<typename Functor>
void initFromFunctor (Functor func)

template<typename Functor>
void fourierApply (Functor func, GridBase<Real> &in, GridBase<Real> &out) const
    Apply a functor in Fourier space.

virtual Real getOperatorNorm () override
    Compute L2 norm of influence functions.

virtual std::pair<UInt, UInt> matvecShape () const override
    Dense shape.

virtual GridBase<Real> matvec (GridBase<Real> &x) const override
    Dense matvec.

```

## Public Members

```
std::shared_ptr<GridHermitian<Real, bdim>> influence
```

```
mutable GridHermitian<Real, bdim> buffer
```

```
mutable std::unique_ptr<FFTEngine> engine
```

## Private Types

```
using trait = model_type_traits<mtype>
```

## Private Static Attributes

```
static constexpr UInt dim = trait::dimension
```

```
static constexpr UInt bdim = trait::boundary_dimension
```

```
static constexpr UInt comp = trait::components
```

```
namespace cufft
```

```
namespace detail
```

```
namespace fftw
```

```
namespace fftw_impl
```

## Functions

template<typename T>  
inline auto **free** (T \*ptr)

Free memory.

inline auto **init\_threads** ()

Init FFTW with threads.

inline auto **plan\_with\_nthreads** (int nthreads)

Set number of threads.

inline auto **cleanup\_threads** ()

Cleanup threads.

inline auto **plan\_many\_forward** (int rank, const int \*n, int howmany, double \*in, const int \*inembed, int  
istride, int idist, fftw\_complex \*out, const int \*onembed, int ostride, int  
odist, unsigned flags)

inline auto **plan\_many\_backward** (int rank, const int \*n, int howmany, fftw\_complex \*in, const int  
\*inembed, int istride, int idist, double \*out, const int \*onembed, int  
ostride, int odist, unsigned flags)

inline auto **plan\_1d\_forward** (int n, double \*in, fftw\_complex \*out, unsigned flags)

inline auto **plan\_1d\_backward** (int n, fftw\_complex \*in, double \*out, unsigned flags)

inline auto **plan\_2d\_forward** (int n0, int n1, double \*in, fftw\_complex \*out, unsigned flags)

inline auto **plan\_2d\_backward** (int n0, int n1, fftw\_complex \*out, double \*in, unsigned flags)

inline auto **execute** (fftw\_plan plan)

inline auto **execute** (fftw\_plan plan, double \*in, fftw\_complex \*out)

inline auto **execute** (fftw\_plan plan, fftw\_complex \*in, double \*out)

inline auto **destroy** (fftw\_plan plan)

inline auto **plan\_many\_forward** (int rank, const int \*n, int howmany, long double \*in, const int \*inembed,  
int istride, int idist, fftwl\_complex \*out, const int \*onembed, int ostride,  
int odist, unsigned flags)

inline auto **plan\_many\_backward** (int rank, const int \*n, int howmany, fftwl\_complex \*in, const int  
\*inembed, int istride, int idist, long double \*out, const int \*onembed, int  
ostride, int odist, unsigned flags)

inline auto **plan\_1d\_forward** (int n, long double \*in, fftwl\_complex \*out, unsigned flags)

inline auto **plan\_1d\_backward** (int n, fftwl\_complex \*in, long double \*out, unsigned flags)

inline auto **plan\_2d\_forward** (int n0, int n1, long double \*in, fftwl\_complex \*out, unsigned flags)

inline auto **plan\_2d\_backward** (int n0, int n1, fftwl\_complex \*out, long double \*in, unsigned flags)

inline auto **execute** (fftwl\_plan plan)

inline auto **execute** (fftwl\_plan plan, long double \*in, fftwl\_complex \*out)

```

inline auto execute (fftwl_plan plan, fftwl_complex *in, long double *out)

inline auto destroy (fftwl_plan plan)

inline auto plan_many_forward (int rank, const int *n, int howmany, float *in, const int *inembed, int
                                istrade, int idist, fftwf_complex *out, const int *onembed, int ostride, int
                                odist, unsigned flags)

inline auto plan_many_backward (int rank, const int *n, int howmany, fftwf_complex *in, const int
                                *inembed, int istrade, int idist, float *out, const int *onembed, int ostride,
                                int odist, unsigned flags)

inline auto plan_1d_forward (int n, float *in, fftwf_complex *out, unsigned flags)

inline auto plan_1d_backward (int n, fftwf_complex *in, float *out, unsigned flags)

inline auto plan_2d_forward (int n0, int n1, float *in, fftwf_complex *out, unsigned flags)

inline auto plan_2d_backward (int n0, int n1, fftwf_complex *out, float *in, unsigned flags)

inline auto execute (fftwf_plan plan)

inline auto execute (fftwf_plan plan, float *in, fftwf_complex *out)

inline auto execute (fftwf_plan plan, fftwf_complex *in, float *out)

inline auto destroy (fftwf_plan plan)

```

```
namespace mpi_dummy
```

### Functions

```

inline void init ()

inline void cleanup ()

inline auto local_size_many (int rank, const std::ptrdiff_t *size, std::ptrdiff_t howmany)

```

```
namespace std
```

```
namespace tamaas
```

### Typedefs

```

template<typename T>

using Allocator = FFTWAllocator<T>

template<typename T, UInt n, UInt m>

using Matrix = Tensor<StaticMatrix, T, n, m>

template<typename T, UInt n>

```

```
using SymMatrix = Tensor<StaticSymMatrix, T, n>

template<typename T, UInt n>

using Vector = Tensor<StaticVector, T, n>

template<typename T, UInt n, UInt m>

using MatrixProxy = TensorProxy<StaticMatrix, T, n, m>

template<typename T, UInt n>

using SymMatrixProxy = TensorProxy<StaticSymMatrix, T, n>

template<typename T, UInt n>

using VectorProxy = TensorProxy<StaticVector, T, n>

using Real = double
    default floating point type

using Int = int
    default signed integer type

using UInt = std::make_unsigned_t<Int>
    default unsigned integer type

template<typename T>

using complex = thrust::complex<T>
    template complex wrapper

using Complex = complex<Real>
    default floating point complex type

using random_engine = ::thrust::random::default_random_engine
```

## Enums

```
enum class LogLevel
    Log levels enumeration.

    Values:

    enumerator debug

    enumerator info

    enumerator warning
```

enumerator **error**

enum class **operation**

Enumeration of reduction operations.

*Values:*

enumerator **plus**

enumerator **times**

enumerator **min**

enumerator **max**

enum class **integration\_method**

Integration method enumeration.

*Values:*

enumerator **cutoff**

enumerator **linear**

enum class **model\_type**

Types for grid dimensions and number of components.

*Values:*

enumerator **basic\_1d**

one component line

enumerator **basic\_2d**

one component surface

enumerator **surface\_1d**

two components line

enumerator **surface\_2d**

three components surface

enumerator **volume\_1d**

two components volume

enumerator **volume\_2d**

three components volume

## Functions

void **eigenvalues** (*model\_type* type, *GridBase<Real>* &eigs, const *GridBase<Real>* &field)

void **vonMises** (*model\_type* type, *GridBase<Real>* &eigs, const *GridBase<Real>* &field)

void **deviatoric** (*model\_type* type, *GridBase<Real>* &dev, const *GridBase<Real>* &field)

template<typename **Compute**>

void **applyCompute** (*model\_type* type, *GridBase<Real>* &result, const *GridBase<Real>* &field)

template<typename **T**, *UInt dim*>

inline *std::ostream* &**operator**<< (*std::ostream* &stream, const *Grid<T, dim>* &\_this)

template<template<typename, *UInt*> class **Base**, typename **T**, *UInt base\_dim*, typename ...**Args**>  
*GridView<Base, T, base\_dim, base\_dim - sizeof...(Args)>* **make\_view** (*Base<T, base\_dim>* &base, *Args...*  
indices)

template<template<typename, *UInt*> class **Base**, typename **T**, *UInt base\_dim*>  
*GridView<Base, T, base\_dim, base\_dim>* **make\_component\_view** (*Base<T, base\_dim>* &base, *UInt*  
component)

*std::ostream* &**operator**<< (*std::ostream* &o, const *LogLevel* &val)

template<typename ...**Ranges**>

void **checkLoopSize** (*Ranges&&...* ranges)

template<typename **LocalType**, class **Container**>

*std::enable\_if\_t<is\_proxy<LocalType>::value, Range<LocalType, typename LocalType::value\_type, LocalType::size>>* **range** (*Container*  
&&cont)

Make range with proxy type.

template<typename **LocalType**, class **Container**>

*std::enable\_if\_t<not is\_proxy<LocalType>::value, Range<LocalType, LocalType, 1>>* **range** (*Container*  
&&cont)

Make range with standard type.

template<typename **DT1**, typename **ST1**, typename **DT2**, typename **ST2**, *UInt dim*>  
*Vector<decltype(DT1(0) + DT2(0)), dim>* **operator+** (const *StaticVector<DT1, ST1, dim>* &a, const  
*StaticVector<DT2, ST2, dim>* &b)

template<typename **DT1**, typename **ST1**, typename **DT2**, typename **ST2**, *UInt dim*>  
*Vector<decltype(DT1(0) - DT2(0)), dim>* **operator-** (const *StaticVector<DT1, ST1, dim>* &a, const  
*StaticVector<DT2, ST2, dim>* &b)

template<typename **DT1**, typename **ST1**, *UInt dim*>  
*Vector<decltype(DT1(0)), dim>* **operator-** (const *StaticVector<DT1, ST1, dim>* &a)

template<typename **DT1**, typename **ST1**, typename **DT2**, typename **ST2**, *UInt n*, *UInt m*>  
*Matrix<decltype(DT1(0) + DT2(0)), n, m>* **operator+** (const *StaticMatrix<DT1, ST1, n, m>* &a, const  
*StaticMatrix<DT2, ST2, n, m>* &b)

template<typename **DT1**, typename **ST1**, typename **DT2**, typename **ST2**, *UInt n*, *UInt m*>  
*Matrix<decltype(DT1(0) - DT2(0)), n, m>* **operator-** (const *StaticMatrix<DT1, ST1, n, m>* &a, const  
*StaticMatrix<DT2, ST2, n, m>* &b)

template<typename **DT1**, typename **ST1**, *UInt n*, *UInt m*>

```

Matrix<decltype(DT1(0)), n, m> operator- (const StaticMatrix<DT1, ST1, n, m> &a)

template<typename DT1, typename ST1, typename DT2, typename ST2, UInt n>
SymMatrix<decltype(DT1(0) + DT2(0)), n> operator+ (const StaticSymMatrix<DT1, ST1, n> &a, const
StaticSymMatrix<DT2, ST2, n> &b)

template<typename DT1, typename ST1, typename DT2, typename ST2, UInt n>
SymMatrix<decltype(DT1(0) - DT2(0)), n> operator- (const StaticSymMatrix<DT1, ST1, n> &a, const
StaticSymMatrix<DT2, ST2, n> &b)

template<typename DT1, typename ST1, UInt dim>
SymMatrix<decltype(DT1(0)), dim> operator- (const StaticSymMatrix<DT1, ST1, dim> &a)

template<typename DT, typename ST, typename T, UInt n, typename =
std::enable_if_t<is_arithmetic<T>::value>>
Vector<decltype(DT(0) * T(0)), n> operator* (const StaticVector<DT, ST, n> &a, const T &b)

template<typename DT, typename ST, typename T, UInt n, typename =
std::enable_if_t<is_arithmetic<T>::value>>
Vector<decltype(DT(0) * T(0)), n> operator* (const T &b, const StaticVector<DT, ST, n> &a)

template<typename DT, typename ST, typename T, UInt n, UInt m, typename =
std::enable_if_t<is_arithmetic<T>::value>>
Matrix<decltype(DT(0) * T(0)), n, m> operator* (const StaticMatrix<DT, ST, n, m> &a, const T &b)

template<typename DT, typename ST, typename T, UInt n, UInt m, typename =
std::enable_if_t<is_arithmetic<T>::value, void>>
Matrix<decltype(DT(0) * T(0)), n, m> operator* (const T &b, const StaticMatrix<DT, ST, n, m> &a)

template<typename DT, typename ST, typename T, UInt n, typename =
std::enable_if_t<is_arithmetic<T>::value>>
SymMatrix<decltype(DT(0) * T(0)), n> operator* (const StaticSymMatrix<DT, ST, n> &a, const T &b)

template<typename DT, typename ST, typename T, UInt n, typename =
std::enable_if_t<is_arithmetic<T>::value>>
SymMatrix<decltype(DT(0) * T(0)), n> operator* (const T &b, const StaticSymMatrix<DT, ST, n> &a)

template<typename DT1, typename ST1, typename DT2, typename ST2, UInt n, UInt m>
Vector<decltype(DT1(0) * DT2(0)), n> operator* (const StaticMatrix<DT1, ST1, n, m> &a, const
StaticVector<DT2, ST2, m> &b)

Matrix-vector multiplication.

template<typename DT1, typename ST1, typename DT2, typename ST2, UInt n, UInt m, UInt l>
Matrix<decltype(DT1(0) * DT2(0)), n, m> operator* (const StaticMatrix<DT1, ST1, n, l> &a, const
StaticMatrix<DT2, ST2, l, m> &b)

Matrix-matrix multiplication.

template<typename DT1, typename ST1, typename DT2, typename ST2, UInt n, UInt m>
Matrix<decltype(DT1(0) * DT2(0)), n, m> outer (const StaticVector<DT1, ST1, n> &a, const
StaticVector<DT2, ST2, m> &b)

template<typename DT, typename ST, UInt n>
Matrix<std::remove_cv_t<DT>, n, n> dense (const StaticSymMatrix<DT, ST, n> &m)

template<typename DT, typename ST, UInt n>

```

```
auto dense (const StaticVector<DT, ST, n> &v) -> Vector<DT, n>

template<typename DT, typename ST, Uint n>
SymMatrix<std::remove_cv_t<DT>, n> symmetrize (const StaticMatrix<DT, ST, n, n> &m)

template<typename DT, typename ST>
Vector<std::remove_cv_t<DT>, 3> invariants (const StaticSymMatrix<DT, ST, 3> &m)

template<typename DT, typename ST>
Vector<std::remove_cv_t<DT>, 3> eigenvalues (const StaticSymMatrix<DT, ST, 3> &m)

void initialize (Uint num_threads = 0)
    initialize tamaas (0 threads => let OMP_NUM_THREADS decide)

void finalize ()
    cleanup tamaas

template<class U, class V = U>
U exchange (U &obj, V &&new_value)
    CUDA-compatible exchange function.

void solve (IntegralOperator::kind kind, const std::map<IntegralOperator::kind,
    std::shared_ptr<IntegralOperator>> &operators, GridBase<Real> &input, GridBase<Real>
    &output)

template<model_type mtype, IntegralOperator::kind otype>
void registerWestergaardOperator (std::map<IntegralOperator::kind,
    std::shared_ptr<IntegralOperator>> &operators, Model &model)

Real boussinesq (Real x, Real y, Real a, Real b)
    Square patch pressure solution, Johnson (1985) page 54.

std::ostream &operator<< (std::ostream &o, const IntegralOperator::kind &val)

std::ostream &operator<< (std::ostream &o, const Model &_this)

template<bool boundary, typename T>
std::unique_ptr<GridBase<T>> allocateGrid (Model &model)

template<bool boundary, typename T>
std::unique_ptr<GridBase<T>> allocateGrid (Model &model, Uint nc)

inline ModelDumper &operator<< (ModelDumper &dumper, Model &model)

template<typename Abstract, template<model_type> class Concrete, class ...Args>
decltype(auto) createFromModelType (model_type type, Args&&... args)

inline std::ostream &operator<< (std::ostream &o, const model_type &val)
    Print function for model_type.

template<class Function>
constexpr decltype(auto) model_type_dispatch (Function &&function, model_type type)
    Static dispatch lambda to model types.

template<class Function>
```

```
constexpr decltype(auto) dimension_dispatch (Function &&function, UInt dim)
```

Static dispatch lambda to dimensions.

```
template<model_type type, bool boundary, typename T, template<typename, UInt> class GridType =
Grid, class Container = void>
std::unique_ptr<GridType<T, detail::dim_choice<type, boundary>::value>> allocateGrid (Container &&n,
UInt nc)
```

Allocate a *Grid* *unique\_ptr*.

```
template<bool boundary, typename T, typename Container>
decltype(auto) allocateGrid (model_type type, Container &&n)
```

Helper function for grid allocation with model type.

```
template<bool boundary, typename T, typename Container>
decltype(auto) allocateGrid (model_type type, Container &&n, UInt nc)
```

Helper function for grid allocation with non-standard components.

```
template<model_type type, bool boundary, typename T, template<typename, UInt> class GridType =
Grid, class Container = void>
std::unique_ptr<GridType<T, detail::dim_choice<type, boundary>::value>> viewGrid (Container &&n, UInt
nc, span<T> data)
```

```
template<bool boundary, typename T, typename Container>
decltype(auto) viewGrid (model_type type, Container &&n, UInt nc, span<T> data)
```

Helper function to view an existing span.

```
Int wrap_pbc (Int i, Int n)
```

```
template<std::size_t dim>
std::array<UInt, dim> wrap_pbc (const std::array<Int, dim> &t, const std::array<Int, dim> &n)
```

```
template<std::size_t dim>
std::array<Int, dim> cast_int (const std::array<UInt, dim> &a)
```

```
auto factorize (Grid<Real, 2> A)
```

Crout(e) (Antoine... et Daniel...) factorization from [https://en.wikipedia.org/wiki/Crout\\_matrix\\_decomposition](https://en.wikipedia.org/wiki/Crout_matrix_decomposition)

```
auto LUsubstitute (std::pair<Grid<Real, 2>, Grid<Real, 2>> LU, Grid<Real, 1> b)
```

## Variables

```
static complex<Real> dummy
```

```
namespace tamaas
```

```
namespace tamaas
```

```
namespace tamaas
```

```
namespace tamaas
```

namespace **compute**

namespace **detail**

## Typedefs

```
template<model_type type>
```

```
using model_type_t = std::integral_constant<model_type, type>
```

Convert enum value to a type.

```
template<UInt dim>
```

```
using dim_t = std::integral_constant<UInt, dim>
```

Convert dim value to a type.

```
model_types_t = std::tu-
```

```
ple< BOOST_PP_SEQ_ENUM(BOOST_PP_SEQ_FOR_EACH(MAKE_MODEL_TYPE, ~,  
(model_type::basic_1d) (model_type::basic_2d) (model_type::surface_1d) (model_type::surfa
```

Enumeration of model types.

```
dims_t = std::tuple< BOOST_PP_SEQ_ENUM(BOOST_PP_SEQ_FOR_EACH(MAKE_DIM_TYPE,  
~, (1) (2) (3) ) )>
```

Enumeration of dimension types.

## Functions

```
template<class T>
```

```
void append_to_stream (std::ostream &s, T &&head)
```

```
template<class T, class ...Args>
```

```
void append_to_stream (std::ostream &s, T &&head, Args&&... tail)
```

```
template<class ...Args>
```

```
std::string concat_args (Args&&... args)
```

```
template<bool only_points = false, typename ...Grids>
```

```
UInt loopSize (Grids&&... grids)
```

```
template<typename ...Sizes>
```

```
void areAllEqual (bool, std::ptrdiff_t)
```

```
template<typename ...Sizes>
```

```
void areAllEqual (bool result, std::ptrdiff_t prev, std::ptrdiff_t current)
```

```
template<typename ...Sizes>
```

```
void areAllEqual (bool result, std::ptrdiff_t prev, std::ptrdiff_t current, Sizes... rest)
```

```
template<class Function, class DynamicType, class DefaultFunction, std::size_t... Is>
```

```
constexpr decltype(auto) static_switch_dispatch (const model_types_t&, Function &&function, const
DynamicType &type, DefaultFunction
&&default_function, std::index_sequence<Is...>)
```

Specialized static dispatch for all model types.

```
template<class Function, class DynamicType, class DefaultFunction, std::size_t... Is>
constexpr decltype(auto) static_switch_dispatch (const dims_t&, Function &&function, const
DynamicType &dim, DefaultFunction
&&default_function, std::index_sequence<Is...>)
```

Specialized static dispatch for all dimensions.

```
template<class TypeTuple, class Function, class DefaultFunction, class DynamicType>
constexpr decltype(auto) tuple_dispatch_with_default (Function &&function, DefaultFunction
&&default_function, const DynamicType
&type)
```

Dispatch to tuple of types with a default case.

```
template<class TypeTuple, class Function, class DynamicType>
constexpr decltype(auto) tuple_dispatch (Function &&function, const DynamicType &type)
```

Dispatch to tuple of types, error on default.

namespace **functional**

namespace **influence**

## Functions

```
template<bool conjugate, UInt dim_q>
inline Vector<Complex, dim_q + 1> computed (const VectorProxy<const Real, dim_q> &q)
```

```
template<UInt dim_q>
inline Vector<Complex, dim_q + 1> computed2 (const VectorProxy<const Real, dim_q> &q)
```

namespace **influence**

namespace **iterator\_**

namespace **mpi\_dummy**

Contains mock mpi functions.

## Enums

```
enum class thread : int
```

*Values:*

enumerator **single**

enumerator **funneled**

enumerator **serialized**

enumerator **multiple**

## Functions

inline bool **initialized** ()

inline bool **finalized** ()

inline int **init** (int\*, char\*\*\*)

inline int **init\_thread** (int\*, char\*\*\*, *thread*, *thread* \*provided)

inline int **finalize** ()

inline void **abort** (int) noexcept

inline int **rank** (*comm* = *comm::world*())

inline int **size** (*comm* = *comm::world*())

template<operation **op** = *operation::plus*, typename **T**>  
inline decltype(auto) **reduce** (*T* &&val, *comm* = *comm::world*())

template<operation **op** = *operation::plus*, typename **T**>  
inline decltype(auto) **allreduce** (*T* &&val, *comm* = *comm::world*())

template<typename **T**>  
inline decltype(auto) **gather** (const *T* \*send, *T* \*recv, int count, *comm* = *comm::world*())

template<typename **T**>  
inline decltype(auto) **scatter** (const *T* \*send, *T* \*recv, int count, *comm* = *comm::world*())

template<typename **T**>  
inline decltype(auto) **scatterv** (const *T* \*send, const *std::vector*<int>&, const *std::vector*<int>&, *T* \*recv, int  
recvcount, *comm* = *comm::world*())

template<typename **T**>  
inline decltype(auto) **bcast** (*T*\*, int, *comm* = *comm::world*())

namespace **petsc**

## Functions

PetscErrorCode **form\_residual** (SNES, Vec x, Vec f, void \*ctx)

PetscErrorCode **form\_jacobian** (SNES, Vec, Mat, Mat, void\*)

PetscErrorCode **tangent\_shell** (Mat mat, Vec x, Vec y)

PetscErrorCode **monitor** (Tao tao, void \*ctx)

PetscErrorCode **convergence** (Tao tao, void \*ctx)

PetscErrorCode **form\_gradient** (Tao, Vec x, PetscReal \*f, Vec g, void \*ctx)

PetscErrorCode **form\_hessian** (Tao, Vec, Mat, Mat, void\*)

PetscErrorCode **hessian\_shell** (Mat mat, Vec x, Vec y)

PetscErrorCode **apply\_preconditioner** (PC pc, Vec x, Vec y)

namespace **thrust**

file **allocator.hh**

```
#include "tamaas.hh" #include "fftw/fftw_allocator.hh"
```

file **array.hh**

```
#include "allocator.hh" #include "errors.hh" #include "logger.hh" #include "span.hh" #include "tamaas.hh" #include
<memory> #include <thrust/copy.h> #include <thrust/fill.h> #include <utility>
```

file **computes.cpp**

```
#include "computes.hh"
```

file **computes.hh**

```
#include "grid.hh" #include "loop.hh" #include "model_type.hh" #include "ranges.hh" #include "static_types.hh"
```

file **cufft\_engine.cpp**

```
#include "cufft_engine.hh" #include <algorithm> #include <functional> #include <numeric>
```

file **cufft\_engine.hh**

```
#include "fft_engine.hh" #include <cufft.h>
```

file **unified\_allocator.hh**

```
#include "span.hh" #include <cuda_runtime_api.h> #include <memory>
```

file **errors.hh**

```
#include <sstream> #include <stdexcept>
```

## Defines

**TAMAAS\_LOCATION**

**TAMAAS\_MSG** (...)

**TAMAAS\_ASSERT** (cond, ...)

file **fft\_engine.cpp**

```
#include "fft_engine.hh" #include "fftw/fftw_engine.hh"
```

## Defines

**inst** (x)

file **fft\_engine.hh**

```
#include "grid.hh"#include "grid_base.hh"#include "grid_hermitian.hh"#include "partitioner.hh"#include <algorithm>#include <array>#include <map>#include <memory>#include <string>
```

file **fftw\_allocator.hh**

```
#include "span.hh"#include <fftw3.h>#include <memory>
```

file **fftw\_engine.cpp**

```
#include "fftw_engine.hh"#include <algorithm>#include <functional>#include <numeric>
```

file **fftw\_engine.hh**

```
#include "fft_engine.hh"#include "fftw/interface.hh"
```

file **interface\_impl.hh**

```
#include <cstdlib>#include <fftw3.h>#include <functional>#include <numeric>#include <utility>
```

file **fftw\_mpi\_engine.cpp**

```
#include "fftw/mpi/fftw_mpi_engine.hh"#include "fftw/interface.hh"#include "logger.hh"#include "mpi_interface.hh"#include "partitioner.hh"#include <algorithm>
```

file **fftw\_mpi\_engine.hh**

```
#include "fftw/fftw_engine.hh"#include "fftw/interface.hh"#include "grid.hh"#include "grid_hermitian.hh"#include <map>
```

file **interface.hh**

```
#include "mpi/interface.hh"
```

## Defines

**FFTW\_ESTIMATE**

file **interface.hh**

```
#include "mpi_interface.hh"#include <cstdlib>#include <numeric>#include <stdexcept>#include <tuple>
```

file **grid.cpp**

```
#include "grid.hh"#include "tamaas.hh"#include <algorithm>#include <complex>#include <cstring>
```

**Defines****GRID\_INSTANCIATE\_TYPE** (type)

Class instantiation.

*file* **grid.hh**

```
#include "grid_base.hh" #include "tamaas.hh" #include <array> #include <numeric> #include <utility> #include <vector> #include "grid_tmpl.hh"
```

*file* **grid\_base.hh**

```
#include "array.hh" #include "iterator.hh" #include "loop.hh" #include "mpi_interface.hh" #include "static_types.hh" #include "tamaas.hh" #include <cstdlib> #include <limits> #include <utility> #include <vector>
```

**Defines****VEC\_OPERATOR** (op)**SCALAR\_OPERATOR** (op)**BROADCAST\_OPERATOR** (op)

Broadcast operators.

**SCALAR\_OPERATOR\_IMPL** (op)**VEC\_OPERATOR\_IMPL** (op)**BROADCAST\_OPERATOR\_IMPL** (op)*file* **grid\_hermitian.cpp**

```
#include "grid_hermitian.hh"
```

**Defines****GRID\_HERMITIAN\_INSTANCIATE** (type)*file* **grid\_hermitian.hh**

```
#include "grid.hh" #include "tamaas.hh" #include <complex> #include <type_traits> #include <vector>
```

*file* **grid\_tmpl.hh**

```
#include "grid.hh" #include "tamaas.hh"
```

*file* **grid\_view.hh**

```
#include "grid.hh" #include "tamaas.hh" #include <vector>
```

*file* **iterator.hh**

```
#include "tamaas.hh" #include <cstdlib> #include <iterator> #include <thrust/iterator/iterator_categories.h> #include <utility> #include <vector>
```

file `logger.cpp`

```
#include "logger.hh" #include "mpi_interface.hh" #include <cstdlib> #include <iostream> #include <map>
```

file `logger.hh`

```
#include "tamaas.hh" #include <sstream>
```

file `loop.cpp`

```
#include "loop.hh" #include "tamaas.hh"
```

file `loop.hh`

```
#include "loops/apply.hh" #include "loops/loop_utils.hh" #include "mpi_interface.hh" #include "ranges.hh" #include "tamaas.hh" #include <thrust/execution_policy.h> #include <thrust/for_each.h> #include <thrust/iterator/counting_iterator.h> #include <thrust/iterator/zip_iterator.h> #include <thrust/transform_reduce.h> #include <thrust/tuple.h> #include <thrust/version.h> #include <type_traits> #include <utility>
```

file `apply.hh`

```
#include "tamaas.hh" #include <cstdlib> #include <thrust/tuple.h> #include <utility>
```

file `loop_utils.hh`

```
#include "errors.hh" #include "tamaas.hh" #include <limits> #include <thrust/functional.h> #include <type_traits>
```

file `mpi_interface.cpp`

```
#include "mpi_interface.hh"
```

file `mpi_interface.hh`

```
#include "static_types.hh" #include "tamaas.hh" #include <cstdlib> #include <type_traits> #include <vector>
```

## Defines

```
MPI_ERR_TOPOLOGY
```

file `partitioner.hh`

```
#include "fftw/interface.hh" #include "grid.hh" #include "mpi_interface.hh" #include "tamaas.hh" #include <algorithm> #include <array> #include <cstdlib> #include <functional>
```

file `ranges.hh`

```
#include "errors.hh" #include "iterator.hh" #include "mpi_interface.hh" #include "static_types.hh"
```

file `span.hh`

```
#include "tamaas.hh" #include <cstdlib> #include <iterator> #include <type_traits>
```

file `static_types.hh`

```
#include "tamaas.hh" #include <thrust/detail/config/config.h> #include <thrust/sort.h> #include <type_traits>
```

## Defines

**VECTOR\_OP** (op)

**SCALAR\_OP** (op)

file **statistics.cpp**

```
#include "statistics.hh" #include "fft_engine.hh" #include "loop.hh" #include "static_types.hh"
```

## Variables

*std::array<UInt, dim>* **exponent**

file **statistics.hh**

```
#include "fft_engine.hh" #include "grid.hh"
```

file **tamaas.cpp**

```
#include "tamaas.hh" #include "errors.hh" #include "fftw/interface.hh" #include "logger.hh" #include "mpi_interface.hh"
```

## Variables

static const entry\_exit\_points **singleton**

file **tamaas.hh**

```
#include <exception> #include <iostream> #include <memory> #include <string> #include <type_traits> #include <thrust/complex.h> #include <thrust/random.h>
```

## Defines

**TAMAAS\_USE\_FFTW**

**TAMAAS\_FFTW\_BACKEND\_OMP**

**TAMAAS\_FFTW\_BACKEND\_THREADS**

**TAMAAS\_FFTW\_BACKEND\_NONE**

**TAMAAS\_LOOP\_BACKEND\_OMP**

**TAMAAS\_LOOP\_BACKEND\_TBB**

**TAMAAS\_LOOP\_BACKEND\_CPP**

**TAMAAS\_LOOP\_BACKEND\_CUDA**

**TAMAAS\_LOOP\_BACKEND**

**TAMAAS\_FFTW\_BACKEND**

**THRUST\_DEVICE\_SYSTEM**

**TAMAAS\_ACCESSOR** (var, type, name)

Convenience macros.

**CUDA\_LAMBDA**

Cuda specific definitions.

**TAMAAS\_REAL\_TYPE**

Common types definitions.

**TAMAAS\_INT\_TYPE**

*file* **adhesion\_functional.cpp**

*#include* "adhesion\_functional.hh"

*file* **adhesion\_functional.hh**

*#include* "functional.hh" *#include* <map>

*file* **be\_engine.cpp**

*#include* "be\_engine.hh" *#include* "logger.hh" *#include* "model.hh"

*file* **be\_engine.hh**

*#include* "integral\_operator.hh" *#include* "model\_type.hh" *#include* "westergaard.hh"

*file* **boussinesq.cpp**

*#include* "boussinesq.hh" *#include* "boussinesq\_helper.hh" *#include* "influence.hh" *#include* "model.hh"

*file* **boussinesq.hh**

*#include* "grid\_hermitian.hh" *#include* "model\_type.hh" *#include* "volume\_potential.hh"

*file* **boussinesq\_helper.hh**

*#include* "grid.hh" *#include* "grid\_hermitian.hh" *#include* "influence.hh" *#include* "integration/accumulator.hh" *#include* "kelvin\_helper.hh" *#include* "model.hh" *#include* "model\_type.hh" *#include* <vector>

*file* **dcfft.cpp**

*#include* "dcfft.hh" *#include* "model.hh" *#include* <cmath>

file **dcfft.hh**

```
#include "westergaard.hh"
```

file **elastic\_functional.cpp**

```
#include "elastic_functional.hh"
```

file **elastic\_functional.hh**

```
#include "functional.hh"#include "model.hh"#include "tamaas.hh"
```

file **field\_container.hh**

```
#include "grid.hh"#include "model_type.hh"#include <algorithm>#include <boost/variant.hpp>#include <memory>#include <string>#include <unordered_map>
```

file **functional.hh**

```
#include "be_engine.hh"#include "tamaas.hh"
```

file **hooke.cpp**

```
#include "hooke.hh"#include "influence.hh"#include "loop.hh"#include "model.hh"#include "static_types.hh"#include <boost/preprocessor/seq.hpp>
```

## Defines

```
INstantiate_Hooke (r, _, type)
```

file **hooke.hh**

```
#include "influence.hh"#include "integral_operator.hh"#include "model_type.hh"
```

file **influence.hh**

```
#include "loop.hh"#include "static_types.hh"#include <array>#include <type_traits>
```

file **integral\_operator.cpp**

```
#include "integral_operator.hh"#include "model.hh"#include <map>#include <ostream>
```

file **integral\_operator.hh**

```
#include "field_container.hh"#include "grid_base.hh"#include "model_type.hh"
```

file **accumulator.hh**

```
#include "grid_hermitian.hh"#include "integrator.hh"#include "model_type.hh"#include "static_types.hh"#include <array>#include <thrust/iterator/zip_iterator.h>#include <vector>
```

file **element.cpp**

```
#include "element.hh"
```

file **element.hh**

```
#include "tamaas.hh"#include <expolit/expolit>
```

file **integrator.hh**

```
#include "element.hh"#include <expolit/expolit>
```

## Defines

**BOUNDS**

file **kelvin.cpp**

```
#include "kelvin.hh"#include "logger.hh"
```

file **kelvin.hh**

```
#include "grid_hermitian.hh"#include "influence.hh"#include "integration/accumulator.hh"#include "kelvin_helper.hh"#include "model_type.hh"#include "volume_potential.hh"
```

file **kelvin\_helper.hh**

```
#include "grid.hh"#include "grid_hermitian.hh"#include "influence.hh"#include "integration/accumulator.hh"#include "logger.hh"#include "model.hh"#include "model_type.hh"#include <tuple>
```

file **internal.hh**

```
#include "grid.hh"#include <memory>
```

file **isotropic\_hardening.cpp**

```
#include "isotropic_hardening.hh"#include "influence.hh"#include "tamaas.hh"
```

file **isotropic\_hardening.hh**

```
#include "grid.hh"#include "influence.hh"#include "internal.hh"#include "material.hh"#include "model.hh"#include "model_type.hh"#include "static_types.hh"
```

file **linear\_elastic.cpp**

```
#include "linear_elastic.hh"
```

file **linear\_elastic.hh**

```
#include "material.hh"
```

file **material.hh**

```
#include "grid.hh"#include "model.hh"#include "model_type.hh"
```

file **meta\_functional.cpp**

```
#include "meta_functional.hh"
```

file **meta\_functional.hh**

```
#include "functional.hh"#include "tamaas.hh"#include <list>#include <memory>
```

file `mindlin.cpp`

```
#include "mindlin.hh" #include "boussinesq_helper.hh" #include "influence.hh" #include "kelvin_helper.hh" #include "model_type.hh"
```

file `mindlin.hh`

```
#include "grid_hermitian.hh" #include "kelvin.hh" #include "model_type.hh" #include "volume_potential.hh"
```

file `model.cpp`

```
#include "model.hh" #include "be_engine.hh" #include "logger.hh"
```

file `model.hh`

```
#include "be_engine.hh" #include "field_container.hh" #include "grid_base.hh" #include "integral_operator.hh" #include "model_dumper.hh" #include "model_type.hh" #include "tamaas.hh" #include <algorithm> #include <memory> #include <vector>
```

file `model_dumper.hh`

file `model_factory.cpp`

```
#include "model_factory.hh" #include "dcfft.hh" #include "materials/isotropic_hardening.hh" #include "model_template.hh" #include <functional>
```

### Defines

`CAST` (derivative)

file `model_factory.hh`

```
#include "be_engine.hh" #include "model.hh" #include "model_type.hh" #include "residual.hh" #include <vector>
```

file `model_template.cpp`

```
#include "model_template.hh" #include "computes.hh" #include "hooke.hh" #include "influence.hh" #include "kelvin.hh" #include "partitioner.hh" #include "westergaard.hh"
```

### Defines

`CAST` (derivative, ptr)

file `model_template.hh`

```
#include "grid_view.hh" #include "model.hh" #include "model_type.hh"
```

file `model_type.cpp`

```
#include "model_type.hh"
```

file `model_type.hh`

```
#include "grid.hh" #include "grid_base.hh" #include "static_types.hh" #include "tamaas.hh" #include <algorithm> #include <boost/preprocessor/cat.hpp> #include <boost/preprocessor/seq.hpp> #include <boost/preprocessor/stringize.hpp> #include <memory>
```

## Defines

**MODEL\_TYPE\_TRAITS\_MACRO** (type, dim, comp, bdim)

**TAMAAS\_MODEL\_TYPES**

**MAKE\_MODEL\_TYPE** (r, x, type)

**MAKE\_DIM\_TYPE** (r, x, dim)

**PRINT\_MODEL\_TYPE** (r, data, type)

**SWITCH\_DISPATCH\_CASE** (r, data, type)

**SWITCH\_DISPATCH\_CASE** (r, data, dim)

file **residual.cpp**

```
#include "residual.hh" #include "grid_view.hh" #include "model_factory.hh" #include "model_type.hh" #include <list> #include <memory>
```

file **residual.hh**

```
#include "boussinesq.hh" #include "materials/material.hh" #include "mindlin.hh" #include "model_type.hh" #include <unordered_set>
```

file **volume\_potential.cpp**

```
#include "volume_potential.hh" #include "model.hh" #include <algorithm>
```

file **volume\_potential.hh**

```
#include "fft_engine.hh" #include "grid_hermitian.hh" #include "grid_view.hh" #include "integral_operator.hh" #include "logger.hh" #include "model_type.hh" #include <functional>
```

file **westergaard.cpp**

```
#include "grid_hermitian.hh" #include "grid_view.hh" #include "influence.hh" #include "loop.hh" #include "model.hh" #include "model_type.hh" #include "static_types.hh" #include "westergaard.hh" #include <functional> #include <numeric>
```

file **westergaard.hh**

```
#include "fft_engine.hh" #include "grid_hermitian.hh" #include "integral_operator.hh" #include "model_type.hh" #include "tamaas.hh"
```

file **flood\_fill.cpp**

```
#include "flood_fill.hh" #include "partitioner.hh" #include <algorithm> #include <limits> #include <queue>
```

file **flood\_fill.hh**

```
#include "grid.hh" #include <list>
```

file **anderson.cpp**

```
#include "anderson.hh" #include <algorithm> #include <iomanip>
```

file **anderson.hh**

```
#include "epic.hh"#include <deque>
```

file **beck\_teboulle.cpp**

```
#include "beck_teboulle.hh"#include "logger.hh"#include <iomanip>
```

file **beck\_teboulle.hh**

```
#include "kato.hh"
```

file **condat.cpp**

```
#include "condat.hh"#include "logger.hh"#include <iomanip>
```

file **condat.hh**

```
#include "kato.hh"
```

file **contact\_solver.cpp**

```
#include "contact_solver.hh"#include "logger.hh"#include <iomanip>#include <iostream>
```

file **contact\_solver.hh**

```
#include "meta_functional.hh"#include "model.hh"#include "tamaas.hh"
```

file **dfsane\_solver.cpp**

```
#include "dfsane_solver.hh"
```

file **dfsane\_solver.hh**

```
#include "ep_solver.hh"#include "grid_base.hh"#include "residual.hh"#include <deque>#include <functional>#include <utility>
```

file **ep\_solver.cpp**

```
#include "ep_solver.hh"#include "model_type.hh"
```

file **ep\_solver.hh**

```
#include "grid_base.hh"#include "residual.hh"
```

file **epic.cpp**

```
#include "epic.hh"#include "logger.hh"
```

file **epic.hh**

```
#include "contact_solver.hh"#include "ep_solver.hh"#include "model.hh"
```

file **kato.cpp**

```
#include "kato.hh"#include "elastic_functional.hh"#include "logger.hh"#include "loop.hh"#include <iomanip>#include <iostream>#include <iterator>
```

file **kato.hh**

```
#include "contact_solver.hh"#include "meta_functional.hh"#include "model_type.hh"#include "static_types.hh"#include "tamaas.hh"
```

file **kato\_saturated.cpp**

```
#include "kato_saturated.hh"#include "logger.hh"#include <iomanip>#include <limits>
```

file **kato\_saturated.hh**

```
#include "polonsky_keer_rey.hh"#include <limits>
```

file **maxwell\_viscoelastic.cpp**

```
#include "maxwell_viscoelastic.hh"#include "logger.hh"#include "loop.hh"#include "model.hh"#include "model_type.hh"
```

file **maxwell\_viscoelastic.hh**

```
#include "polonsky_keer_rey.hh"#include "westergaard.hh"
```

file **snes.cpp**

```
#include "snes.hh"#include <petscsystypes.h>
```

### Defines

**chk** (error)

file **snes.hh**

```
#include "ep_solver.hh"#include "residual.hh"#include <petscmat.h>#include <petscoptions.h>#include <petsc-snes.h>#include <petscsys.h>#include <petscvec.h>#include <string>#include <vector>
```

file **tao.cpp**

```
#include "tao.hh"#include "model_type.hh"#include <iomanip>
```

### Defines

**chk** (error)

**PRECONDITION**

file **tao.hh**

```
#include "polonsky_keer_rey.hh"#include <petscmat.h>#include <petscoptions.h>#include <petscsys.h>#include <petsctao.h>#include <petscvec.h>#include <string>#include <vector>
```

file **polonsky\_keer\_rey.cpp**

```
#include "polonsky_keer_rey.hh"#include "elastic_functional.hh"#include "logger.hh"#include "loop.hh"#include "model_type.hh"#include <iomanip>
```

file **polonsky\_keer\_rey.hh**

```
#include "contact_solver.hh"#include "grid_view.hh"#include "meta_functional.hh"#include "westergaard.hh"
```

### Defines

**WESTERGAARD** (type, kind, desc)

file **polonsky\_keer\_tan.cpp**

```
#include "polonsky_keer_tan.hh"#include <iomanip>
```

file **polonsky\_keer\_tan.hh**

```
#include "kato.hh"
```

file **filter.hh**

```
#include "fft_engine.hh"#include "grid.hh"#include "grid_hermitian.hh"
```

file **isopowerlaw.cpp**

```
#include "isopowerlaw.hh"#include <map>
```

file **isopowerlaw.hh**

```
#include "filter.hh"#include "grid_hermitian.hh"#include "static_types.hh"
```

file **regularized\_powerlaw.cpp**

```
#include "regularized_powerlaw.hh"
```

file **regularized\_powerlaw.hh**

```
#include "filter.hh"#include "grid_hermitian.hh"#include "static_types.hh"
```

file **surface\_generator.cpp**

```
#include "surface_generator.hh"#include "partitioner.hh"#include <algorithm>
```

file **surface\_generator.hh**

```
#include "grid.hh"#include <array>
```

file **surface\_generator\_filter.cpp**

```
#include "surface_generator_filter.hh"#include <iostream>
```

file **surface\_generator\_filter.hh**

```
#include "fft_engine.hh"#include "filter.hh"#include "partitioner.hh"#include "surface_generator.hh"#include "tamaas.hh"
```

file **surface\_generator\_random\_phase.cpp**

```
#include "surface_generator_random_phase.hh"#include <iostream>
```

*file* **surface\_generator\_random\_phase.hh**

*#include* "filter.hh" *#include* "surface\_generator\_filter.hh" *#include* "tamaas.hh"

*file* **tamaas\_info.hh**

*#include* <string>

*dir* /home/docs/checkouts/readthedocs.org/user\_builds/tamaas/checkouts/latest/  
**src/core**

*dir* /home/docs/checkouts/readthedocs.org/user\_builds/tamaas/checkouts/latest/  
**src/core/cuda**

*dir* /home/docs/checkouts/readthedocs.org/user\_builds/tamaas/checkouts/latest/  
**src/core/fftw**

*dir* /home/docs/checkouts/readthedocs.org/user\_builds/tamaas/checkouts/latest/  
**src/model/integration**

*dir* /home/docs/checkouts/readthedocs.org/user\_builds/tamaas/checkouts/latest/  
**src/core/loops**

*dir* /home/docs/checkouts/readthedocs.org/user\_builds/tamaas/checkouts/latest/  
**src/model/materials**

*dir* /home/docs/checkouts/readthedocs.org/user\_builds/tamaas/checkouts/latest/  
**src/model**

*dir* /home/docs/checkouts/readthedocs.org/user\_builds/tamaas/checkouts/latest/  
**src/core/fftw/mpi**

*dir* /home/docs/checkouts/readthedocs.org/user\_builds/tamaas/checkouts/latest/  
**src/percolation**

*dir* /home/docs/checkouts/readthedocs.org/user\_builds/tamaas/checkouts/latest/  
**src/solvers/petsc**

*dir* /home/docs/checkouts/readthedocs.org/user\_builds/tamaas/checkouts/latest/  
**src/solvers**

*dir* /home/docs/checkouts/readthedocs.org/user\_builds/tamaas/checkouts/latest/**src**

*dir* /home/docs/checkouts/readthedocs.org/user\_builds/tamaas/checkouts/latest/  
**src/surface**

*page* **index**

## 11.2.1 Introduction

Tamaas is a spectral-integral-equation based contact library. It is made with love to be fast and friendly!

**Author**

Lucas Frérot [lucas.frerot@sorbonne-universite.fr](mailto:lucas.frerot@sorbonne-universite.fr)

**Author**

Guillaume Anciaux [guillaume.anciaux@epfl.ch](mailto:guillaume.anciaux@epfl.ch)

**Author**

Valentine Rey [valentine.rey@univ-nantes.fr](mailto:valentine.rey@univ-nantes.fr)

**Author**

Son Pham-Ba [son.phamba@epfl.ch](mailto:son.phamba@epfl.ch)

**Author**

Zichen Li [zichen.li@dalembert.upmc.fr](mailto:zichen.li@dalembert.upmc.fr)

**Author**

Jean-François Molinari [jean-francois.molinari@epfl.ch](mailto:jean-francois.molinari@epfl.ch)

## 11.2.2 License

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## INDICES AND TABLES

- genindex
- modindex
- search



## PYTHON MODULE INDEX

### t

tamaas, [41](#)  
tamaas.\_tamaas, [41](#)  
tamaas.\_tamaas.compute, [67](#)  
tamaas.\_tamaas.mpi, [67](#)  
tamaas.dumpers, [68](#)  
tamaas.nonlinear\_solvers, [70](#)  
tamaas.utils, [72](#)